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ZGOUBI USERS' GUIDE

Latest version : https://sourceforge.net/p/zgoubi/code/HEAD/tree/trunk/guide/Zgoubi.pdf Zgoubi on web : http://sourceforge.net/projects/zgoubi/

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Spin Flip During Acceleration Ramp AGS With Partial Snakes



Snake Resonance Crossing in RHIC



An Ergodic Approach of Polarization Lifetime in the EIC Electron Storage Ring



Cover figures

- Top: spin precession in a cyclotron [1],
- Bottom:

upper left : collision optics at ATLAS and CMS [82],

upper right : average bunch polarization upon crossing of $393+Q_y$ spin resonance in RHIC [15],

lower left : spin-flipping at integer $G\gamma$ during acceleration in the AGS with two partial snakes [14],

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		AUTOREF. Transport beam have reference frame
		DEAMIDEAMI . Dealli-Dealli lelis
		DEND : Defining magnet, Cartesian frame
		BETATION : Betatron core (momentum kick)
		BREVOL: I-D uniform mesh magnetic field map
		CARTEMES: 2-D Cartesian uniform mesh magnetic field map
		CAVITE: Accelerating cavity
		CHAMBR : Long transverse aperture limitation
		CHANGREF : Transformation to a new reference frame
		CIBLE or TARGET : Generate a secondary beam following target interaction
		COLLIMA : Collimator
		CYCLOTRON : Spiral setor cyclotron
		DECAPOLE : Decapole magnet
		DIPOLE : Dipole magnet, polar frame
		DIPOLE-M : Generation of dipole mid-plane 2-D map, polar frame
		DIPOLES : Dipole magnet N-tuple, polar frame
		EBMULT : Electro-magnetic multipole
		FFAG : FFAG magnet, <i>N</i> -tuple
		OCTUPOLE : Octupole magnet
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		GOTO : Branching statement
		INCLUDE : File include statement
		MCDESINT : Monte-Carlo simulation of in-flight decay
		OPTICS : Write out optical functions. Log to zgoubi.OPTICS.out
		OPTIONS : Global or special options
		ORDRE : Taylor expansions order
		PARTICUL : Particle characteristics
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PART A

Description of software contents

Available keywords and where they are to be found in Part A

AGSMM	AGS main magnet	67
AGSQUAD	AGS quadrupole	68
AIMANT	Generation of dipole mid-plane 2-D map, polar frame	69
AUTOREF	Transport beam into a new reference frame	74
BEAMBEAM	Beam-beam lens	75
BEND	Bending magnet, Cartesian frame	76
BETATRON	Betatron core (momentum kick)	
BINARY	BINARY↔FORMATTED data converter	153
BREVOL	1-D uniform mesh magnetic field map	79
CARTEMES	2-D Cartesian uniform mesh magnetic field map	80
CAVITE	Accelerating cavity	
CHAMBR	Long transverse aperture limitation	88
CHANGREF	Transformation to a new reference frame	89
CIBLE	Generate a secondary beam following target interaction	91
COLLIMA	Collimator	92
CYCLOTRON	Spiral setor cyclotron	93
DECAPOLE	Decapole magnet	95
DIPOLE	Dipole magnet, polar frame	96
DIPOLE-M	Generation of dipole mid-plane 2-D map, polar frame	
DIPOLES	Dipole magnet N-tuple, polar frame	101
DODECAPO	Dodecapole magnet	105
DRIFT	Field free drift space	106
EBMULT	Electro-magnetic multipole	107
EL2TUB	Two-tube electrostatic lens	108
ELCYLDEF	Electrostatic cylindrical deflector	109
ELMIR	Electrostatic N-electrode mirror/lens, straight slits	110
ELMIRC	Electrostatic N-electrode mirror/lens, circular slits	111
ELMULT	Electric multipole	112
ELREVOL	1-D uniform mesh electric field map	114
EMMA	2-D Cartesian or cylindrical mesh field map for EMMA FFAG	115
END	End of input data list	154
ERRORS	Injecting errors in optical elements	155
ESL	Field free drift space	106
FAISCEAU	Print particle coordinates	191
FAISCNL	Store particle coordinates in file FNAME	191
FAISTORE	Store coordinates every <i>IP</i> other pass at labeled elements	191
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FIN	End of input data list	154
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GASCAT	Gas scattering	165
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MCDESINT	Monte-Carlo simulation of in-flight decay	. 169
MCOBJET	Monte-Carlo generation of a 6-D object	58
MULTIPOL	Magnetic multipole	. 127
OBJET	Generation of an object	61
OBJETA	Object from Monte-Carlo simulation of decay reaction	65
OCTUPOLE	Octupole magnet	. 128
OPTICS	Write out optical functions. Log to zgoubi.OPTICS.out	. 171
OPTIONS	Global or special options	. 172
ORDRE	Taylor expansions order	. 173
PARTICUL	Particle characteristics	. 174
PICKUPS	Bunch centroid path; orbit	. 199
PLOTDATA	Intermediate output for the PLOTDATA graphic software	. 200
POISSON	Read magnetic field data from POISSON output	. 129
POLARMES	2-D polar mesh magnetic field map	. 130
PS170	Simulation of a round shape dipole magnet	. 131
QUADISEX	Sharp edge magnetic multipoles	. 132
QUADRUPO	Quadrupole magnet	.133
REBELOTE	'Do it again'	. 175
RESET	Reset counters and flags	.177
SCALING	Power supplies and R.F. function generator	. 178
SEPARA	Wien Filter - analytical simulation	. 135
SEXQUAD	Sharp edge magnetic multipole	. 132
SEXTUPOL	Sextupole magnet	. 136
SOLENOID	Solenoid	137
SPACECHARG	Space charge	.182
SPINR	Spin rotation	. 139
SPNPRNL	Store spin coordinates into file FNAME	. 201
SPNPRT	Print spin coordinates	. 202
SPNSTORE	Store spin coordinates every <i>IP</i> other pass at labeled elements	.201
SPNTRK	Spin tracking switch, and spin coordinate initialization	. 183
SRLOSS	Synchrotron radiation energy loss	. 185
SRPRNT	Print SR loss statistics	. 203
SVDOC	SVD orbit correction	. 186
SYNRAD	Synchrotron radiation spectral-angular densities	. 188
SYSTEM	System call	. 189
TARGET	Generate a secondary beam following target interaction	91
TOSCA	2-D and 3-D Cartesian or cylindrical mesh field map	. 140
TRANSMAT	Matrix transfer	. 144
TRAKOT	Iranslation-Rotation of the reference frame	. 145
TWISS	Compute periodic optical parameters. Log to zgoubi.TWISS.out	. 204

UNDULATOR	Undulator magnet	146
UNIPOT	Unipotential cylindrical electrostatic lens	147
VENUS	Simulation of a rectangular shape dipole magnet	. 148
VFFA	Simulation of a VFFA dipole, or series of	. 149
WIENFILT	Wien filter	. 150
YMY	Reverse signs of Y and Z reference axes	.151

Optical Elements Versus Keywords

What can be simulated What keyword(s) can be used for that

This glossary gives a list of keywords suitable for the simulation of common optical elements. These are classified in three categories: magnetic, electric and combined electro-magnetic elements.

Field map procedures are also listed; they provide a means for ray-tracing through measured or simulated electric and/or magnetic fields.

MAGNETIC ELEMENTS

AGS main magnet	AGSMM
Betatron core	BETATRON, CAVITE
Cyclotron magnet or sector	DIPOLE[S], DIPOLE-M, FFAG, FFAG-SPI
Decapole	DECAPOLE, MULTIPOL
Dipole[s], spectrometer dipole	AIMANT, BEND, DIPOLE[S][-M], MULTIPOL, QUADISEX
Dodecapole	DODECAPO, MULTIPOL
FFAG magnet	DIPOLES, FFAG, FFAG-SPI, MULTIPOL
Helical dipole	HELIX
Multipole	MULTIPOL, QUADISEX, SEXQUAD
Octupole	OCTUPOLE, MULTIPOL, QUADISEX, SEXQUAD
Quadrupole	QUADRUPO, MULTIPOL, SEXQUAD, AGSQUAD
Sextupole	SEXTUPOL, MULTIPOL, QUADISEX, SEXQUAD
Skew multipoles	MULTIPOL
Solenoid	SOLENOID
Spectrometer dipole	DIPOLE, DIPOLE-M, DIPOLES
Undulator	UNDULATOR

Using field maps

1-D, cylindrical symmetry	BREVOL
2-D, mid-plane symmetry	CARTEMES, POISSON, TOSCA
2-D, no symmetry	MAP2D
2-D, polar mesh, mid-plane symmetry	POLARMES
3-D, no symmetry	TOSCA
EMMA FFAG quadrupole doublet	EMMA
linear composition of field maps	TOSCA

ELECTRIC ELEMENTS

2-tube (bipotential) lens	EL2TUB
3-tube (unipotential) lens	UNIPOT
Decapole	ELMULT
Dipole	ELMULT
Dodecapole	ELMULT
Multipole	ELMULT
N-electrode mirror/lens, straight slits	ELMIR
N-electrode mirror/lens, circular slits	ELMIRC
Octupole	ELMULT

Ouadrupole	ELMULT
R.F. (kick) cavity	CAVITE
Sextupole	ELMULT
Skew multipoles	ELMULT

Using field maps

1-D, cylindrical symmetry	ELREVOL
2-D, no symmetry	MAP2D-E

ELECTRO-MAGNETIC ELEMENTS

Decapole	EBMULT
Dipole	EBMULT
Dodecapole	EBMULT
Multipole	EBMULT
Octupole	EBMULT
Quadrupole	EBMULT
Sextupole	EBMULT
Skew multipoles	EBMULT
Wien filter	SEPARA, WIENFILT

PREFACE TO THE BNL EDITION, 2015+

New functionalities have been introduced :

- GOTO keyword, a conditional goto, useful for RLA simulations,

- *INCLUDE* keyword, working like the Fortran, similar as well to latex's, "include", more or less equivalent to a "call file" as found in various optics codes, useful for long or repetitive sequences. The developed optical sequence is printed out, in the first place, in zgoubi.res. The latter can be run as is, as the '*END*' or '*FIN*' statement which concludes an input sequence causes the execution to ignore whatever follows in that zgoubi.res listing.

PREFACE TO THE BNL EDITION, 2012

The previous release of the Zgoubi Users' Guide as a Lab. report dates from 1997, making the present one the latest in a series of five [2]-[5].

zgoubi has undergone substantial developments since the 4th edition of the Users' Guide, in the frame of a number of projects and of beam dynamics studies, as the Neutrino Factory, lepton and hadron colliders, spin dynamics investigations at SuperB, RHIC, etc. As well the list of optical elements has grown, and so did the "Glossary of Keywords" list, pp. 9 and 219, including new simulation and computing procedures, which range from constraint-matching to overlapping magnetic fields capabilities to spin manipulations and other synchrotron radiation damping recipes.

The ouput files zgoubi.fai (local particle data) and zgoubi.plt (step-by-step-particle data across an optical element) have been reformated in columns, making them readily readable by graphic programs as "gnuplot". Ancillary output files, less voluminous than the latter two and useful for producing plots or for zgoubi functioning checks/debugging, with names of the form "zgoubi.*.out" are available from various keywords, usually by specifying "PRINT" in the keyword's arguments, for instance in the case of "CAVITE" it will produce "zgoubi.CAVITE.Out" containing time dependence of RF parameters as experienced by the particles at traversal of the cavity, whereas "zgoubi.OPTICS.out" can be obtained from *OPTICS* keyword.

This evolution of **zgoubi** allows embedding "*FIT*[2]" procedure within "*REBELOTE*" (**zgoubi**'s Doloop), whereas the latter has been confered the capability of changing values of any numerical data across zgoubi.dat. This allows parameter scans, while possibly using "*SYSTEM*" to store the outcomes in dedicated external files.

A series of auxiliary computing tools and graphic tools (the latter based on "gnuplot") have been developed, aimed at making the designer's life easier, as, search for closed orbits in periodic machines, computation of optical functions and parameters, tune scans, dynamic aperture scans, spin dynamics data treatment, graphic scripts, etc., and including dedicated ones regarding, *e.g.*, FFAG and cyclotron design, AGS and RHIC studies, synchrotron radiation energy losses and their effects. In addition "python" interfaces are being developed by several users, possibly made available on web by their authors.

The code has been installed on SourceForge with the collaboration of J. S. Berg, in Sept. 2007, there it is fully and freely available [6]. The SourceForge package evolves and is maintained at the pace of on-going projects and design studies. It includes the source files, the post-processor program **zpop**, as well as many examples with their input data files ("zgoubi.dat") and output result files ("zgoubi.res") and the auxiliary toolbox.

The Users' Guide is intended to describe the contents of the most recent version of **zgoubi**. The code and its Guide are both far from being "finished products".

J. S. Berg and N. Tsoupas, BNL, have reviewed the final proof of the present document.

INTRODUCTION TO THE 4th EDITION, 1997

The initial version of **zgoubi**, dedicated to ray-tracing in magnetic fields, was developed by D. Garetta and J.C. Faivre at CEN-Saclay in the early 1970s. It was perfected for the purpose of studying the four spectrometers SPES I, II, III, IV at the Laboratoire National SATURNE (CEA-Saclay, France), and SPEG at GANIL (Caen, France). It is being used since long in several national and foreign laboratories.

The first manual was in French [2]. Accounting for many developments and improvements, and in order to facilitate access to the program an English version of the manual was written at TRIUMF with the assistance of J. Doornbos. P. Stewart prepared the manuscript for publication [3]

An updating of the latter was necessary for accompanying the third version of the code which included developments regarding spin tracking and ray-tracing in combined electric and magnetic fields; this was done with the help of D. Bunel (SATURNE Laboratory, Saclay) for the preparation of the document and lead to the third release [4].

In the mid-1990s, the computation of synchrotron radiation electromagnetic impulse and spectra was introduced for the purpose of studying interference effects at the LEP synchrotron radiation based diagnostic mini-wiggler. In the mean time, several new optical elements were added, such as electro-magnetic and other electrostatic lenses. Used since several years for special studies in periodic machines (*e.g.*, SATURNE at Saclay, COSY at Julich, LEP and LHC at CERN, Neutrino Factory rings), **zgoubi** has also undergone extensive developments regarding storage ring related features.

These developments of **zgoubi** have strongly benefited of the environment of the Groupe Théorie, Laboratoire National SATURNE, CEA/DSM-Saclay, in the years 1985-1995.

The graphic interface to **zgoubi** (addressed in Part D) has also undergone concomitant extensive developments, which make it a performing tool for the post-processing of **zgoubi** outputs.

The Users' Guide is intended to describe the contents of the most recent version of **zgoubi**, which is far from being a "finished product".

INTRODUCTION

The computer code **zgoubi** calculates trajectories of charged particles in magnetic and electric fields. At the origin specially adapted to the definition and adjustment of beam lines and magnetic spectrometers, it has so evolved that it allows the study of systems including complex sequences of optical elements such as dipoles, quadrupoles, arbitrary multipoles, FFAG magnets and other magnetic or electric devices, and is able as well to handle periodic structures. Compared to other codes, it presents several peculiarities, as follows - a non-exhaustive list :

- a numerical method for integrating the Lorentz equation, based on Taylor series, which optimizes computing time and provides high accuracy and strong symplecticity,
- spin tracking, using the same numerical method as for the Lorentz equation,
- account of stochastic photon emission, and its effects on particle dynamics,
- calculation of the synchrotron radiation electric field and spectra in arbitrary magnetic fields, from the ray-tracing outcomes,
- the possibility of using a mesh, which allows ray-tracing from simulated or measured (1-D, 2-D or 3-D) electric and magnetic field maps,
- a number Monte Carlo procedures : unlimited number of trajectories, in-flight decay, stochastic radiation, etc.,
- built-in fitting procedures allowing arbitrary variables and a large variety of constraints, easily expandable,
- multi-turn tracking in circular accelerators including features proper to machine parameter calculation and survey,
- simulation of time-varying power supplies,
- simulation of arbitrary radio-frequency programs.

The initial version of **zgoubi** was dedicated to ray-tracing in magnetic elements, beam lines, spectrometers. It was perfected for the purpose of studying, and operating, the four spectrometers SPES I, II, III, IV at the Laboratoire National SATURNE (CEA-Saclay, France), and, later, SPEG at GANIL (Caen, France).

Developments regarding spin tracking and ray-tracing in combined electric and magnetic fields were implemented, in the late 1980s and early 1990s respectively.

In the mid-1990s, the computation of synchrotron radiation electromagnetic impulse and spectra was introduced, for the purpose of synchrotron radiation diagnostic R&D at LEP, and further applied to the design of the Synchrotron radiation diagnostics installations at LHC in the early 2000s. In the mean time, several new optical elements were added, such as electro-magnetic and other electrostatic lenses. Used since several years for special studies in periodic machines (*e.g.*, SATURNE at Saclay, COSY at Julich, LEP and LHC at CERN), **zgoubi** has also undergone extensive developments regarding storage ring related features.

Many developments have been accomplished since the early 2000s in the frame of a number of project design and beam dynamics studies, as the neutrino factory, lepton and hadron colliders, spin studies at AGS and RHIC, etc. As a consequence the list of optical elements and the compendium of numerical methods, so-called "Glossary of Keywords" list, pp. 9 and 219, has stretched with new simulation and computing procedures, ranging from fitting (*FIT2* procedure ; additional constraints) to overlapping magnetic field capabilities (*DIPOLES*, *FFAG*), spin manipulation (*SPINR*), optical elements (*BEAMBEAM*), radiation damping tools (*SRLOSS*) and many others (*FAISTORE*, *MAP2D-E*, *OPTICS*, *PICKUPS*, *TWISS*, etc.).

The graphic interface to **zgoubi** (**zpop**, Part D) has undergone extensive developments, making it a convenient companion tool to the use of **zgoubi**.

1 NUMERICAL CALCULATION OF MOTION AND FIELDS

1.1 zgoubi Frame

The reference frame of **zgoubi** is presented in Fig. 1. Its origin and orientation are arbitrary. However, its origin is generally in the median plane, considered to be (O; X, Y).

In optical elements defined in a Cartesian frame, OX gnerally coincides with the optical axis of the element (for instance, the longitudinal axis in a multipole). In optical elements defined in a polar frame, OX is tangent to a reference arc (for instance, a circle with reference radius RM in a bending magnet) and the (O; X, Y) frame moves with the particle (located in the (Y,Z) plane) across the optical element.

1.2 Integration of the Lorentz Equation

The Lorentz equation, which governs the motion of a particle of charge q, relativistic mass m and velocity \vec{v} in electric and magnetic fields \vec{e} and \vec{b} , is written

$$\frac{d(m\vec{v})}{dt} = q\left(\vec{e} + \vec{v} \times \vec{b}\right) \tag{1.2.1}$$

Noting $()' = \frac{d()}{ds}$ and taking

$$\vec{u} = \frac{\vec{v}}{v}, \quad ds = v \, dt \,, \quad \vec{u}' = \frac{d\vec{u}}{ds} \,, \quad m\vec{v} = mv\vec{u} = q \, B\rho \, \vec{u} \tag{1.2.2}$$

where $B\rho$ is the rigidity of the particle, this equation can be rewritten

$$(B\rho)'\vec{u} + B\rho\vec{u}' = \frac{\vec{e}}{v} + \vec{u} \times \vec{b}$$
(1.2.3)

From position $\vec{R}(M_0)$ and unit velocity $\vec{u}(M_0)$ at point M_0 , position $\vec{R}(M_1)$ and unit velocity $\vec{u}(M_1)$ at point M_1 following a displacement Δs , are obtained from truncated Taylor expansions (Fig. 2)

$$\vec{R}(M_1) \approx \vec{R}(M_0) + \vec{u}(M_0)\,\Delta s + \vec{u}'(M_0)\,\frac{\Delta s^2}{2!} + \dots + \vec{u}''''(M_0)\,\frac{\Delta s^6}{6!}$$

$$\vec{u}(M_1) \approx \vec{u}(M_0) + \vec{u}'(M_0)\,\Delta s + \vec{u}''(M_0)\,\frac{\Delta s^2}{2!} + \dots + \vec{u}'''''(M_0)\,\frac{\Delta s^5}{5!}$$
(1.2.4)

The rigidity at M_1 , in case it varies (in electric fields), is obtained in a similar manner using

$$(B\rho)(M_1) \approx (B\rho)(M_0) + (B\rho)'(M_0)\Delta s + \dots + (B\rho)''''(M_0)\frac{\Delta s^5}{5!}$$
(1.2.5)

The equation of time of flight is written in a similar manner

$$T(M_1) \approx T(M_0) + T'(M_0) \Delta s + T''(M_0) \frac{\Delta s^2}{2} + \dots + T''''(M_0) \frac{\Delta s^5}{5!}$$
(1.2.6)

The derivatives $\vec{u}^{(n)} = \frac{d^n \vec{u}}{ds^n}$ and $(B\rho)^{(n)} = \frac{d^n (B\rho)}{ds^n}$ involved in these expressions are calculated as described in the next sections. For the sake of computing speed, three distinct software procedures are involved, depending on whether \vec{e} or \vec{b} is zero, or \vec{e} and \vec{b} are both non-zero.



Figure 1: Reference frame and coordinates (Y, T, Z, P) in **zgoubi**.

Reference curve: a staight axis in optical elements defined in a Cartesian frame; an arc of a circle in optical elements defined in a cylindrical frame.

OX: in the direction of motion, tangent to the Reference curve,

OY : normal to OX,

OZ : orthogonal to the $(\boldsymbol{X},\boldsymbol{Y})$ plane,

- \vec{W} : projection of the velocity, \vec{v} , in the (X, Y) plane,
- T = angle between \vec{W} and the X-axis,
- P = angle between \vec{W} and \vec{v} .



Figure 2: Position and velocity of a particle in the reference frame.

1.2.1 Integration in Magnetic Fields

Considering $\vec{e} = 0$ and given $\vec{B} = \frac{\vec{b}}{B\rho}$, eq. (1.2.3) reduces to $\vec{u}' = \vec{u} \times \vec{B}$

The successive derivatives
$$\vec{u}^{(n)} = \frac{d^n \vec{u}}{ds^n}$$
 of \vec{u} needed in the Taylor expansions (eqs. 1.2.4) are calculated by differentiating $\vec{u}' = \vec{u} \times \vec{B}$

$$\vec{u}'' = \vec{u}' \times \vec{B} + \vec{u} \times \vec{B}'$$

$$\vec{u}''' = \vec{u}'' \times \vec{B} + 2\vec{u}' \times \vec{B}' + \vec{u} \times \vec{B}''$$

$$\vec{u}'''' = \vec{u}''' \times \vec{B} + 3\vec{u}'' \times \vec{B}' + 3\vec{u}' \times \vec{B}'' + \vec{u} \times \vec{B}'''$$

$$\vec{u}''''' = \vec{u}'''' \times \vec{B} + 4\vec{u}''' \times \vec{B}' + 6\vec{u}'' \times \vec{B}'' + 4\vec{u}' \times \vec{B}''' + \vec{u} \times \vec{B}'''$$
(1.2.8)

where $\vec{B}^{(n)} = \frac{d^n \vec{B}}{ds^n}$. From

$$d\vec{B} = \frac{\partial \vec{B}}{\partial X} dX + \frac{\partial \vec{B}}{\partial Y} dY + \frac{\partial \vec{B}}{\partial Z} dZ = \sum_{i=1,3} \frac{\partial \vec{B}}{\partial X_i} dX_i$$
(1.2.9)

and by successive differentiation, we get

$$\vec{B}' = \sum_{i} \frac{\partial \vec{B}}{\partial X_{i}} u_{i}$$

$$\vec{B}'' = \sum_{ij} \frac{\partial^{2} \vec{B}}{\partial X_{i} \partial X_{j}} u_{i} u_{j} + \sum_{i} \frac{\partial \vec{B}}{\partial X_{i}} u_{i}'$$

$$\vec{B}''' = \sum_{ijk} \frac{\partial^{3} \vec{B}}{\partial X_{i} \partial X_{j} \partial X_{k}} u_{i} u_{j} u_{k} + 3 \sum_{ij} \frac{\partial^{2} \vec{B}}{\partial X_{i} \partial X_{j}} u_{i}' u_{j} + \sum_{i} \frac{\partial \vec{B}}{\partial X_{i}} u_{i}'$$

$$\vec{B}'''' = \sum_{ijkl} \frac{\partial^{4} \vec{B}}{\partial X_{i} \partial X_{j} \partial X_{k} \partial X_{l}} u_{i} u_{j} u_{k} u_{l} + 6 \sum_{ijk} \frac{\partial^{3} \vec{B}}{\partial X_{i} \partial X_{j} \partial X_{k}} u_{i}' u_{j} u_{k}$$

$$+ 4 \sum_{ij} \frac{\partial^{2} \vec{B}}{\partial X_{i} \partial X_{j}} u_{i}'' u_{j} + 3 \sum_{ij} \frac{\partial^{2} \vec{B}}{\partial X_{i} \partial X_{j}} u_{i}' u_{j}' + \sum_{i} \frac{\partial \vec{B}}{\partial X_{i}} u_{i}''$$
(1.2.10)

From the knowledge of $\vec{u}(M_0)$ and $\vec{B}(M_0)$ at point M_0 of the trajectory, we calculate alternately the derivatives of $\vec{u}(M_0)$ and $\vec{B}(M_0)$, by means of eqs. (1.2.8) and (1.2.10), and inject these into eq. (1.2.4) so yielding $\vec{R}(M_1)$ and $\vec{u}(M_1)$.

1.2.2 Integration in Electric Fields [7]

Admitting that $\vec{b} = 0$, eq. (1.2.3) reduces to

$$(B\rho)'\vec{u} + B\rho\vec{u}' = \frac{\vec{e}}{v}$$
(1.2.11)

(1.2.7)

which, by successive differentiations, gives the recursive relations

$$(B\rho)'\vec{u} + B\rho\vec{u}' = \frac{\vec{e}}{v}$$

$$(B\rho)''\vec{u} + 2(B\rho)'\vec{u}' + B\rho\vec{u}'' = \left(\frac{1}{v}\right)'\vec{e} + \frac{\vec{e}'}{v}$$

$$(B\rho)'''\vec{u} + 3(B\rho)''\vec{u}' + 3(B\rho)'\vec{u}'' + B\rho\vec{u}''' = \left(\frac{1}{v}\right)''\vec{e} + 2\left(\frac{1}{v}\right)'\vec{e}' + \left(\frac{1}{v}\right)\vec{e}''$$

$$(B\rho)''''\vec{u} + 4(B\rho)'''\vec{u}' + 6(B\rho)''\vec{u}'' + 4(B\rho)'\vec{u}''' + B\rho\vec{u}'''' = \left(\frac{1}{v}\right)''\vec{e} + 3\left(\frac{1}{v}\right)''\vec{e}' + 3\left(\frac{1}{v}\right)'\vec{e}'' + \frac{1}{v}\vec{e}'''$$

$$(B\rho)'''''\vec{u} + 5(B\rho)''''\vec{u}' + etc.$$

$$(1.2.12)$$

that provide the derivatives $\frac{d^n \vec{u}}{ds^n}$ needed in the Taylor expansions (eq. 1.2.4)

$$\vec{u}' = \left(\frac{1}{v}\right) \vec{E} - \frac{(B\rho)'}{B\rho} \vec{u}$$

$$\vec{u}''' = \left(\frac{1}{v}\right)' \vec{E} + \left(\frac{1}{v}\right) \vec{E}'|_{B\rho} - 2\frac{(B\rho)'}{B\rho} \vec{u}' - \frac{(B\rho)''}{B\rho} \vec{u}$$

$$\vec{u}'''' = \left(\frac{1}{v}\right)'' \vec{E} + 2\left(\frac{1}{v}\right)' \vec{E}'|_{B\rho} + \frac{1}{v} \vec{E}''|_{B\rho} - 3\frac{(B\rho)'}{B\rho} \vec{u}'' - 3\frac{(B\rho)''}{B\rho} \vec{u}' - \frac{(B\rho)'''}{B\rho} \vec{u}$$

$$\vec{u}'''' = \left(\frac{1}{v}\right)''' \vec{E} + 3\left(\frac{1}{v}\right)'' \vec{E}'|_{B\rho} + 3\left(\frac{1}{v}\right)' \vec{E}''|_{B\rho} + \left(\frac{1}{v}\right) \vec{E}'''|_{B\rho}$$

$$-4\frac{(B\rho)'}{B\rho} \vec{u}''' - 6\frac{(B\rho)''}{B\rho} \vec{u}'' - 4\frac{(B\rho)'''}{B\rho} \vec{u}' - \frac{(B\rho)''''}{B\rho} \vec{u}$$

$$\vec{u}''''' = \left(\frac{1}{v}\right)'''' \vec{E} + 4\left(\frac{1}{v}\right)''' \vec{E}'|_{B\rho} + 6\left(\frac{1}{v}\right)'' \vec{E}''|_{B\rho} + 4\left(\frac{1}{v}\right)' \vec{E}'''|_{B\rho} + \left(\frac{1}{v}\right) \vec{E}''''|_{B\rho}$$

$$-5\frac{(B\rho)'}{B\rho} \vec{u}''' - 10\frac{(B\rho)''}{B\rho} \vec{u}''' - 10\frac{(B\rho)'''}{B\rho} \vec{u}'' - 5\frac{(B\rho)''''}{B\rho} \vec{u}' - \frac{(B\rho)''''}{B\rho} \vec{u}$$

where $\vec{E} = \frac{\vec{e}}{B\rho}$, and $()^{(n)}|_{B\rho}$ denotes differentiation at constant $B\rho : \vec{E}^{(n)}|_{B\rho} = \frac{1}{B\rho} \frac{d^n \vec{e}}{ds^n}$. These derivatives of the electric field are obtained from the total derivative

$$d\vec{E} = \frac{\partial \vec{E}}{\partial X} dX + \frac{\partial \vec{E}}{\partial Y} dY + \frac{\partial \vec{E}}{\partial Z} dZ$$
(1.2.14)

by successive differentiations

$$\vec{E}' = \sum_{i} \frac{\partial \vec{E}}{\partial X_{i}} u_{i}$$

$$\vec{E}'' = \sum_{ij} \frac{\partial^{2} \vec{E}}{\partial X_{i} \partial X_{j}} u_{i} u_{j} + \sum_{i} \frac{\partial \vec{E}}{\partial X_{i}} u_{i}'$$

$$\vec{E}''' = \sum_{ijk} \frac{\partial^{3} \vec{E}}{\partial X_{i} \partial X_{j} \partial X_{k}} u_{i} u_{j} u_{k} + 3 \sum_{ij} \frac{\partial^{2} \vec{E}}{\partial X_{i} \partial X_{j}} u_{i}' u_{j} + \sum_{i} \frac{\partial \vec{E}}{\partial X_{i}} u_{i}''$$
(1.2.15)

etc. as in eq. 1.2.10. The eqs. (1.2.13), as well as the calculation of the rigidity, eq. (1.2.5), involve derivatives $(B\rho)^{(n)} = \frac{d^n(B\rho)}{ds^n}$, which are obtained in the following way. Considering that

$$\frac{dp^2}{dt} = \frac{d\vec{p}^2}{dt} \quad i.e., \quad \frac{dp}{dt}p = \frac{d\vec{p}}{dt}\vec{p}$$
(1.2.16)

with $\frac{d\vec{p}}{dt} = q \left(\vec{e} + \vec{v} \times \vec{b} \right)$ (eq. 1.2.1), we obtain

$$\frac{dp}{dt}p = q\left(\vec{e} + v \times \vec{b}\right) \cdot \vec{p} = q\vec{e} \cdot \vec{p}$$
(1.2.17)

since $(\vec{v} \times \vec{b}) \cdot \vec{p} = 0$. Normalizing as previously with $\vec{p} = p\vec{u} = qB\rho\vec{u}$ and ds = vdt, and by successive differentiations, eq. (1.2.17) leads to the $(B\rho)^{(n)}$

$$(B\rho)' = \frac{1}{v} (\vec{e} \cdot \vec{u})
(B\rho)'' = \left(\frac{1}{v}\right)' (\vec{e} \cdot \vec{u}) + \frac{1}{v} (\vec{e} \cdot \vec{u})'
(B\rho)''' = \left(\frac{1}{v}\right)'' (\vec{e} \cdot \vec{u}) + 2\left(\frac{1}{v}\right)' (\vec{e} \cdot \vec{u})' + \frac{1}{v} (\vec{e} \cdot \vec{u})''
(B\rho)'''' = \left(\frac{1}{v}\right)''' (\vec{e} \cdot \vec{u}) + 3\left(\frac{1}{v}\right)'' (\vec{e} \cdot \vec{u})' + 3\left(\frac{1}{v}\right)' (\vec{e} \cdot \vec{u})'' + \frac{1}{v} (\vec{e} \cdot \vec{u})'''
(B\rho)''''' = etc.$$
(1.2.18)

The derivatives $(\vec{e} \cdot \vec{u})^{(n)} = \frac{d^n (\vec{e} \cdot \vec{u})}{ds^n}$ are obtained by recursive differentiation

$$(\vec{e} \cdot \vec{u})' = \vec{e}' \cdot \vec{u} + \vec{e} \cdot \vec{u}' (\vec{e} \cdot \vec{u})'' = \vec{e}'' \cdot \vec{u} + 2 \vec{e}' \cdot \vec{u}' + \vec{e} \cdot \vec{u}''$$
(1.2.19)
etc.

Note that they can be related to the derivatives of the kinetic energy W by $dW = \frac{d\vec{p}}{dt} \cdot \vec{v} \, dt = q\vec{e} \cdot \vec{v} \, dt$ which leads to

$$\frac{d^{n+1}W}{ds^{n+1}} = q \frac{d^n(\vec{e} \cdot \vec{u})}{ds^n}$$
(1.2.20)
Finally, the derivatives $\left(\frac{1}{v}\right)^{(n)} = \frac{d^n\left(\frac{1}{v}\right)}{ds^n}$ involved in eqs. (1.2.13,1.2.18) are obtained from

$$p = \frac{v}{c} \frac{W + m_0 c^2}{c}$$

 $(m_0 \text{ is the rest mass})$ by successive differentiations, that give the recursive relations

$$\begin{pmatrix} \frac{1}{v} \end{pmatrix} = \frac{1}{c^2} \frac{W + m_0 c^2}{qB\rho} \begin{pmatrix} \frac{1}{v} \end{pmatrix}' = \frac{1}{c^2} \frac{(\vec{e} \cdot \vec{u})}{B\rho} - \frac{1}{v} \frac{(B\rho)'}{B\rho} \begin{pmatrix} \frac{1}{v} \end{pmatrix}'' = \frac{1}{c^2} \frac{(\vec{e} \cdot \vec{u})'}{B\rho} - 2 \left(\frac{1}{v}\right)' \frac{(B\rho)'}{B\rho} - \frac{1}{v} \frac{(B\rho)''}{B\rho} \begin{pmatrix} \frac{1}{v} \end{pmatrix}''' = \frac{1}{c^2} \frac{(\vec{e} \cdot \vec{u})''}{B\rho} - 3 \left(\frac{1}{v}\right)'' \frac{(B\rho)'}{B\rho} - 3 \left(\frac{1}{v}\right)' \frac{(B\rho)''}{B\rho} - \frac{1}{v} \frac{(B\rho)'''}{B\rho} \begin{pmatrix} \frac{1}{v} \end{pmatrix}'''' = etc.$$
 (1.2.21)

1.2.3 Integration in Combined Electric and Magnetic Fields

When both \vec{e} and \vec{b} are non-zero, the complete eq. (1.2.3) must be considered. Recursive differentiations give the following relations

$$(B\rho)'\vec{u} + B\rho\vec{u}' = \frac{\vec{e}}{v} + \vec{u} \times \vec{b}$$

$$(B\rho)''\vec{u} + 2(B\rho)'\vec{u}' + B\rho\vec{u}'' = \left(\frac{1}{v}\right)'\vec{e} + \left(\frac{1}{v}\right)\vec{e}' + (\vec{u} \times \vec{b})'$$

$$(B\rho)'''\vec{u} + 3(B\rho)''\vec{u}' + 3(B\rho)'\vec{u}'' + B\rho\vec{u}''' = \left(\frac{1}{v}\right)''\vec{e} + 2\left(\frac{1}{v}\right)'\vec{e}' + \left(\frac{1}{v}\right)\vec{e}'' + (\vec{u} \times \vec{b})''$$

$$(B\rho)''''\vec{u} + 4(B\rho)'''\vec{u}' + 6(B\rho)''\vec{u}'' + 4(B\rho)'\vec{u}''' + B\rho\vec{u}'''' = \left(\frac{1}{v}\right)''\vec{e}' + 3\left(\frac{1}{v}\right)''\vec{e}' + 3\left(\frac{1}{v}\right)'\vec{e}'' + \frac{1}{v}\vec{e}''' + (\vec{u} \times \vec{b})'''$$

$$(1.2.22)$$

that provide the derivatives $\frac{d^n \vec{u}}{ds^n}$ needed in the Taylor expansions (1.2.4)

where $\vec{E} = \frac{\vec{e}}{B\rho}$, $\vec{B} = \frac{\vec{b}}{B\rho}$, and ${}^{(n)}|_{B\rho}$ denotes differentiation at constant $B\rho$

$$\vec{E}^{(n)}|_{B\rho} = \frac{1}{B\rho} \frac{d^n \vec{e}}{ds^n}$$
 and $(\vec{u} \times \vec{B})^{(n)}|_{B\rho} = \frac{1}{B\rho} (\vec{u} \times \vec{b})^{(n)}.$ (1.2.24)

These derivatives $\vec{E}^{(n)}$ and $\vec{B}^{(n)}$ of the electric and magnetic fields are calculated from the vector fields $\vec{E}(X,Y,Z)$, $\vec{B}(X,Y,Z)$ and their derivatives $\frac{\partial^{i+j+k}\vec{E}}{\partial X^i \partial Y^j \partial Z^k}$ and $\frac{\partial^{i+j+k}\vec{B}}{\partial X^i \partial Y^j \partial Z^k}$, following eqs. (1.2.14, 1.2.15) and eqs. (1.2.9, 1.2.10), respectively.

1.2.4 Calculation of the Time of Flight

The time of flight eq. (1.2.6) involves the derivatives dT/ds = 1/v, $d^2T/ds^2 = d(1/v)/ds$, etc. that are obtained from eq. (1.2.21). In the absence of electric field, however, eq. (1.2.6) reduces to the simple form

$$T(M_1) = T(M_0) + \Delta s/v \tag{1.2.25}$$

1.3 Calculation of \vec{E} and \vec{B} Fields and their Derivatives

In this section, unless otherwise stated, $\vec{B} = (B_X(X, Y, Z), B_Y(X, Y, Z), B_Z(X, Y, Z))$ stands indifferently for electric field \vec{E} or magnetic field \vec{B} .

B(X, Y, Z) and derivatives are calculated in various ways, depending whether field maps or analytic representations of optical elements are used. The basic means are the following.

1.3.1 1-D (Axial) Analytical Field Models and Extrapolation

This procedure assumes cylindrical symmetry with respect to the X-axis. The longitudinal field component B_X or $E_X(X, r = 0)$ $(r = (Y^2 + Z^2)^{1/2})$, along that axis is derived by differentiation of an appropriate model of the potential V(X) (e.g., magnetic in *SOLENOID*, electrostatic in *EL2TUB*, *UNIPOT*). The longitudinal and radial field components $B_X(X,r)$, $B_r(X,r)$ and their derivatives off-axis $\frac{\partial^{i+j}B_X}{\partial X^i\partial r^j}$ and $\frac{\partial^{i+j}B_r}{\partial X^i\partial r^j}$ are obtained by Taylor expansions to the second to fifth order in r (depending on the optical element) assuming cylindrical symmetry (eq. (1.3.1)), and then transformed to the (X,Y,Z) Cartesian frame of **zgoubi** in order to provide the derivatives $\frac{\partial^{i+j+k}\vec{B}}{\partial X^i\partial Y^j\partial Z^k}$ needed in eq. (1.2.15).

1.3.2 Extrapolation from 1-D axial field map [8]

A cylindrically symmetric field (*e.g.*, using *BREVOL*, *ELREVOL*) can be described by an axial 1-D field map of its longitudinal component $B_X(X, r = 0)$ $(r = (Y^2 + Z^2)^{1/2})$, while the radial component on axis $B_r(X, r = 0)$ is assumed to be zero. $B_X(X, r = 0)$ is obtained at any point along the X-axis by a polynomial interpolation from the map mesh (see section 1.4.1). Then the field components $B_X(X, r)$, $B_r(X, r)$ at the position of the particle, (X, r) are obtained from Taylor expansions truncated at the fifth order in r (hence, up to the fifth order derivative $\frac{\partial^5 B_X}{\partial X^5}(X, 0)$), assuming cylindrical symmetry

$$B_{X}(X,r) = B_{X}(X,0) - \frac{r^{2}}{4} \frac{\partial^{2} B_{X}}{\partial X^{2}} (X,0) + \frac{r^{4}}{64} \frac{\partial^{4} B_{X}}{\partial X^{4}} (X,0)$$

$$B_{r}(X,r) = -\frac{r}{2} \frac{\partial B_{X}}{\partial X} (X,0) + \frac{r^{3}}{16} \frac{\partial^{3} B_{X}}{\partial X^{3}} (X,0) - \frac{r^{5}}{384} \frac{\partial^{5} B_{X}}{\partial X^{5}} (X,0)$$
(1.3.1)

Then, by differentiation with respect to X and r, up to the second order, these expressions provide the derivatives of $\vec{B}(X,r)$. Finally a conversion from the (X,r) coordinates to the (X,Y,Z) Cartesian coordinates of **zgoubi** is performed, thus providing the expressions $\frac{\partial^{i+j+k}\vec{B}}{\partial X^i \partial Y^j \partial Z^k}$ needed in the eq. (1.2.10).

1.3.3 Extrapolation From Median Plane Field Models

In the median plane, $B_Z(X, Y, 0)$ and its derivatives with respect to X or Y may be derived from analytical models (*e.g.*, in Venus magnet - VENUS, and sharp edge multipoles SEXQUAD and QUADISEX) or numerically by polynomial interpolation from 2-D field maps (*e.g.*, CARTEMES, TOSCA).

Median plane antisymmetry is assumed, which results in

$$B_X(X, Y, 0) = 0$$

$$B_Y(X, Y, 0) = 0$$

$$B_X(X, Y, Z) = -B_X(X, Y, -Z)$$

$$B_Y(X, Y, Z) = -B_Y(X, Y, -Z)$$

$$B_Z(X, Y, Z) = B_Z(X, Y, -Z)$$

(1.3.2)

Accommodated with Maxwell's equations, this results in Taylor expansions below, for the three components of \vec{B} (here, B stands for $B_Z(X, Y, 0)$)

$$B_X(X,Y,Z) = Z \frac{\partial B}{\partial X} - \frac{Z^3}{6} \left(\frac{\partial^3 B}{\partial X^3} + \frac{\partial^3 B}{\partial X \partial Y^2} \right)$$

$$B_Y(X,Y,Z) = Z \frac{\partial B}{\partial Y} - \frac{Z^3}{6} \left(\frac{\partial^3 B}{\partial X^2 \partial Y} + \frac{\partial^3 B}{\partial Y^3} \right)$$

$$B_Z(X,Y,Z) = B - \frac{Z^2}{2} \left(\frac{\partial^2 B}{\partial X^2} + \frac{\partial^2 B}{\partial Y^2} \right) + \frac{Z^4}{24} \left(\frac{\partial^4 B}{\partial X^4} + 2 \frac{\partial^4 B}{\partial X^2 \partial Y^2} + \frac{\partial^4 B}{\partial Y^4} \right)$$

(1.3.3)

which are then differentiated one by one with respect to X, Y, or Z, up to second or fourth order (depending on optical element or *IORDRE* option, see section 1.4.2) so as to get the expressions involved in eq. (1.2.10).

1.3.4 Extrapolation from Arbitrary 2-D Field Maps

2-D field maps that give the three components $B_X(X, Y, Z_0)$, $B_Y(X, Y, Z_0)$ and $B_Z(X, Y, Z_0)$ at each node (X, Y) of a Z_0 Z-elevation map may be used. \vec{B} and its derivatives at any point (X, Y, Z) are calculated by polynomial interpolation followed by Taylor expansions in Z, without any hypothesis of symmetries (see section 1.4.3 and keywords *MAP2D*, *MAP2D-E*).

1.3.5 Interpolation in 3-D Field Maps [9]

In 3-D field maps \vec{B} and its derivatives up to the second order with respect to X, Y or Z are calculated by means of a second order polynomial interpolation, from 3-D $3 \times 3 \times 3$ -point grid (see section 1.4.4).

1.3.6 2-D Analytical Field Models and Extrapolation

Several optical elements such as *BEND*, *WIENFILT* (that uses the *BEND* procedures), *QUADISEX*, *VENUS*, etc., are defined from the expression of the field and derivatives in the median plane. 3-D extrapolation of these off the median plane is drawn from Taylor expansions and Maxwell's equations.

1.3.7 3-D Analytical Models of Fields

In many optical elements such as QUADRUPO, SEXTUPOL, MULTIPOL, EBMULT, etc., the three components of \vec{B} and their derivatives with respect to X, Y or Z are obtained at any step along trajectories from analytical expression drawn from the scalar potential V(X, Y, Z), namely

$$B_X = \frac{\partial V}{\partial X}, \quad B_Y = \frac{\partial V}{\partial Y}, \quad B_Z = \frac{\partial V}{\partial Z}, \quad \frac{\partial B_X}{\partial X} = \frac{\partial^2 V}{\partial X^2}, \quad \frac{\partial B_X}{\partial Y} = \frac{\partial^2 V}{\partial X \partial Y}, \quad \text{etc.}$$
(1.3.4)

and similarly for \vec{E} with opposite sign for the gradients.

Multipoles

The scalar potential used for the calculation of $\frac{\partial^{i+j+k}\vec{B}_n(X,Y,Z)}{\partial X^i \partial Y^i \partial Z^k}$ (i+j+k=0 to 4) in the case of magnetic and electro-magnetic multipoles with 2n poles (namely, QUADRUPO (n=2) to DODECAPO (n=6), MULTIPOL (n=1 to 10), EBMULT (n=1 to 10)) is [10]

$$V_n(X,Y,Z) = (n!)^2 \left(\sum_{q=0}^{\infty} (-1)^q \frac{G^{(2q)}(X)(Y^2 + Z^2)^q}{4^q q!(n+q)!} \right) \left(\sum_{m=0}^n \frac{\sin\left(m\frac{\pi}{2}\right) Y^{n-m} Z^m}{m!(n-m)!} \right)$$
(1.3.5)

where G(X) is a longitudinal form factor, defined at the entrance or exit of the optical element by

$$G(s) = \frac{G_0}{1 + \exp(P(s))}, \quad G_0 = \frac{B_0}{R_0^{n-1}}$$
(1.3.6)

wherein B_0 is the field at pole tip radius R_0 , and

$$P(s) = C_0 + C_1\left(\frac{s}{\lambda}\right) + C_2\left(\frac{s}{\lambda}\right)^2 + C_3\left(\frac{s}{\lambda}\right)^3 + C_4\left(\frac{s}{\lambda}\right)^4 + C_5\left(\frac{s}{\lambda}\right)^5$$

and s is the distance to the EFB.

Skew Multipoles

A multipole component with arbitrary order n can be tilted independently of the others by an arbitrary angle A_n around the X-axis. If so, the calculation of the field and derivatives in the rotated axis (X, Y_R, Z_R) is done in two steps. First, they are calculated at the rotated position (X, Y_R, Z_R) , in the (X, Y, Z) frame, using the expression (1.3.5) above. Second, \vec{B} and its derivatives at (X, Y_R, Z_R) in the (X, Y, Z) frame are transformed into the new, (X, Y_R, Z_R) frame, by a rotation with angle A_n .

In particular a skew 2*n*-pole component is created by taking $A_n = \pi/2n$.

A Note on Electrostatic Multipoles

A right electric multipole has the same field equations as the like-order skew magnetic multipole. Therefore, calculation of right or skew electric or electro-magnetic multipoles (*ELMULT*, *EBMULT*, *ELMULT*) uses the same eq. (1.3.5) together with the rotation process as described in section 1.3.7. The same method is used for arbitrary rotation of any multipole component around the X-axis.

1.4 Calculation of \vec{E} and \vec{B} from Field Maps

In this section, unless otherwise stated, $\vec{B} = (B_X(X, Y, Z), B_Y(X, Y, Z), B_Z(X, Y, Z))$ stands indifferently for electric field \vec{E} or magnetic field \vec{B} .

1.4.1 1-D Axial Map, with Cylindrical Symmetry

Let B_i be the value of the longitudinal component $B_X(X, r = 0)$ of the field \vec{B} , at node *i* of a uniform mesh that defines a 1-D field map along the symmetry X-axis, while $B_r(X, r = 0)$ is assumed to be zero $(r = (Y^2 + Z^2)^{1/2})$. The field component $B_X(X, r = 0)$ is calculated by a polynomial interpolation of the fifth degree in X, using a 5 points grid centered at the node of the 1-D map which is closest to the actual coordinate X of the particle.

The interpolation polynomial is

$$B(X,0) = A_0 + A_1 X + A_2 X^2 + A_3 X^3 + A_4 X^4 + A_5 X^5$$
(1.4.1)

and the coefficients A_i are calculated by expressions that minimize the quadratic sum

$$S = \sum_{i} (B(X,0) - B_i)^2$$
(1.4.2)

Namely, the source code contains the explicit analytical expressions of the coefficients A_i solutions of the normal equations $\partial S/\partial A_i = 0$.

The derivatives $\frac{\partial^n B}{\partial X^n}(X,0)$ at the actual position X, as involved in eqs. (1.3.1), are then obtained by differentiation of the polynomial (1.4.1), giving

$$\frac{\partial B}{\partial X}(X,0) = A_1 + 2A_2X + 3A_3X^2 + 4A_4X^3 + 5A_5X^4$$

$$\frac{\partial^2 B}{\partial X^2}(X,0) = 2A_2 + 6A_3X + 12A_4X^2 + 20A_5X^3$$
...
$$\frac{\partial^5 B}{\partial X^5}(X,0) = 120A_5$$
(1.4.3)

1.4.2 2-D Median Plane Map, with Median Plane Antisymmetry

Let B_{ij} be the value of $B_Z(X, Y, 0)$ at the nodes of a mesh which defines a 2-D field map in the (X, Y) plane while $B_X(X, Y, 0)$ and $B_Y(X, Y, 0)$ are assumed to be zero. Such a map may have been built or measured in either Cartesian or polar coordinates. Whenever polar coordinates are used, a change to Cartesian coordinates (described below) provides the expression of \vec{B} and its derivatives as involved in eq. (1.2.10). **zgoubi** provides three types of polynomial interpolation from the mesh (option *IORDRE*); namely, a second order interpolation, with either a 9- or a 25-point grid, or a fourth order interpolation with a 25-point grid (Fig. 3).

If the 2-D field map is built up from computer simulation, the grid in principle simply aims at interpolating the field and derivatives at a given point from its 9 or 25 neighbors. On the other hand if the map results from field measurements, the grid also has the virtue of smoothing field fluctuations.

The mesh may be defined in Cartesian coordinates, (Figs. 3A and 3B) or in polar coordinates (Fig. 3C).

The interpolation grid is centered on the node which is closest to the projection in the (X, Y) plane of the actual point of the trajectory.

The interpolation polynomial is

$$B(X,Y,0) = A_{00} + A_{10}X + A_{01}Y + A_{20}X^2 + A_{11}XY + A_{02}Y^2$$
(1.4.4)

to the second order, or

$$B(X, Y, 0) = A_{00} + A_{10}X + A_{01}Y + A_{20}X^{2} + A_{11}XY + A_{02}Y^{2} + A_{30}X^{3} + A_{21}X^{2}Y + A_{12}XY^{2} + A_{03}Y^{3} + A_{40}X^{4} + A_{31}X^{3}Y + A_{22}X^{2}Y^{2} + A_{13}XY^{3} + A_{04}Y^{4}$$
(1.4.5)

to the fourth order. The coefficients A_{ij} are calculated by expressions that minimize, with respect to A_{ij} , the quadratic sum

$$S = \sum_{ij} (B(X, Y, 0) - B_{ij})^2$$
(1.4.6)

The source code contains the explicit analytical expressions of the coefficients A_{ij} solutions of the normal equations $\partial S/\partial A_{ij} = 0$.



- Figure 3: Mesh in the (X, Y) plane. The grid is centered on the node closest to the actual position of the particle.
 - A : Cartesian mesh, 9-point interpolation grid.
 - B : Cartesian mesh, 25-point interpolation grid.
 - C : Polar mesh and moving Cartesian frame.

The A_{ij} may then be identified with the derivatives of B(X, Y, 0) at the central node of the grid

$$A_{ij} = \frac{1}{i!j!} \frac{\partial^{i+j}B}{\partial X^i \partial Y^j} (0,0,0)$$
(1.4.7)

The derivatives of B(X, Y, 0) with respect to X and Y, at the actual point (X, Y, 0) are obtained by differentiation of the interpolation polynomial, which gives (*e.g.*, from (1.4.4) in the case of second order interpolation)

$$\frac{\partial B}{\partial X}(X, Y, 0) = A_{10} + 2A_{20}X + A_{11}Y
\frac{\partial B}{\partial Y}(X, Y, 0) = A_{01} + A_{11}X + 2A_{02}Y
etc.$$
(1.4.8)

This allows stepping to the calculation of $\vec{B}(X, Y, Z)$ and its derivatives as described in subsection 1.3.3 (eq. 1.3.3).

The Case of Polar Maps

In some optical elements (*e.g.*, *POLARMES*, *DIPOLE*[S]) the field is given in polar coordinates. It is thus necessary to transform the field and derivatives from the polar frame of the map, (R, α, Z) to the Cartesian moving frame (X, Y, Z), Fig. 3C. This is done as follows.

In second order calculations the correspondence is (we note $B \equiv B_Z(Z=0)$)

$$\frac{\partial B}{\partial X} = \frac{1}{R} \frac{\partial B}{\partial \alpha}$$

$$\frac{\partial B}{\partial Y} = \frac{\partial B}{\partial R}$$

$$\frac{\partial^2 B}{\partial X^2} = \frac{1}{R^2} \frac{\partial^2 B}{\partial \alpha^2} + \frac{1}{R} \frac{\partial B}{\partial R}$$

$$\frac{\partial^2 B}{\partial X^2} = \frac{1}{R^2} \frac{\partial^2 B}{\partial \alpha \partial R} - \frac{1}{R^2} \frac{\partial B}{\partial \alpha}$$

$$\frac{\partial^2 B}{\partial Y^2} = \frac{\partial^2 B}{\partial R^2}$$
(1.4.9)
$$\frac{\partial^3 B}{\partial X^3} = \frac{3}{R^2} \frac{\partial^2 B}{\partial \alpha \partial R} - \frac{2}{R^3} \frac{\partial B}{\partial \alpha}$$

$$\frac{\partial^3 B}{\partial X^2 \partial Y} = \frac{2}{R^3} \frac{\partial B}{\partial \alpha} - \frac{2}{R^2} \frac{\partial^2 B}{\partial \alpha \partial R}$$

$$\frac{\partial^3 B}{\partial X^3} = 0$$

In fourth order calculations the relations above are pushed to fourth order in X, Y whereas

$$\frac{\partial^{3}B}{\partial X^{3}} = \frac{1}{R^{3}} \frac{\partial^{3}B}{\partial \alpha^{3}} + \frac{3}{R^{2}} \frac{\partial^{2}B}{\partial \alpha \partial R} - \frac{2}{R^{3}} \frac{\partial B}{\partial \alpha}$$

$$\frac{\partial^{3}B}{\partial X^{2} \partial Y} = \frac{1}{R^{2}} \frac{\partial^{3}B}{\partial \alpha^{2} \partial R} - \frac{2}{R^{3}} \frac{\partial^{2}B}{\partial \alpha^{2}} - \frac{1}{R^{2}} \frac{\partial B}{\partial R} + \frac{1}{R} \frac{\partial^{2}B}{\partial R^{2}}$$

$$\frac{\partial^{3}B}{\partial X^{2} \partial Y^{2}} = \frac{1}{R} \frac{\partial^{3}B}{\partial \alpha \partial R^{2}} + \frac{2}{R^{3}} \frac{\partial B}{\partial \alpha} - \frac{2}{R^{2}} \frac{\partial^{2}B}{\partial \alpha \partial R}$$

$$\frac{\partial^{3}B}{\partial X^{3}} = \frac{\partial^{3}B}{\partial R^{3}}$$

$$\frac{\partial^{4}B}{\partial X^{4}} = \frac{1}{R^{4}} \frac{\partial^{4}B}{\partial \alpha^{4}} - \frac{8}{R^{4}} \frac{\partial^{2}B}{\partial \alpha^{2}} + \frac{6}{R^{3}} \frac{\partial^{3}B}{\partial \alpha^{2} \partial R} + \frac{3}{R^{2}} \frac{\partial^{2}B}{\partial R^{2}} - \frac{3}{R^{3}} \frac{\partial B}{\partial R}$$

$$\frac{\partial^{4}B}{\partial X^{3} \partial Y} = \frac{1}{R^{3}} \frac{\partial^{4}B}{\partial \alpha^{3} \partial R} - \frac{3}{R^{4}} \frac{\partial^{3}B}{\partial \alpha^{3}} + \frac{3}{R^{2}} \frac{\partial^{3}B}{\partial \alpha \partial R^{2}} - \frac{8}{R^{3}} \frac{\partial^{2}B}{\partial \alpha \partial R} + \frac{6}{R^{4}} \frac{\partial B}{\partial \alpha}$$

$$\frac{\partial^{4}B}}{\partial X^{2} 2Y^{2}} = \frac{1}{R^{4}} \frac{\partial^{2}B}{\partial \alpha^{2}} - \frac{4}{R^{3}} \frac{\partial^{3}B}{\partial \alpha^{2} \partial R} - \frac{2}{R^{2}} \frac{\partial^{2}B}{\partial R^{2}} + \frac{2}{R^{3}} \frac{\partial B}{\partial R} + \frac{1}{R^{2}} \frac{\partial^{4}B}{\partial \alpha \partial R} + \frac{1}{R} \frac{\partial^{3}B}{\partial \alpha^{2}}$$

$$\frac{\partial^{4}B}}{\partial X^{2} Y^{3}} = \frac{1}{R} \frac{\partial^{4}B}{\partial \alpha \partial R^{3}} - \frac{3}{R^{2}} \frac{\partial^{3}B}{\partial \alpha \partial R^{2}} + \frac{6}{R^{3}} \frac{\partial^{2}B}{\partial \alpha \partial R} - \frac{6}{R^{4}} \frac{\partial^{4}B}{\partial \alpha^{4}}$$

$$(1.4.10)$$

NOTE : In case a particle goes beyond the limits of the field map, the field and its derivatives are extrapolated using a grid at the border of the map, which is the closest to the actual position of the particle. The flag *IEX* attached to the particle (section 7.12, p. 211) is then given the value -1.

1.4.3 Arbitrary 2-D Map, no Symmetry

The map is assumed to describe the field $\vec{B}(B_X, B_Y, B_Z)$ in the (X, Y) plane at elevation Z_0 . It provides the components $B_{X,ij}$, $B_{Y,ij}$, $B_{Z,ij}$ at each node (i, j) of a 2-D mesh.



Figure 4: A 3-D, 27-point grid is used for interpolation of magnetic or electric fields and derivatives up to second order. The central node of the grid (i = j = k = 0) is the closest to the actual position of the particle.

The value of \vec{B} and its derivatives at the projection (X, Y, Z_0) of the actual position (X, Y, Z) of a particle is obtained by means of (parameter *IORDRE* in the keyword argument list - see for instance *MAP2D*, *MAP2D*-E) either a second degree polynomial interpolation from a 3×3 points grid (*IORDRE*=2), or a fourth degree polynomial interpolation from a 5×5 points grid (*IORDRE*=4), centered at the node (i, j) closest to the position (X, Y).

To second order for instance

$$B_{\ell}(X,Y,Z_0) = A_{00} + A_{10}X + A_{01}Y + A_{20}X^2 + A_{11}XY + A_{02}Y^2$$
(1.4.11)

where B_{ℓ} stands for any of the three components B_X , B_Y or B_Z . Differentiating then gives the derivatives

$$\frac{\partial B_{\ell}}{\partial X}(X, Y, Z_0) = A_{10} + 2A_{20}X + A_{11}Y$$

$$\frac{\partial^2 B_{\ell}}{\partial X \partial Y}(X, Y, Z_0) = A_{11}$$
etc.
(1.4.12)

Then follows a procedure of extrapolation from (X, Y, Z_0) to the actual position (X, Y, Z), based on Taylor series development.

No special symmetry is assumed, which allows the treatment of arbitrary field distribution (*e.g.*, solenoid, helical snake).

1.4.4 3-D Field Map

When using a 3-D field map, the vector field $\vec{B}(X, Y, Z)$ and its derivatives necessary for the calculation of position and velocity of the particle are obtained via second degree polynomial interpolation,

$$B_{\ell}(X,Y,Z) = A_{000} + A_{100}X + A_{010}Y + A_{001}Z + A_{200}X^2 + A_{020}Y^2 + A_{002}Z^2 + A_{110}XY + A_{101}XZ + A_{011}YZ$$
(1.4.13)

 B_{ℓ} stands for any of the three components, B_X , B_Y or B_Z . By differentiation of B_{ℓ} one gets

$$\frac{\partial B_{\ell}}{\partial X} = A_{100} + 2A_{200}X + A_{110}Y + A_{101}Z$$

$$\frac{\partial^2 B_{\ell}}{\partial X^2} = 2A_{200}$$
(1.4.14)

and so on up to second order derivatives with respect to X, Y or Z.

The interpolation involves a $3 \times 3 \times 3$ -point parallelepipedic grid (Fig. 4), the origin of which is positioned at the node of the 3-D field map which is closest to the actual position of the particle.

Let B_{ijk}^{ℓ} be the value of the — measured or computed — magnetic field at each one of the 27 nodes of the 3-D grid (B^{ℓ} stands for B_X , B_Y or B_Z), and $B_{\ell}(X, Y, Z)$ be the value at a position (X, Y, Z) with respect to the central node of the 3-D grid. Thus, any coefficient A_i of the polynomial expansion of B_{ℓ} is obtained by means of expressions that minimize, with respect to A_i , the sum

$$S = \sum_{ijk} \left(B_{\ell}(X, Y, Z) - B_{ijk}^{\ell} \right)^2$$
(1.4.15)

where the indices *i*, *j* and *k* take the values -1, 0 or +1 so as to sweep the 3-D grid. The source code contains the explicit analytical expressions of the coefficients A_{ijk} solutions of the normal equations $\partial S/\partial A_{ijk} = 0$.
2 SPIN TRACKING

Spin motion computation was implemented in **zgoubi** in the SATURNE years [11], it has since been used in a number of studies, including the transport of polarized muons in the Neutrino Factory [12]; polarization survival in the superB project [13]; studies on proton polarization with helical snakes at AGS [14] and RHIC [15]; in the magic-energy electrostatic ring of the proton-EDM project [16]; in the Booster [17], AGS, RHIC hadron rings of the Electron Ion Collider (EIC) (Fig. 5); for polarization transmission in rapid cycling injector synchrotrons [18, 19]; at the EIC electron injector [20]: for an ergodic approach of spin diffusioon and polarization lifetime in the EIC electron storage ring [21].

The Electron Ion Collider at BNL



Figure 5: Zgoubi has tacked polarization in all the rings of the future EIC at BNL: polarized electron bunches in the RCS injector and the downstream ESR storage ring; polarized proton and ³He bunches in the AGS Booster, the AGS, and the HSR storage ring.

2.1 Introduction

The precession of the spin \vec{S} of a charged particle in electric and magnetic fields is governed by the Thomas-BMT first order differential equation [22]

$$\frac{d\vec{S}}{dt} = \frac{q}{m}\vec{S}\times\vec{\omega}$$
(2.1.1)

with, in the laboratory frame,

$$\vec{\omega} = (1+\gamma G)\vec{b} + G(1-\gamma)\vec{b}_{\parallel} + \gamma \left(G + \frac{1}{1+\gamma}\right)\frac{\vec{e}\times\vec{v}}{c^2}$$

$$= (1+G)\vec{b}_{\parallel} + (1+\gamma G)\vec{b}_{\perp} + \gamma \left(G + \frac{1}{1+\gamma}\right)\frac{\vec{e}\times\vec{v}}{c^2}$$

$$(2.1.2)$$

t, q, m, c, γ and G are respectively the time, charge, relativistic mass, speed of light, Lorentz relativistic factor and anomalous magnetic moment of the particle, \vec{b} and \vec{e} are the fields in the laboratory, \vec{b}_{\parallel} is the component of \vec{b} parallel to the velocity \vec{v} of the particle, $\vec{b} = \vec{b}_{\parallel} + \vec{b}_{\perp}$.

Equation (2.1.1) is normalized by introducing the same notation as for the Lorentz equation, page 21, namely $b = ||\vec{b}||, v = ||\vec{v}||, \vec{v} = v\vec{u}, ds = vdt$ the differential path, $\frac{\gamma mv}{q} = B\rho$ the rigidity of the particle, $\vec{dS} = 1 d\vec{S}$

whereas $\vec{S}' = \frac{d\vec{S}}{ds} = \frac{1}{v} \frac{d\vec{S}}{dt}$ is the derivative of the spin with respect to the path. This yields

$$(B\rho)\vec{S}' = \vec{S} \times \vec{\omega} \quad \text{or} \quad \vec{S}' = \vec{S} \times \vec{\Omega}$$
 (2.1.3)

where, noting $\vec{B} = \vec{b}/B\rho, \vec{E} = \vec{e}/B\rho$,

$$\vec{\Omega} = \frac{\vec{\omega}}{B\rho} = (1+\gamma G)\vec{B} + G(1-\gamma)\vec{B}_{/\!\!/} + \frac{\beta\gamma}{c}\left(G + \frac{1}{1+\gamma}\right)\vec{E} \times \vec{u}$$
(2.1.4)

This equation is solved in the same way as the reduced Lorentz equation (1.2.3). From the values of the precession factor $\vec{\omega}(M_0)$ and spin $\vec{S}(M_0)$ of the particle at position M_0 , the spin $\vec{S}(M_1)$ at position M_1 , following a displacement Δs (fig. 2), is obtained from truncated Taylor expansion

$$\vec{S}(M_1) \approx \vec{S}(M_0) + \frac{d\vec{S}}{ds}(M_0)\,\Delta s + \frac{d^2\vec{S}}{ds^2}\,(M_0)\frac{\Delta s^2}{2} + \frac{d^3\vec{S}}{ds^3}\,(M_0)\frac{\Delta s^3}{3!} + \frac{d^4\vec{S}}{ds^4}\,(M_0)\frac{\Delta s^4}{4!} + \frac{d^5\vec{S}}{ds^5}\,(M_0)\frac{\Delta s^5}{5!}$$
(2.1.5)

2.2 Integration in Magnetic Fields

In purely magnetic fields $\vec{e} = 0$ thus eq. (2.1.4) reduces to

$$\vec{\Omega}_{b} = (1 + \gamma G)\vec{B} + G(1 - \gamma)\vec{B}_{\#}$$
(2.2.1)

 \vec{S} and its derivatives $\vec{S}^{(n)} = d^n \vec{S}/ds^n$ satisfy the recursive differentiation relations

$$\vec{S}' = \vec{S} \times \vec{\Omega}_{b}$$

$$\vec{S}'' = \vec{S}' \times \vec{\Omega}_{b} + \vec{S} \times \vec{\Omega}_{b}'$$

$$\vec{S}''' = \vec{S}'' \times \vec{\Omega}_{b} + 2\vec{S}' \times \vec{\Omega}_{b}' + \vec{S} \times \vec{\Omega}_{b}''$$

etc.
(2.2.2)

with the derivatives $d^n \vec{\Omega}_b/ds^n$ obtained by differentiation of eq. (2.2.1). This requires \vec{B}_{\parallel} and derivatives, obtained in the following way,

$$\vec{B}_{\parallel} = (\vec{B} \cdot \vec{u}) \vec{u}
\vec{B}_{\parallel}' = (\vec{B}' \cdot \vec{u} + \vec{B} \cdot \vec{u}') \vec{u} + (\vec{B} \cdot \vec{u}) \vec{u}'
\vec{B}_{\parallel}'' = (\vec{B}'' \cdot \vec{u} + 2\vec{B}' \cdot \vec{u}' + \vec{B} \cdot \vec{u}'') \vec{u} + 2(\vec{B}' \cdot \vec{u} + \vec{B} \cdot \vec{u}') \vec{u}' + (\vec{B} \cdot \vec{u}) \vec{u}''
etc.$$
(2.2.3)

The quantities \vec{u} , \vec{B} and their derivatives as involved in these equations are known, being sub-products of the integration of the motion of the particle, eqs. (1.2.8, 1.2.10) p. 23.

2.3 Integration in Electric Fields

In purely electric fields $\vec{b} = 0$, thus eq. (2.1) reduces to

$$\omega_e = \frac{\beta\gamma}{c} (G + \frac{1}{1+\gamma}) \vec{e} \times \vec{u}$$
(2.3.1)

 \vec{S} and its derivatives $\vec{S}^{(n)} = d^n \vec{S}/ds^n$ satisfy the recursive differentiation relations

$$B\rho \vec{S'} = \vec{S} \times \vec{\omega}_e$$

$$(B\rho)'\vec{S'} + B\rho \vec{S''} = \vec{S'} \times \vec{\omega}_e + \vec{S} \times \vec{\omega}'_e$$

$$(B\rho)''\vec{S'} + 2(B\rho)'\vec{S''} + B\rho \vec{S'''} = \vec{S''} \times \vec{\omega}_e + 2\vec{S'} \times \vec{\omega}'_e + \vec{S'} \times \vec{\omega}''_e$$
etc.
$$(2.3.2)$$

that provide the derivatives $d^n \vec{S}/ds^n$ needed in the Taylor expansion (eq. 2.1.5). The derivatives $(B\rho)^{(n)} = d^n (B\rho)/ds^n$ above are a sub-product of the integration of the force law (eq. 1.2.18). The derivatives of ω_e (eq. 2.3.1) are obtained by recursive differentiation,

$$\vec{\omega}_{e}^{\prime} = \left(\frac{\beta\gamma}{c}(G+\frac{1}{1+\gamma})\right)^{\prime} \vec{e} \times \vec{u} + \frac{\beta\gamma}{c}(G+\frac{1}{1+\gamma})(\vec{e} \times \vec{u})^{\prime}$$
$$\vec{\omega}_{e}^{\prime\prime} = \left(\frac{\beta\gamma}{c}(G+\frac{1}{1+\gamma})\right)^{\prime\prime} \vec{e} \times \vec{u} + 2\left(\frac{\beta\gamma}{c}(G+\frac{1}{1+\gamma})\right)^{\prime}(\vec{e} \times \vec{u})^{\prime} + \frac{\beta\gamma}{c}(G+\frac{1}{1+\gamma})(\vec{e} \times \vec{u})^{\prime\prime} \quad (2.3.3)$$
etc.

The quantities $\left(\frac{1}{1+\gamma}\right)^{(n)}$ in the $(\omega_e)^{(n)}$ above are obtained as follows.

From
$$\gamma^2 = 1/(1-\beta^2)$$
 it comes $(\gamma+1)(\gamma-1)\beta^2/(1-\beta^2)$ and then

$$\frac{1}{1+\gamma} = \left(\frac{1}{\beta}-1\right)\left(\frac{1}{\beta}+1\right)(\gamma-1)$$

which is differentiated, recursively,

$$\begin{pmatrix} \frac{1}{1+\gamma} \end{pmatrix}' = \begin{pmatrix} \frac{1}{\beta} \end{pmatrix}' \begin{pmatrix} \frac{1}{\beta}+1 \end{pmatrix} (\gamma-1) + \begin{pmatrix} \frac{1}{\beta}-1 \end{pmatrix} \begin{pmatrix} \frac{1}{\beta} \end{pmatrix}' (\gamma-1) + \begin{pmatrix} \frac{1}{\beta}-1 \end{pmatrix} \begin{pmatrix} \frac{1}{\beta}+1 \end{pmatrix} \gamma' \begin{pmatrix} \frac{1}{1+\gamma} \end{pmatrix}'' = \begin{pmatrix} \frac{1}{\beta} \end{pmatrix}'' \begin{pmatrix} \frac{1}{\beta}+1 \end{pmatrix} (\gamma-1) + \begin{pmatrix} \frac{1}{\beta}-1 \end{pmatrix} \begin{pmatrix} \frac{1}{\beta}-1 \end{pmatrix} \begin{pmatrix} \frac{1}{\beta}-1 \end{pmatrix} \begin{pmatrix} \frac{1}{\beta}+1 \end{pmatrix} \gamma'' + 2 \begin{pmatrix} \frac{1}{\beta} \end{pmatrix}' \begin{pmatrix} \frac{1}{\beta} \end{pmatrix} (\gamma-1) + 2 \begin{pmatrix} \frac{1}{\beta} \end{pmatrix}' \begin{pmatrix} \frac{1}{\beta} \end{pmatrix}' (\gamma-1) + 2 \begin{pmatrix} \frac{1}{\beta}-1 \end{pmatrix} \begin{pmatrix} \frac{1}{\beta} \end{pmatrix}' \gamma'$$

etc. (2.3.4)

The interest of that formulation is that the $\left(\frac{1}{\beta}\right)^{(n)}$ are already known from the particle dynamics, eq. (1.2.21), as well as the derivatives $d^{n+1}\alpha = \alpha d^n(\vec{z} \cdot \vec{x})$

following eq. (1.2.20), whereas the $d^n(\vec{e} \cdot \vec{u})/ds^n$ are given by eq. (1.2.19).

2.4 Integration in Combined Electric and Magnetic Fields

When both \vec{e} and \vec{b} are non-zero, the complete eqs. (2.1.3, 2.1.4) must be considered. The precession vector (eq. 2.1.4) and its derivatives can be split into independent, magnetic and electric components, namely

$$\vec{\omega} = \vec{\omega}_b + \vec{\omega}_e, \ \vec{\omega}' = \vec{\omega}_b' + \vec{\omega}_e', \quad \text{etc.}$$

As a consequence, the spin vector $\vec{S}(s)$ and its derivatives at location M_0 prior to a Δs push to location M_1 (fig. 2) can be obtained by linear superposition of the separate solutions for the magnetic case (eq. 2.2.2) and for the electric case (eq. 2.3.2), namely

$$B\rho \vec{S}' = \vec{S} \times \vec{\omega}_{b} + \vec{S} \times \vec{\omega}_{b} + \vec{S} \times \vec{\omega}_{b}' + \vec{S} \times \vec{\omega}_{b}' + \vec{S} \times \vec{\omega}_{b}' + \vec{S} \times \vec{\omega}_{b}' + \vec{S} \times \vec{\omega}_{e} + \vec{S} \times \vec{\omega}_{e}' - (B\rho)'\vec{S}' + \vec{S}' \times \vec{\omega}_{e} + \vec{S}' \times \vec{\omega}_{e} + \vec{S} \times \vec{\omega}_{e}' - ((B\rho)'\vec{S}' + 2(B\rho)'\vec{S}')) + \vec{S}'' \times \vec{\omega}_{e} + 2\vec{S}' \times \vec{\omega}_{e}' + \vec{S} \times \vec{\omega}_{e}'' - ((B\rho)''\vec{S}' + 2(B\rho)'\vec{S}')) + \vec{S}'' \times \vec{\omega}_{e} + 2\vec{S}' \times \vec{\omega}_{e}' + \vec{S} \times \vec{\omega}_{e}'' - ((B\rho)''\vec{S}' + 2(B\rho)'\vec{S}')) + \vec{S}'' \times \vec{\omega}_{e} + \vec{S} \times \vec{\omega}_{e}' + \vec{S} \times \vec{\omega}_{e}'' + \vec$$

etc.

The process is then completed by applying the Δs push, eq. (2.1.5).

2.5 Radiative polarization

Radiative spin transition is accounted for in a classical manner with an additional term in the Thomas-BMT differential equation for the motion of the polarization vector [23], namely, see Eqs. 2.1.1, 2.1 (in the absence of electric fields),

$$\frac{d\vec{S}}{dt} = \frac{q}{m}\vec{S} \times \left((1+a\gamma)\vec{b} + a(1-\gamma)\vec{b}_{\parallel}\right) - \frac{1}{\tau_{ST}}\left(\vec{S} - \frac{2}{9}(\vec{S}\cdot\vec{u})\vec{u} + \frac{8}{5\sqrt{3}}\frac{\vec{u}\times\dot{\vec{u}}}{|\dot{\vec{u}}|}\right)$$
(2.5.1)

where the electron notation for the magnetic anomaly, a, replaces hadron's G (and q = -e with e the elementary charge, for electrons), \vec{u} is the unit velocity vector of the particle and $\dot{\vec{u}} = d\vec{u}/dt = v\vec{u}'$ (eq. 1.2.2). The Sokolov-Ternov polarization equilibrium time constant has been introduced,

$$\tau_{ST} = \frac{4}{5\sqrt{3}} \frac{E}{\hbar\omega_c} \tau_0 \tag{2.5.2}$$

with $E = \gamma m_0$ the particle energy and $\hbar \omega_c = h \times 3\gamma^3 c / 2\rho$ the critical photon energy.

This radiative term is only added if the particle does radiate [24], that event being determined by the Monte Carlo photon emission simulation process described in Sec. 3.1, switched on using the keyword *SRLOSS*. It has the effect of slightly changing the electron polarization, under the effect of radiation induced spin transition.

This radiative correction process is under installation in **zgoubi**. Its benchmarking includes comparison with statistical averages of quantum spin physics.

As to the numerical integration of spin motion with diffusion (*i.e.*, solving the differential eq. 2.5.1), the technique follows the **zgoubi** Taylor expansion method, as detailed in Sec. 2.1, using insead the successive derivatives of \vec{S} with respect to the path variable *s* drawn from Eq. 2.5.1.

2.6 Spin Diffusion

Spin diffusion is a sub-product of the Monte Carlo synchrotron radiation technique. The spin vector of a particle will diffuse under the effect of stochastic photon emission.

TO BE DOCUMENTED FURTHER.

Spin Diffusion Integrals

They write

DK spin integrals (2.6.1)

These intergals are evaluated by stepwise integration¹ along a reference orbit (using a mid-point method), therefore requiring prior knowledge - or computation - of the latter and of the spin precession direction along. If the latter two quantities are known, they may just be specified as the initial coordinates in *OBJET* and in *SPNTRK*. If not, then (see Sec. 7.3) a *FIT*[2] of both initial orbit and initial spin conditions will update both *OBJET* and *SPNTRK* data to the required values. Note that, in the case of a ring sequence, these initial conditions are expected to be the periodic orbit coordinates and periodic (*aka* "closed") spin precession axis coordinates, which *FIT*[2] can find.

TWISS keyword manages the all process (possibly preceded by a prior *FIT[2]* following the periodicity considerations above). Namely, *TWISS* will trigger DK spin integral computation if both *SRLOSS* and *SP*-*NTRK* are present. Note that the presence of *SRLOSS* also results in the numerical, stepwise, computation of the synchrtron radiation integrals (Sec 3.1).

UNDER INSTALLATION/BENCHMARKING. TO BE DOCUMENTED FURTHER.

3 SYNCHROTRON RADIATION

zgoubi provides the simulation of two distinct types of synchrotron radiation (SR) manifestations namely, on the one hand energy loss by stochastic emission of photons and the ensuing perturbation on particle dynamics and, on the other hand the time-dependent radiated electro-magnetic field impulse, and its spectral-angular energy density as observed in the laboratory.

SR loss simulation was first installed in **zgoubi** in view of beam dynamics studies in the beam delivery system of the Next Linear Collider [25], based on a method developed in the frame of the ELFE project ("EU Lab. For Electrons") [26, 27, 28]. It was later used, and benchmarked including coupling, to account for damping effects in beam studies for various electron-ring and recirculator projects [13, 29, 30], and to account for spin diffusion studies in eRHIC collider lattice - which includes spin rotators [21].

SR electromagnetic impulse and spectrum computation was first installed in **zgoubi** for the study of interference effects at the LEP beam diagnostics miniwiggler [32]. These simulation tools were next used to design the LHC SR beam diagnostics systems, located in the IR4 RF section [33].

3.1 Energy Loss and Dynamical Effects

Most of the contents of the present section are drawn from Ref. [25].

Given a particle wandering in the magnetic field of an arbitrary optical element or field map, **zgoubi** computes the energy loss undergone, and its effect on the particle motion. The energy loss is calculated in a classical manner, by invoking two random processes that accompany the emission of a photon namely,

- the probability of emission,
- the energy of the photon.

The effects on the dynamics of the emitting particle either account for the sole alteration of its energy, or, if requested, include the angle kick. Particle position is supposed not to change upon emission of a photon. These calculations and ensuing dynamics corrections are performed at each integration step. In a practical manner, this requires centimeters to tens of centimeters steps in smoothly varying magnetic fields (a quantity to be determined before any simulation, from convergence trials).

Main aspects of the method are developed in the following.

Probability of Emission of a Photon

Given that the number of photons emitted within a step Δs can be very small (units or fractions of a unit)² a Poisson probability law

$$p(k) = \frac{\lambda^k}{k!} \exp(-\lambda) \tag{3.1.1}$$

is considered. k is the number of photons emitted over a $\Delta \theta$ (circular) arc of trajectory such that, the average number of photons per radian expresses as³

$$\lambda = \frac{20er_0}{8\hbar\sqrt{3}}\beta^2 B\rho \frac{\Delta s}{\rho}$$
(3.1.2)

where $r_0 = e^2/4\pi\epsilon_0 m_0 c^2$ is the classical radius of the particle of rest-mass m_0 , e is the elementary charge, $\hbar = h/2\pi$, h is the Planck constant, $\beta = v/c$, $B\rho$ is the particle stiffness. λ is evaluated at each integration step from the current values β , $B\rho$ and Δs , then a value of k is drawn by a rejection method.

²For instance, a 1 GeV electron will emit about 20.6 photons per radian ; an integration step size $\Delta s = 0.1$ m upon $\rho = 10$ m bending radius results in 0.2 photon per step.

³This leads for instance, in the case of electrons, to the classical formula $\lambda/\Delta\theta \approx 129.5 \text{E}(\text{GeV})/2\pi \approx \gamma/94.9$.

Energy of the Photons

These k photons are assigned energies $\epsilon = h\nu$ at random, in the following way. The cumulative distribution of the energy probability law $p(\epsilon/\epsilon_c) d\epsilon/\epsilon_c$ (*i.e.*, the probability of emission of a photon with energy in $[0, \epsilon]$) writes ⁴

$$\mathcal{P}(\epsilon/\epsilon_c) = \frac{3}{5\pi} \int_0^{\epsilon/\epsilon_c} \frac{d\epsilon}{\epsilon_c} \int_{\epsilon/\epsilon_c}^{\infty} K_{5/3}(x) dx$$
(3.1.3)

where $K_5/3$ is a modified Bessel function and, $\epsilon_c =$ $\hbar\omega_c, \omega_c = 2\pi \times 3\gamma^3 c/2\rho$ being the critical frequency in the presence of bending radius ρ ; ω_c is evaluated at each integration step from the current values γ and ρ , in other words, this energy loss calculation assumes constant magnetic field over the trajectory arc Δs . In the low frequency region ($\epsilon/\epsilon_c \ll 1$) it can be approximated by

$$\mathcal{P}(\epsilon/\epsilon_c) = \frac{12\sqrt{3}}{2^{1/3} 5 \Gamma(1/3)} \left(\frac{\epsilon}{\epsilon_c}\right)^{1/3} \qquad (3.1.4)$$



Cumulative energy distribution $\mathcal{P}(\epsilon/\epsilon_c)$.

About 40 values of $\mathcal{P}(\epsilon/\epsilon_c)$ computed from eq. 3.1.3 [31], honestly spread over a range $\epsilon/\epsilon_c \leq 10$ are tabulated in **zgoubi** source file (see figure). In order to get ϵ/ϵ_c , first a random value $0 < \mathcal{P} < 1$ is generated uniformly, then ϵ/ϵ_c is drawn either by simple inverse linear interpolation of the tabulated values if $\mathcal{P} > 0.26$ (corresponding to $\epsilon/\epsilon_c > 10^{-2}$), or, if $\mathcal{P} < 0.26$ from eq. 3.1.4 that gives $\epsilon/\epsilon_c = \left(\frac{2^{1/3} 5 \Gamma(1/3)}{12\sqrt{3}\mathcal{P}}\right)^3$

precision no less than 1% at $\mathcal{P} \rightarrow 0.26$.

When SR loss tracking is requested, several optical elements that contain a dipole magnetic field component (e.g., MULTIPOL, BEND) provide a printout of various quantities related to SR emission, as drawn from classical theoretical expressions, such as for instance,

- energy loss per particle $\Delta E(eV) = \frac{2}{3}r_0c\gamma^3 B(T)\Delta\theta$, with B the dipole field exclusive of any other multipole component in the magnet, $\Delta\theta$ the total deviation as calculated from B, from the magnet length, and from the reference rigidity BORO (as defined with, e.g., [MC]OBJET)

- critical energy
$$\epsilon_c(eV) = \frac{3\gamma^3 c}{2\rho} \frac{\hbar}{e}$$
, with $\rho = BORO/B$

- average energy of the photons radiated $<\epsilon>=rac{8}{15\sqrt{3}}\epsilon_c$,

- rms energy of radiated photons $\epsilon_{rms} = 0.5591\epsilon_c$,

- number of radiated photons per particle $N = \Delta E / \langle \epsilon \rangle$.

This is done in order to facilitate verifications, since on the other hand statistics regarding those values are drawn from the tracking and may be printed using the dedicated keyword SRPRNT.

Finally, upon user's request as well, SR loss can be limited to particular classes of optical elements, for instance dipole magnets alone, or dipole + quadrupole magnets, etc. This option is made available in order to allow further inspection, or easier comparison with other codes, for instance.

iiiiiii .mine

Synchrotron Radiation Integrals

Numerical computation of Synchrotron radiation integrals, if requested, is a subproduct of the stepwise integration of particle motion⁵. The process is managed by the *TWISS* procedure, SR integrals computation is triggered if (and only if) *SRLOSS* is present in the input sequence. The integral values so obtained are part of the data inventory in the zgoubi.TWISS.out output file header.

Synchrotron radiation integrals are evaluated by stepwise integration (using a mid-point method) along a reference orbit, therefore requiring prior knowledge - or computation - of the latter. If that quantity is known, it may just be specified as the initial coordinates in *OBJET*. If not, then a *FIT* of the initial orbit conditions will update *OBJET* data to the required values. Note that, in the case of a ring sequence, these initial conditions are expected to be the periodic orbit coordinates, which *FIT[2]* can find. *UNDER INSTALLATION/BENCHMARKING. TO BE DOCUMENTED FURTHER*.

3.2 Spectral-Angular Radiated Densities

Most of the content in the present section is drawn from Refs. [32, 33, 34].

The ray-tracing procedures provide the ingredients necessary for the determination of the electric field radiated by the particle subject to acceleration, as shown in Fig. 6, this is developed in section 3.2.1. These ingredients further allow calculating the spectral-angular density of the radiation⁶, this is developed in section 3.2.2.

3.2.1 Calculation of the Radiated Electric Field

The expression for the radiated electric field $\vec{\mathcal{E}}(\vec{n},\tau)$ as seen by the observer in the long distance approximation is [35]

$$\vec{\mathcal{E}}(\vec{n},\tau) = \frac{q}{4\pi\varepsilon_0 c} \frac{\vec{n}(t) \times \left[\left(\vec{n}(t) - \vec{\beta}(t) \right) \times d\vec{\beta}/dt \right]}{r(t) \left(1 - \vec{n}(t) \cdot \vec{\beta}(t) \right)^3}$$
(3.2.1)

where t is the time in which the particle motion is described and τ is the observer time. Namely, when at position $\vec{r}(t)$ with respect to the observer (or as well at position $\vec{R}(t) = \vec{X} - \vec{r}(t)$ in the (O, x, y, z) frame) the particle emits a signal which reaches the observer at time τ , such that $\tau = t + r(t)/c$ where r(t)/c is the delay necessary for the signal to travel from the emission point to the observer, which also leads by differentiation to the well-known relation

$$\frac{d\tau}{dt} = 1 - \vec{n}(t) \cdot \vec{\beta}(t) \tag{3.2.2}$$

The vectors $\vec{R}(t)$ and $\vec{\beta}(t) = \frac{v}{c}\vec{u}$ (eq. 1.2.2) that describe the motion are obtained from the ray-tracing (eqs. 1.2.4). The acceleration is calculated from (a form of eq. 1.2.1 with $\vec{e} = 0$)

$$\frac{d\vec{\beta}}{dt} = \frac{q}{m}\,\vec{\beta}(t) \times \vec{b}(t) \tag{3.2.3}$$



Figure 6: A scheme of the reference frame in **zgoubi** together with the vectors entering in the definition of the electric field radiated by the accelerated particle :

(x, y): horizontal plane; z: vertical axis.

 $\vec{R}(t)$ = particle position in the fixed frame (O, x, y, z);

 \vec{X} (time-independent) = position of the observer in the (O, x, y, z) frame ;

 $\vec{r}(t)=\vec{X}-\vec{R}(t)$ = position of the particle with respect to the observer ;

 $\vec{n}(t)$ = (normalized) direction of observation = $\vec{r}(t)/|\vec{r}(t)|$;

 $\vec{\beta}$ = normalized velocity vector of the particle $\vec{v}/c = (1/c)d\vec{R}/dt$.



Figure 7: Left : typical shapes of the $\mathcal{E}_{\sigma}(t)$ and $\mathcal{E}_{\pi}(t)$ components of the electric field impulse (eq. 3.2.1) emitted by a 2.5 GeV electron on a $\rho = 53.6$ m circular trajectory in a l = 20 cm-long dipole, as observed in the direction of the centre of the dipole, $\phi = 0$, $\gamma \psi = 5$ (observation distance r = 10 m). Right : the related spectral angular densities $\partial^3 W_{\sigma, \pi}/\partial \phi \, \partial \psi \, \partial \omega$ (eq. 3.2.10). After Ref. [34].

Then, given the observer position \vec{X} in the fixed frame, it is possible to calculate

$$\vec{r}(t) = \vec{X} - \vec{R}(t)$$
 and $\vec{n}(t) = \frac{\vec{r}(t)}{|\vec{r}(t)|}$ (3.2.4)

As an illustration, Fig. 7 has been produced using **zpop**, it shows the typical shape of the electric field impulse at the observer, with central peak width [34]

$$2\tau_c = 2\frac{2\rho}{3\gamma^3 c} (1+\gamma^2\psi^2)^{3/2}$$

Computation of $\vec{n}-\vec{\beta}$ and $1-\vec{n}\cdot\vec{\beta}$

Owing to computer precision the crude computation of $\vec{n} - \vec{\beta}$ and $1 - \vec{n} \cdot \vec{\beta}$ may lead to

$$\vec{n} - \vec{\beta} = 0$$
 and $1 - \vec{n} \cdot \vec{\beta} = 0$

since the preferred direction of observation is generally almost parallel to $\vec{\beta}$ (in that case, parallel in the sense of computer precision), while $\beta \approx 1$ as soon as particle energies of a few hundred times the rest mass are concerned.

It is therefore necessary to express $\vec{n} - \vec{\beta}$ and $1 - \vec{n} \cdot \vec{\beta}$ in an adequate form for achieving accurate software computation.

The expression for \vec{n} is

$$\vec{n} = (n_x, n_y, n_z) = (\cos\psi\,\cos\phi, \cos\psi\,\sin\phi, \sin\psi) \\ = \left[1 - 2(\sin^2\phi/2 + \sin^2\psi/2) + 4\sin^2\phi/2\sin^2\psi/2, \sin\phi(1 - 2\sin^2\psi/2), \sin\psi\right] \quad (3.2.5)$$

where ϕ and ψ are the observation angles, given by

$$\phi = \operatorname{Atg}\left(\frac{r_y}{r_x}\right) \text{ and } \psi = \operatorname{Atg}\left(\frac{r_z}{\sqrt{r_x^2 + r_y^2}}\right)$$
(3.2.6)

with $\vec{r} = (r_x, r_y, r_z)$, while $\vec{\beta}$ can be written under the form

$$\vec{\beta} = (\beta_x, \beta_y, \beta_z) = \left[\sqrt{(\beta^2 - \beta_y^2 - \beta_z^2)}, \beta_y, \beta_z\right] \\ = \left[\sqrt{(1 - 1/\gamma^2 - \beta_y^2 - \beta_z^2)}, \beta_y, \beta_z\right] = (1 - a/2 + a^2/8 - a^3/16 + \dots, \beta_y, \beta_z) \quad (3.2.7)$$

where $a=1/\gamma^2+\beta_y^2+\beta_z^2.$ This leads to

$$n_x = 1 - \varepsilon_x$$
 and $\beta_x = 1 - \xi_x$

with

$$\varepsilon_x = 2(\sin^2 \phi/2 + \sin^2 \psi/2) - 4\sin^2 \phi/2 \sin^2 \psi/2$$

and

$$\xi_x = a/2 - a^2/8 + a^3/16 + \dots$$

All this provides, on the one hand,

$$\vec{n} - \vec{\beta} = \left(-\varepsilon_x + \xi_x, n_y - \beta_y, n_z - \beta_z\right), \qquad (3.2.8)$$

whose components are combinations of terms of the same order of magnitude (ε_x and $\xi_x \sim 1/\gamma^2$ while n_y, β_y, n_z and $\beta_z \sim 1/\gamma$) and, on the other hand,

$$1 - \vec{n} \cdot \vec{\beta} = \varepsilon_x + \xi_x - n_y \beta_y - n_z \beta_z - \varepsilon_x \xi_x , \qquad (3.2.9)$$

that combines terms of the same order of magnitude ($\varepsilon_x, \xi_x, n_y \beta_y$ and $n_z \beta_z \sim 1/\gamma^2$), plus $\varepsilon_x \beta_x \sim 1/\gamma^4$. The precision of these expressions is directly related to the order at which the series

$$\xi_x = a/2 - a^2/8 + a^3/16 + \dots \qquad (a = 1/\gamma^2 + \beta_y^2 + \beta_z^2)$$

is pushed, however the convergence is fast since $a \sim 1/\gamma^2 \ll 1$ in situations of concern.

3.2.2 Calculation of the Fourier Transform of the Electric Field

The Fourier transforms

$$FT_{\omega}[\vec{\mathcal{E}}(\tau)] = \int \vec{\mathcal{E}}(\tau) e^{-i\omega\tau} d\tau$$

of the σ and π electric field components provide the spectral angular energy density

$$\frac{\partial^3 W}{\partial \phi \, \partial \psi \, \partial \omega} = \frac{r^2}{\mu_0 c} \left| FT_\omega \left(\vec{\mathcal{E}}(\tau) \right) \right|^2 \tag{3.2.10}$$

Fig. 7-right gives a typical example in the case of a short magnet. These Fourier transforms are computed without resorting to FFT techniques, namely from

$$FT_{\omega}\left[\vec{\mathcal{E}}(\tau)\right] \approx \sum \vec{\mathcal{E}}(\tau_k) e^{-i\omega\tau_k} \Delta \tau_k$$
(3.2.11)

for two reasons. On the one hand, the number of integration steps Δs that define the trajectory (eqs. 1.2.4), is arbitrary and therefore in general not of order 2^n . On the other hand, the integration step defines a constant time differential element $\Delta t_k = \Delta s/\beta c$ which results in the observer differential time element $\Delta \tau_k$, which is also the differential element of the Fourier transform, being non-constant, since both are related by eq. 3.2.2 in which $\vec{\beta}$ and \vec{n} vary as a function of the integration step number k.

An additional issue is that $\Delta \tau_k$ may reach drastically small values in the region of the central peak of the electric impulse emitted in a dipole, *i.e.*, $1 - \vec{n}(t) \cdot \vec{\beta}(t) \rightarrow 1/2\gamma^2$, whereas the total integrated time $\sum_{k=1}^{N} \Delta \tau_k$ may be several orders of magnitude larger. In terms of the physical phenomenon, the total duration of the electric field impulse as seen by the observer corresponds to the time delay $\sum_{k=1}^{N} \Delta \tau_k$ that separates photons emitted at the entrance of the magnet from photons emitted at the exit, but the significant part of it (in terms

of energy density) which can be represented by the width $2\tau_c = 2 \frac{2\rho}{3\gamma^3 c} (1 + \gamma^2 \psi^2)^{3/2}$ of the radiation peak,

is a very small fraction of $\sum_{k=1}^{N} \Delta \tau_k$.

The consequence is that, again in relation to computer precision, the differential element $\Delta \tau_k$ involved in the computation of eq. 3.2.11 cannot be derived from such relation as $\Delta \tau_k = \sum_{k=1}^n \Delta \tau_k - \sum_{k=1}^{n-1} \Delta \tau_k$ but instead must be stored as is, in the course of the ray-tracing process, for subsequent data treatment.

4 SPACE CHARGE

zgoubi provides models for the simulation of space charge effects. This capability has been first developped in the context of a PhD work regarding fixed field ring proton driver design studies and accelerator-driven subcritical reactor applications. This section of the guide is essentially drawn from that PhD dissertation [36, 38], which can be referred to for additional details - the document provides benchmarking proofs in both KV and Gaussian density models (see below), including bunch transport in a drift, transport in a beam line, bunch tracking in an FFAG ring represented using either **zgoubi**'s *FFAG* keyword or magnetic field maps.

TO BE DOCUMENTED FURTHER.

5 ORBIT CORRECTION

Orbit correction in simple cases can be attempted using the *FIT[2]* procedure.

However, **zgoubi** provides an SVD orbit correction method. It is activate by the keyword *SVDOC*. Details can be found in Sec. 6.4, p. 186.

TO BE DOCUMENTED FURTHER.

6 WHAT KEYWORDS DO, AND OTHER AVAILABLE PROCEDURES

6.1 Introduction

This chapter gives an inventory of the procedures available in **zgoubi**, their associated "keyword", and a brief description of the way they function.

The chapter has been split into several sections. Sections 6.2 to 6.5 explain the underlying content - physics and numerical methods - behind the keywords, they are organized by topics :

- How to defined an object (a set of initial coordinates),
- Available options,
- Optical elements and procedures,
- Output procedures.

Section 7 addresses further a series of functionalities that may be accessed by means of special input data or flags.

6.2 Definition of an Object

The description of the object, *i.e.*, initial coordinates of the ensemble of particles, must be the first procedure in the **zgoubi** input data file, zgoubi.dat.

Several types of automatically generated objects are available, they are described in the following pages and include,

- non-random object, with various distributions : individual particles, grids, object for MATRIX, etc.
- Monte Carlo distribution, with various distributions as well : 6-D window, ellipsoids, etc.

A recurrent quantity appearing in these procedures is *IMAX*, the number of particles to be ray-traced. The maximum value allowed for *IMAX* can be changed at leisure in the include file 'MAXTRA.H' where it is defined (that requires re-compiling **zgoubi**).

MCOBJET : Monte-Carlo generation of a 6-D object

MCOBJET generates a set of *IMAX* random 6-D initial conditions (the maximum value for *IMAX* is defined in the include file 'MAXTRA.H'). It can be used in conjunction with the keyword *REBELOTE* which either allows generating an arbitrarily high number of initial conditions, or, in the hypothesis of a periodic structure, allows multi-turn tracking with initial conditions at pass number *IPASS* identical to the conditions at end of pass number *IPASS*-1.

The first datum in *MCOBJET* is the reference rigidity (a negative value is allowed)

$$BORO = \frac{p_0}{q} (\text{kG.cm})$$

Depending on the value of the next datum, *KOBJ*, the *IMAX* particles have their initial random conditions Y, T, Z, P, X and D (relative rigidity, $B\rho/BORO$) generated on 3 different types of supports, as described below.

Next come the data

KY, KT, KZ, KP, KX, KD

that specify the type of probability density for the 6 coordinates. *KY*, *KT*, *KZ*, *KP*, *KX* can take the following values :

1. uniform density, $p(x) = 1/2\delta x$ if $-\delta x \le x \le \delta x$, p(x) = 0 elsewhere,

2. Gaussian density,
$$p(x) = \frac{1}{\delta x \sqrt{2\pi}} e^{-\frac{x^2}{2\delta x^2}}$$

3. parabolic density, $p(x) = \frac{3}{4\delta x}(1 - \frac{x^2}{\delta x^2})$ if $-\delta x \le x \le \delta x$, p(x) = 0 elsewhere.

KD can take the following values :

- 1. uniform density, $p(D) = 1/2\delta D$ if $-\delta D \le \delta D$, p(D) = 0 elsewhere,
- 2. exponential density, $p(D) = N_0 \exp(C_0 + C_1 l + C_2 l^2 + C_3 l^3)$ with $0 \le l \le 1$ and $-\delta D \le \delta D$,
- 3. p(D) is determined by a kinematic relation, namely, with T = horizontal angle, $D = \delta D * T$.

Next come the central values for the random sorting,

$$Y_0, T_0, Z_0, P_0, X_0, D_0$$

namely, the probability density laws p(x) (x = Y, T, Z, P or X) and p(D) described above apply to the variables $x - x_0$ ($\equiv Y - Y_0, T - T_0, ...$) and $D - D_0$ respectively. Negative value for D_0 is allowed (see section 7.13, page 211).

KOBJ = 1 : Random generation of *IMAX* particles in a hyper-window with widths (namely the half-extent for uniform or parabolic distributions (KY, KT, ... = 1 or 3), and the r.m.s. width for Gaussian distributions (KY, KT, ... = 2))

$$\delta Y, \quad \delta T, \quad \delta Z, \quad \delta P, \quad \delta X, \quad \delta D$$

Then follow the cut-off values, in units of the r.m.s. widths δY , δT , ... (used only for Gaussian distributions, $KY, KT, \ldots = 2$)

 $N_{\delta Y}, N_{\delta T}, N_{\delta Z}, N_{\delta P}, N_{\delta X}, N_{\delta D}$

The last data are the parameters

$$N_0, \quad C_0, \quad C_1, \quad C_2, \quad C_3$$

needed for generation of the D coordinate upon option KD = 2 (unused if KD = 1, 3) and a set of three integer seeds for initialization of random sequences,

$$IR1, IR2, IR3$$
 (all $\simeq 10^6$)

All particles generated by *MCOBJET* are tagged with a (non-S) character, for further statistic purposes (*e.g.*, with *HISTO*, *MCDESINT*).

KOBJ = 2 : Random generation of IMAX = IY * IT * IZ * IP * IX * ID particles on a hyper-grid. The input data are the number of bars in each coordinate

IY, IT, IZ, IP, IX, ID

the spacing of the bars

PY, PT, PZ, PP, PX, PD

the width of each bar

 $\delta Y, \quad \delta T, \quad \delta Z, \quad \delta P, \quad \delta X, \quad \delta D$

the cut-offs, used with Gaussian densities (in units of the r.m.s. widths)

$$N_{\delta Y}, \quad N_{\delta T}, \quad N_{\delta Z}, \quad N_{\delta P}, \quad N_{\delta X}, \quad N_{\delta D}$$

This is illustrated in Fig. 8.

The last two sets of data in this option are the parameters

$$N_0, \quad C_0, \quad C_1, \quad C_2, \quad C_3$$

needed for generation of the D coordinate upon option KD= 2 (unused if KD= 1, 3) and a set of three integer seeds for initialization of random sequences, IR1, IR2, and IR3 (all $\simeq 10^6$).

All particles generated by *MCOBJET* are tagged with a (non-S) character, for further statistic purposes (see *HISTO and MCDESINT*).

KOBJ = 3 : Distribution of *IMAX* particles in a 6-D ellipsoid (with possible momentum correlation via dispersion) defined by the three sets of data (one set per 2-D phase-space)

$$\begin{array}{lll} \alpha_{Y}, & \beta_{Y}, & \frac{\varepsilon_{Y}}{\pi}, & N_{\varepsilon_{Y}} & [, & N'_{\varepsilon_{Y}}, \text{ if } N_{\varepsilon_{Y}} < 0] & [, & D_{Y}, & D_{T}] \\ \alpha_{Z}, & \beta_{Z}, & \frac{\varepsilon_{Z}}{\pi}, & N_{\varepsilon_{Z}} & [, & N'_{\varepsilon_{Z}}, & \text{if } N_{\varepsilon_{Z}} < 0] & [, & D_{Z}, & D_{P}] \\ \alpha_{X}, & \beta_{X}, & \frac{\varepsilon_{X}}{\pi}, & N_{\varepsilon_{X}} & [, & N'_{\varepsilon_{X}}, & \text{if } N_{\varepsilon_{X}} < 0], \end{array}$$

where $\alpha_{X,Y,Z}$, $\beta_{X,Y,Z}$, $D_{Y,T}$, $D_{Z,P}$ are the ellipse parameters and the dispersions and derivatives, $\varepsilon_{X,Y,Z}/\pi$ are the *rms* emittances. This defines for each plane an elliptical frontier :

$$\frac{1+\alpha_Y^2}{\beta_Y}Y^2 + 2\alpha_Y YT + \beta_Y T^2 = \varepsilon_Y/\pi,$$
$$\frac{1+\alpha_Z^2}{\beta_Z}Z^2 + 2\alpha_Z ZP + \beta_Z P^2 = \varepsilon_Z/\pi,$$
$$\frac{1+\alpha_l^2}{\beta_l}l^2 + 2\alpha_l l\delta + \beta_l \delta^2 = \varepsilon_l/\pi,$$

with l the bunch length variable (unit is cm) and δ a short notation for $\delta p/p$, momentum spread.

Sorting cut-offs N_{ε_Y} , N_{ε_Z} and N_{ε_X} are accounted for if distributions are Gaussian (KY, KT, ... = 2); in this case *rms* values are

$$\sigma_Y = \sqrt{\beta_Y \times \varepsilon_Y / \pi} \text{ and } \sigma_T = \sqrt{\gamma_Y \times \varepsilon_Y / \pi},$$

$$\sigma_Z = \sqrt{\beta_Z \times \varepsilon_Z / \pi} \text{ and } \sigma_P = \sqrt{\gamma_Z \times \varepsilon_Z / \pi},$$

 $\sigma_l = \sqrt{\beta_l \times \varepsilon_l / \pi}$ (bunch length, unit cm), and $\sigma_{\delta} = \sqrt{\gamma_l \times \varepsilon_l / \pi}$ momentum spread.

For uniform sorting, the distribution extends over the intervals, for respectively the radial, axial and longitudinal distribution,

$$\pm \sqrt{\varepsilon_Y / \pi \times \beta_Y} \text{ and } \pm \sqrt{\varepsilon_Y / \pi \times \gamma_Y}$$

$$\pm \sqrt{\varepsilon_Z / \pi \times \beta_Z} \text{ and } \pm \sqrt{\varepsilon_Z / \pi \times \gamma_Z},$$

$$\pm \sqrt{\varepsilon_l / \pi \times \beta_l} \text{ and } \pm \sqrt{\varepsilon_l / \pi \times \gamma_l}.$$

• N_{ε} may be negative. The meaning of this is for the sorting to fill up an elliptical ring that extends from $|N_{\varepsilon}|$ to N'_{ε} (rather than the inner region determined by the N_{ε} cut-off as discussed above, when $N_{\varepsilon} > 0$).



Figure 8: A scheme of input parameters to MCOBJET when KOBJ= 2. Top : Possible distributions of the Y coordinate. Bottom : A 2-D grid in (Y, Z) space.

OBJET : Generation of an object

OBJET is dedicated to the construction of sets of initial coordinates, in several ways.

The first datum is the reference rigidity (a negative value is allowed)

$$BORO = \frac{p_0}{q}$$

At the object, the beam is defined by a set of *IMAX* particles (the maximum value for *IMAX* is defined in the include file 'MAXTRA.H') with the initial conditions (Y, T, Z, P, X, D) with $D = B\rho/BORO$ the relative rigidity.

Depending on the value of the next datum *KOBJ*, these initial conditions may be generated in different ways, as follows.

KOBJ = 1 : Defines a grid in the Y, T, Z, P, X, D space. One defines the number of points desired

IY, IT, IZ, IP, IX, ID

with $IY \leq n_Y \dots ID \leq n_D$ such that $n_Y \times n_T \times \dots \times n_D \leq max(IMAX)$. One defines the sampling range in each coordinate

dY, dT, dZ, dP, dX, dD

zgoubi then generates IMAX = IY * IT * IZ * IP * IX * ID particles with initial coordinates

0,	$\pm dY$,	$\pm 2 * dY$,	,	$\pm IY/2 * dY,$
0,	$\pm dT$,	$\pm 2 * dT$,	,	$\pm IT/2 * dT$,
0,	$\pm dZ$,	$\pm 2 * dZ$,	,	$\pm IZ/2 * dZ,$
0,	$\pm dP$,	$\pm 2 * dP$,	,	$\pm IP/2 * dP$,
0,	$\pm dX$,	$\pm 2 * dX$,	,	$\pm IX/2 * dX,$
0,	$\pm dD$,	$\pm 2 * dD$,	,	$\pm ID/2 * dD$,

In this option relative rigidities will be classified automatically in view of possible further use of IMAGES[Z] for momentum analysis and image formation.

The particles are tagged with an index *IREP* possibly indicating a symmetry with respect to the (X,Y) plane, as explained in option *KOBJ*= 3. If two trajectories have mid-plane symmetry, only one will be ray-traced, while the other will be deduced using the mid-plane symmetries. This is done for the purpose of saving computing time. It may be non-compatible with the use of some procedures (*e.g. MCDESINT*, which involves random processes) or with the use of non mid-plane symmetric fields.

The last datum is a reference in each coordinate, YR, TR, ZR, PR, XR, DR. For instance the reference rigidity is DR * BORO, resulting in the rigidity of a particle defined by I * dD to be (DR + I * dD) * BORO.

KOBJ = 1.1 : The initial Z and P conditions are

0, dZ, 2 * dZ, ..., (IZ - 1) * dZ, 0, dP, 2 * dP, ..., (IP - 1) * dP,

This object results in shorter outputs/CPU-time when studying problems with Z symmetry.

KOBJ = 1.2 : Same as *KOBJ*= 1, but the mid-plane symmetry of the tracking is lifted, all particles are actually tracked.

KOBJ = 2 : Next data : *IMAX*, *IDMAX*. Initial coordinates are entered explicitly for each trajectory. *IMAX* is the total number of particles. These may be classified in groups of equal number for each value of momentum, in order to fulfill the requirements of image calculations by IMAGES[Z]. *IDMAX* is the number of groups of momenta. The following initial conditions defining a particle are specified for each one of the *IMAX* particles

 $Y, \quad T, \quad Z, \quad P, \quad X, \quad D, \quad 'A'$

where D * BORO is the rigidity (negative value allowed) and 'A' is a (arbitrary) tagging character.

The last record *IEX* (I=1, *IMAX*) contains *IMAX* times either the character "1" to indicates that the particle has to be tracked, or "-9" to indicates that the particle should not be tracked.

This option KOBJ= 2 may be be useful for the definition of objects including kinematic effects.

KOBJ = 2.1 : Same as *KOBJ*= 2 except for the units, meter and radian in that case.

Note that in this option KOBJ = 2[.]], only the first 7 trajectories can possibly have their coordinates varied when using the *FIT*[2] procedure.

KOBJ = 3 : This option allows the reading of initial conditions, including spin coordinates, from an external input file *FNAME*.

The next three data lines are :

IT1, IT2, ITStep IP1, IP2, IPStep YF, TF, ZF, PF, SF, DPF, TiF, TAG YR, TR, ZR, PR, SR, DPR, TiR InitC

followed by the storage file name FNAME.

IT1, IT2, ITStep cause the code to read coordinates of particles number IT1 through IT2 by step ITStep.

IP1, *IP2*, *IPStep* cause the code to read coordinates belonging in the passes range *IP1* through *IP2*, step *IPStep*.

YF, TF, ZF, PF, SF, DPF, TiF are scaling factors whereas YR, TR, ZR, PR, SR, DPR, TiR are references added to the values of respectively Y, T, Z, P, S, DP as read in file *FNAME*, so that any coordinate C = Y, T, Z... is changed into CF*C + CR. In addition a flag character TAG allows retaining only particles with identical tagging letter LET, unless TAG='*' in which case it has no selection effect - for instance TAG='S' can be used to retain only secondary particles following in-flight decay simulations.

If InitC = 1 ray-tracing starts from the current coordinates F(J, I),

if InitC = 0 ray-tracing starts from the initial coordinates FO(J, I), as read from file FNAME.

The file *FNAME* must be formatted in the same way as a zgoubi.fai ouptput file, following the *FORTRAN* sequence below - details and possible updates are to be found in the source file ' obj3.f':

```
OPEN (UNIT = NL, FILE = FNAME, STATUS = 'OLD')
DO I = 1, IMAX
   READ (NL, 100)
         IEX(I),-1.D0+FO(1,I), (FO(J,I), J=2, MXJ),
    1
          -1.D0+F(1,I),F(2,I),F(3,I),
         (F(J,I), J=4, MXJ),
          (SI(J,I), J=1,4), (SF(J,I), J=1,4),
    4
    5
         ENEKI, ENERG,
    6
          I, IREP(I), SORT(I), (AMQ(J,I), J=1,5), PH(I), DPR(I), PS,
         BORO, IPASS, NOEL,
KLEY, LBL1C, LBL2C, LETC,
    8
    9
          SRLT(I), DPREF, HDPRF, DMY, HMS,
         NI, MXITR, NBFT, KBYD, LAST
 ENDDO
```

The meaning of some of the parameters above is the following (see Sec. 8.2 for the detailed content of a zgoubi.fai style of file) :

IEX(I)	: flag, see <i>KOBJ</i> = 2 and page 211
FO(1-6,I)	: coordinates D, Y, T, Z, P and path length of particle num-
	ber I, at the origin. $D * BORO =$ rigidity
<i>F</i> (1-6, <i>I</i>)	: <i>idem</i> , at the current position
(SI(J,I),J=1,4),(SF(J,I),J=1,4)	: initial and current spin coordinates
etc.	:
LETC	: one-character string (for tagging)
etc.	:

IREP is an index which indicates a symmetry with respect to the median plane. For instance, if Z(I+1) = -Z(I), then normally *IREP*(I+1) = *IREP*(I). Consequently the coordinates of particle I + 1 will not be obtained from ray-tracing but instead deduced from those of particle I by simple symmetry. This saves on computing time.

KOBJ= 3 can be used for reading files filled by FAISCNL or FAISTORE. If more than MaxIMAX⁷ particles are to be read from a file, use REBELOTE.

Note : In this option, one has to make sure that input data do not conflict with possible use of the keyword *PARTICUL* that assigns mass and charge.

KOBJ = 3.1 : Same as **KOBJ = 3**, except for the formatting of trajectory coordinate data in *FNAME*, namely, according to the following *FORTRAN* sequence

```
OPEN (UNIT = NL, FILE = FNAME, STATUS = 'OLD')

1 CONTINUE

READ (NL,*,END=10,ERR=99) Y, T, Z, P, S, D

GOTO 1

10 CALL ENDFIL

99 CALL ERREAD
```

KOBJ = 3.2 to 3.6 : As for **KOBJ=3.1**, except for a different format, as follows:

3.2: READ (NL,*) X, Y, Z, PX, PY, PZ
with PX, PY, and PZ, the momenta in MeV/c.
3.3: READ (NL,*) DP, Y, T, Z, P, S, TIME, MASS, CHARGE
with MASS the mass in MeV/c² and CHARGE the charge in units of the elementary charge.
3.4: READ (NL,*) Y, T, Z, P, S, DP, LET, IEN, IT
with LET a tag letter, IEN an integer, IT the particle number.
3.5: READ (NL,*, ERR=97, END=95) Y, T, Z, P, TIME, GAMMA
with TIME the particle time and GAMMA its Lorentz relativistic factor.
3.6: READ (NL,*) Y, Z, X, PY, PZ, PX
similar to 3.2, just a different ordering of the coordinates.

Note 1 : Conversion from the input file to proper units (namely, Y, Z in cm, T, P in mrad, path variable in cm, time in μ s), can be performed using the scaling factors YF, YF, etc. (see above). **Note 2 :** For details and possible updates in the formatted read of concern in the EORTRAN regarding

Note 2 : For details and possible updates in the formatted read of concern in the *FORTRAN*, regarding options 3.1-3.5 and possibly beyond, see the source file 'obj3.f'.

RECOVERING FROM A CRASH :

OBJET with option *KOBJ*=3 can be used to recover from a job crash, which would occur when multi-turn tracking - due to computer crash or else. This is discussed in the *SCALING* section, page 178, an example of job resuming is given page 299.

KOBJ = 5 : Mostly dedicated to the calculation of first order transport matrix and various other optical parameters, using for instance *MATRIX* or *TWISS*. The user defines the coordinate sampling

dY, dT, dZ, dP, dS, dD

These values should be small enough, so that the paraxial ray approximation be valid. The code generates 13 particles, with initial coordinates

0, $YR \pm dY$, $TR \pm dT$, $ZR \pm dZ$, $PR \pm dP$, $SR \pm dS$, $DR \pm dD$

given the reference trajectory

YR, TR, ZR, PR, DR

(with DR * BORO the reference rigidity - negative value allowed).

 7 Max(*IMAX*) here stands for the maximum number of particles allowed in one go. The reason for a limitation is the dimensioning of arrays in the source code: Max(*IMAX*) is controlled, and can be changed, in the include file [pathTo]/include/MAXTRA.H.

KOBJ = 5.1 : Same as KOBJ = 5, except for an additional data line giving initial beam ellipse parameters and dispersions, α_Y , β_Y , α_Z , β_Z , α_X , β_X , D_Y , D_Y , D_Z , D_Z , for further transport of these using *MATRIX* or *OPTICS*, or for possible use by the *FIT*[2] procedure.

KOBJ = 5.N ($N \ge 2$) : Like *KOBJ = 5* except for its allowing $N \ge 2$ reference trajectories, rather than just one as in *KOBJ = 5* case (thus *N*-1 additional input data lines are needed in this case). These reference trajectories can be for instance chromatic orbits. Zgoubi will generate *N* sets of 13 particles with initial coordinates in each set taken *wrt*. one of the *N* references.

A subsequent use of MATRIX would then cause the computation of N transport matrices.

Note that in the option KOBJ= 5.N, $N \ge 2$, only the first 7 reference trajectories can possibly have their coordinates varied when using the FIT[2] procedure.

KOBJ = 6 : Dedicated to the calculation of first and second order transport matrices, and some additional higher order transport coefficients, using for instance *MATRIX*. The input data are a reference trajectory and a coordinate sampling with respect to that reference (normally taken paraxial)

dY, dT, dZ, dP, dD

to allow the building up of an object containing 61 particles (note : their coordinates can be checked by printing out into zgoubi.res using *FAISCEAU*), whereas a last data line gives the reference

YR, TR, ZR, PR, DR

(with DR * BORO the reference rigidity - negative value allowed), which adds to the previous coordinate values.

KOBJ = 6.1 : Dedicated to the calculation of first, second and third order transport matrices, using for instance *MATRIX*. It builds fort that a 102 particle initial object. The sampling and functionning are similar to the 61 particle (KOBJ=6) and 13 particle (KOBJ=5) object cases.

KOBJ = 7 : Object with kinematics

The data and functioning are the same as for KOBJ= 1, except for the following

- *ID* is not used,
- PD is the kinematic coefficient, such that for particle number I, the initial relative rigidity D_I is calculated from the initial angle T_I following

$$D_I = DR + PD * T_I$$

while T_I is in the range

```
0, \pm PT, \pm 2 * PT, ..., \pm IT/2 * PT
```

as when using *KOBJ*= 1.

KOBJ = 8 : Generation of phase-space coordinates on ellipses. The ellipses are defined by the three sets of data (one set per ellipse)

where α , β are the ellipse parameters and ε / is the ellipse surface, corresponding to an ellipse with equation

$$\frac{1+\alpha_Y^2}{\beta_Y}Y^2 + 2\alpha_Y YT + \beta_Y T^2 = \varepsilon_Y/\pi$$

(*idem* for the (Z, P) or (X, D) planes).

The ellipses are centered respectively on (Y_0, T_0) , (Z_0, P_0) , (X_0, D_0) .

The number of samples per plane is respectively IX, IY, IZ. If that value is zero, the central value above is assigned.

OBJETA : Object from Monte-Carlo simulation of decay reaction

This generator simulates the reactions[39]

$$M_1 + M_2 \longrightarrow M_3 + M_4$$

and then

$$M_4 \longrightarrow M_5 + M_6$$

where M_1 is the mass of the incoming body; M_2 is the mass of the target; M_3 is an outgoing body; M_4 is the rest mass of the decaying body; M_5 and M_6 are decay products. Example :

$$p + d \longrightarrow^{3} \operatorname{He} + \eta$$

 $\eta \longrightarrow \mu^{+} + \mu^{-}$

The first input data are the reference rigidity

$$BORO = p_0/q$$

an index *IBODY* which specifies the particle to be ray-traced, namely M3 (*IBODY* = 1), M5 (*IBODY* = 2) or M6 (*IBODY* = 3). In this last case, initial conditions for M6 must be generated by a first run of *OBJETA* with *IBODY* = 2; they are then stored in a buffer array, and restored as initial conditions at the next occurrence of *OBJETA* with *IBODY* = 3. Note that **zgoubi** by default assumes positively charged particles.

Another index, *KOBJ*, specifies the type of distribution for the initial transverse coordinates Y, Z; namely either uniform (*KOBJ*= 1) or Gaussian (*KOBJ*= 2). The other three coordinates T, P and D are deduced from the kinematic of the reactions.

The next data are the number of particles to be generated, *IMAX*, the masses involved in the two previous reactions.

 $M_1, M_2, M_3, M_4, M_5, M_6$

and the kinetic energy T_1 of the incoming body (M_1) . Then one gives the central value of the distribution for each coordinate

 $Y_0, \quad T_0, \quad Z_0, \quad P_0, \quad D_0$

and the width of the distribution around the central value

$$\delta Y, \quad \delta T, \quad \delta Z, \quad \delta P, \quad \delta D$$

so that only those particles in the range

$$Y_0 - \delta Y \le Y \le Y_0 + \delta Y$$
 ... $D_0 - \delta D \le D \le D_0 + \delta D$

will be retained. The longitudinal initial coordinate is uniformly sorted in the range

$$-XL \le X_0 \le XL$$

The random sequences involved may be initialized with different values of the two integer seeds IR_1 and $IR_2 (\simeq 10^6)$.

Possible use of *PARTICUL* will have no effect : it will not change the mass and charge assumptions as set by *OBJETA*.

6.3 Optical Elements and Related Numerical Procedures

AGSMM : AGS main magnet

The AGS main magnet is a combined function dipole with straight axis (lines of constant field are straight lines).

The field computation routines for *AGSMM* are the same as for *MULTIPOL* (details in section 1.3.7, page 28), however *AGSMM* has the following four particularities :

- There are only three multipole components present in AGSMM : dipole, quadrupole and sextupole.
- The dipole field B_0 is drawn from the reference rigidity, $B\rho_{ref}$, and follows the latter so to preserve $\rho = B\rho_{ref}/B_0$ and the orbit deviation L/ρ . In particular,
 - in the absence of acceleration, $B\rho_{ref} \equiv BORO$, with BORO the quantity appearing in the object definition using [MC]OBJET,
 - in presence of acceleration using CAVITE, $B\rho_{ref}$ is changed to $BORO \times D_{ref}$ at each passage in the cavity, with D_{ref} the relative synchronous momentum increase, a quantity that **zgoubi** updates at cavity traversal.
- The field indices, quadrupole K1 and sextupole K2, are derived from the reference rigidity, $B\rho_{ref}$, via momentum-dependent polynomials, taken from Ref. [44], and following in that the methods found in the MAD model of the AGS [45].
- The AGS main dipole has back-leg windings, used for instance for injection and extraction orbit bumps. The number of winding turns and the number of ampere-turns are part of the data in the keyword argument list. The intensity in the windings is accounted for in the conversion from total ampere-turns in the magnet to momentum and then to magnetic field.

Note : A consequence of items 2 and 3 above is that no field value is required in defining the AGS main magnets using *AGSMM*.

(page 227 in PART B)

AGSQUAD : AGS quadrupole

The AGS quadrupoles are regular quadrupoles. The simulation of *AGSQUAD* uses the same field modelling as *MULTIPOL*, section 1.3.7, page 28. However amperes are provided as input to *AGSQUAD* rather than fields, the reason being that some of the AGS quadrupoles have two superimposed coil circuits, with separate power supplies. It has been dealt with this particularity by allowing for an additional set of quadrupole data in *AGSQUAD*, compared to *MULTIPOL*.

The field in *AGSQUAD* is computed using transfer functions, from the specified ampere-turns in the coils to magnetic field at pole-tip, that account for the non-linearity of the magnetic permeability [45].

AIMANT : Generation of dipole mid-plane 2-D map, polar frame

The keyword *AIMANT* provides an automatic generation of a dipole median plane field map in polar coordinates.

A more recent and improved version will be found in *DIPOLE-M*. In addition, a similar modelling, that however skips the stage of an intermediate mid-plane field map, can be found in *DIPOLE[S]*.

The extent of the map is defined by the following parameters, as shown in Figs. 9A and 9B,

AT	:	total angular aperture
RM	:	mean radius used for the positioning of field boundaries
RMIN, RMAX	:	minimum and maximum radial boundaries of the map

The 2 or 3 effective field boundaries (EFB) inside the map are defined from geometric boundaries, the shape and position of which are determined by the following parameters,

ACENT : arbitrary angle, used for the positioning of the EFBs.

- ω : azimuth of an EFB with respect to ACENT
- θ : angle of a boundary with respect to its azimuth (wedge angle)
- R_1, R_2 : radius of curvature of an EFB
- U_1, U_2 : extent of the linear part of the EFB.

At any node of the map mesh, the value of the Z component of the field is calculated as

$$B_Z = \mathcal{F}(R,\theta) * B_0 * \left(1 + N * \left(\frac{R - RM}{RM}\right) + B * \left(\frac{R - RM}{RM}\right)^2 + G * \left(\frac{R - RM}{RM}\right)^3\right)$$
(6.3.1)

where N, B and G are respectively the first, second and third order field indices and $\mathcal{F}(R,\theta)$ is the fringe field coefficient (it determines the "flutter" in periodic structures).

Calculation of the Fringe Field Coefficient

With each EFB a realistic extent of the fringe field, λ , is associated (Figs. 9A and 9B), and a fringe field coefficient F is calculated. In the following λ stands for either λ_E (Entrance), λ_S (Exit) or λ_L (Lateral EFB).

If a node of the map mesh is at a distance of the EFB larger than λ , then F = 0 outside the field map and F = 1 inside. If a node is inside the fringe field zone, then F is calculated as follows.

Two options are available, for the calculation of F, depending on the value of ξ .

If $\xi \ge 0$, F is a second order type fringe field (Fig. 10) given by

$$F = \frac{1}{2} \frac{(\lambda - s)^2}{\lambda^2 - \xi^2} \quad \text{if } \xi \le s \le \lambda$$
(6.3.2)

$$F = 1 - \frac{1}{2} \frac{(\lambda - s)^2}{\lambda^2 - \xi^2}$$
 if $-\lambda \le s \le -\xi$ (6.3.3)

where s is the distance to the EFB, and

$$F = \frac{1}{2} + \frac{s}{\lambda + \xi} \quad \text{if } 0 \le s \le \xi \tag{6.3.4}$$

$$F = \frac{1}{2} - \frac{s}{\lambda + \xi}$$
 if $-\xi \le s \le 0$ (6.3.5)

This simple model allows a rapid calculation of the fringe field, but may lead to erratic behavior of the field when extrapolating out of the median plane, due to the discontinuity of d^2B/ds^2 , at $s = \pm \xi$ and $s = \pm \lambda$. For better accuracy it is advised to use the next option.



- Figure 9: A : Parameters used to define the field map and geometrical boundaries.
 - B : Parameters used to define the field map and fringe fields.

If $\xi = -1$, F is an exponential type fringe field (Fig. 10) given by [46]

$$F = \frac{1}{1 + \exp P(s)}$$
(6.3.6)

where s is the distance to the EFB, and

$$P(s) = C_0 + C_1 \left(\frac{s}{\lambda}\right) + C_2 \left(\frac{s}{\lambda}\right)^2 + C_3 \left(\frac{s}{\lambda}\right)^3 + C_4 \left(\frac{s}{\lambda}\right)^4 + C_5 \left(\frac{s}{\lambda}\right)^5$$
(6.3.7)

The values of the coefficients C_0 to C_5 should be such that the derivatives of B_Z with respect to s be negligible at a distance s of a few λ from the EFB, so to allow a safe extrapolation of \vec{B} out of the median plane.

It is also possible to simulate a shift of the EFB, by giving a non zero value to the parameter *shift*. s is then changed to s-*shift* in the previous equation. This allows small variations of the total magnetic length.

Let F_E (respectively F_S , F_L) be the fringe field coefficient attached to the entrance (respectively exit, lateral) EFB following the equations above. At any node of the map mesh, the resulting value of the fringe field coefficient (eq. 6.3.1) is (Fig. 11)

$$\mathcal{F}(R,\theta) = F_E * F_S * F_L$$

In particular, $F_L \equiv 1$ if no lateral EFB is requested.

The Mesh of the Field Map

The magnetic field is calculated at the nodes of a mesh with polar coordinates, in the median plane. The radial step is given by

$$\delta R = \frac{RMAX - RMIN}{IRMAX - 1}$$

and the angular step by

$$\delta\theta = \frac{AT}{IAMAX - 1}$$

where, *RMIN* and *RMAX* are the lower and upper radial limits of the field map, and *AT* is its total angular aperture (Fig. 9B). *IRMAX* and *IAMAX* are the total number of nodes in the radial and angular directions.

Simulating Field Defects and Shims

Once the initial map is calculated, it is possible to perturb it by means of the parameter *NBS*, so as to simulate field defects or shims.

If NBS = -2, the map is globally modified by a perturbation proportional to $R - R_0$, where R_0 is an arbitrary radius, with an amplitude $\Delta B_Z/B_0$, so that B_Z at the nodes of the mesh is replaced by

$$B_Z * \left(1 + \frac{\Delta B_Z}{B_0} \frac{R - R_0}{RMAX - RMIN} \right)$$

If NBS = -1, the perturbation is proportional to $\theta - \theta_0$, and B_Z is replaced by

$$B_Z * \left(1 + \frac{\Delta B_Z}{B_0} \frac{\theta - \theta_0}{AT} \right)$$



Figure 10: Second order type fringe field (upper plot) and exponential type fringe field (lower plot).



Figure 11: Effective value of $\mathcal{F}(R,\theta)$ for overlapping fringe fields F_1 and F_2 centered at O_1 and O_2 .
If NBS \geq 1, then NBS shims are introduced at positions $\frac{R_1 + R_2}{2}$, $\frac{\theta_1 + \theta_2}{2}$ (Fig. 12) [47] The initial field map is modified by shims with second order profiles given by

$$\theta = \left(\gamma + \frac{\alpha}{\mu}\right) \,\beta \, \frac{X^2}{\rho^2}$$

where X is shown in Fig. 12, $\rho = \frac{R_1 + R_2}{2}$ is the central radius, α and γ are the angular limits of the shim, β and μ are parameters.

At each shim, the value of B_Z at any node of the initial map is replaced by

$$B_Z * \left(1 + F\theta * FR * \frac{\Delta B_Z}{B_0} \right)$$

where $F\theta = 0$ or FR = 0 outside the shim, and $F\theta = 1$ and FR = 1 inside.

Extrapolation Off Median Plane

The vertical field \vec{B} and its derivatives in the median plane are calculated by means of a second or fourth order polynomial interpolation, depending on the value of the parameter *IORDRE* (*IORDRE*=2, 25 or 4, see section 1.4.2). The transformation from polar to Cartesian coordinates is performed following eqs. (1.4.9 or 1.4.10). Extrapolation off median plane is then performed by means of Taylor expansions following the procedure described in section 1.3.3.



Figure 12: A second order profile shim. The shim is centered at $\frac{(R_1 + R_2)}{2}$ and $\frac{(\theta_1 + \theta_2)}{2}$.

AUTOREF : Transport beam into a new reference frame

AUTOREF positions the new reference frame following four different options (apart from I = 0 which is just an "off" switch) :

If I = 1, AUTOREF is equivalent to

$$CHANGREF[XCE = 0, YCE = Y(1), ALE = T(1)]$$

so that the new reference frame is at the exit of the last element, with particle 1 at the origin with its horizontal angle set to T = 0.

If I = 2, it is equivalent to

CHANGREF[XW, YW, T(1)]

so that the new reference frame is at the position (XW, YW) of the waist (calculated automatically in the same way as for *IMAGE*) of the three rays number 1, 4 and 5 (compatible for instance with *OBJET*, *KOBJ* = 5, 6, together with the use of *MATRIX*) while T(1), the horizontal angle of particle number *I*1, is set to zero.

If I = 3, it is equivalent to

CHANGREF[XW, YW, T(I1)]

so that the new reference frame is at the position (XW, YW) of the waist (calculated automatically in the same way as for *IMAGE*) of the three rays number I1, I2 and I3 specified as data, while T(I1) is set to zero.

If I = 4: new horizontal beam centroid positionning *XCE*, *YCE*, *ALE* is provided. The beam is moved by *XCE* and then centered on *YCE*, *ALE*.

If I = 4.1: new beam centroid positionning *XCE*, *YCE*, *ALE*, *DCE*, *TIME* is provided. The beam is moved by *XCE* and then centered on *YCE*, *ALE*. In addition, the beam is centered on a new relative momentum *DCE* and new timing value *TIME*.

If I = 4.2: same as 4.1, except that particles all have their timing set to *TIME*.

If I = 5: new vertical beam centroid positionning *ZCE*, *PLE* (position, angle) is provided. The beam is centered on vertical position and angle *ZCE*, *PLE*.

BEAMBEAM : Beam-beam lens

BEAMBEAM is a beam-beam lens simulation, a thin-lens transform [48], in the weak-strong approximation.

Upon option using SPNTRK, BEAMBEAM will include spin kicks, after modelling as described in Ref. [49].

For software developers

<code>rbb.f</code> reads the data from zgoubi.dat; <code>bb.f</code> and programs therein do the beam (and spin when requested) dynamics.

BEND : Bending magnet, Cartesian frame

BEND is one of several keywords available for the simulation of dipole magnets. It presents the interest of easy handling, and is well adapted for the simulation of synchrotron dipoles and such other regular dipoles as sector magnets with wedge angles.

The field in *BEND* is defined in a Cartesian coordinate frame (unlike for instance *DIPOLE[S]* that uses a polar frame). As a consequence, having particle coordinates at entrance or exit of the magnet referring to the curved main direction of motion may require using *KPOS*, in particular *KPOS=3* (in a circular accelerator cell for instance, see section 7.9, p. 208).

The dipole simulation accounts for the magnet geometrical length XL, for a possible skew angle (X-rotation, useful for obtaining vertical deviation magnet), and for the field B1 such that in absence of fringe field the deviation θ satisfies $XL = 2 \frac{BORO}{B1} \sin \frac{\theta}{2}$.

Then follows the description of the entrance and exit EFBs and fringe fields. The wedge angles W_E (entrance) and W_S (exit) are defined with respect to the sector angle, with the signs as described in Fig. 13. Within a distance $\pm X_E(\pm X_S)$ on both sides of the entrance (exit) EFB, the fringe field model is used (same as for *QUADRUPO*, Fig. 36, p. 134); elsewhere, the field is supposed to be uniform.

If λ_E (resp. λ_S) is zero sharp edge field model is assumed at entrance (resp. exit) of the magnet and X_E (resp. X_S) is forced to zero. In this case, the wedge angle vertical first order focusing effect (if $\vec{B}1$ is non zero) is simulated at magnet entrance and exit by a kick $P_2 = P_1 - Z_1 \tan(\epsilon/\rho)$ applied to each particle (P_1 , P_2 are the vertical angles upstream and downstream the EFB, Z_1 the vertical particle position at the EFB, ρ the local horizontal bending radius and ϵ the wedge angle experienced by the particle ; ϵ depends on the horizontal angle T).

Magnet (mis-)alignment is assured by *KPOS*. *KPOS* also allows some degrees of automatic alignment useful for periodic structures (section 7.9).



Figure 13: Geometry and parameters of BEND: XL = length, θ = deviation, W_E , W_S are the entrance and exit wedge angles. The motion is computed in the Cartesian frame (O, X, Y, Z).

• MAD style 'BEND' definition :

L = 1.A = 0.1

From matrice-style code modeling, to zgoubi : Fig. 14 illustrates the conversion of matrix method style of data where the magnet is defined by its length and deviation angle (see MAD input below, using 'SBEND'), to **zgoubi** input data using *BEND* (in this particular case of an illustration of a rectangular magnet, *MUL-TIPOL* could be used, as well).



Figure 14: Simulating a matrix method style of rectangular magnet (*e.g.*, MAD's 'SBEND') by means of *BEND*, in three different ways, see text. In case (a), the straight length in **zgoubi**'s *BEND* is $L' = \rho \sin(A)$, whereas in cases (b, c) it is $L = 2\rho \sin(A/2)$.

• zgoubi, case (b) or (c) using KPOS=1 or 3 :

(b) A/2 Z-rotated BEND followed by A/2 Z-rotation of frame

```
Larc = L \star (A/2.) / sin(A/2.)
                                                               'CHANGREF'
                                                              ZR -2.86478897565
e1 = 0.
                                                               'BEND'
e2 = A
B: SBEND, L=Larc, ANGLE=A, e1 = e1, e2 = e2
                                                              100. 0.
                                                                      1.
                                                              0. 0. 0.
                                                                               ! e1=0
                                                              0 0. 0. 0. 0. 0. 0.
• zgoubi, case (a) :
                                                              0. 0. 0.1
                                                                               ! e2=A
                                                              0 0. 0. 0. 0. 0. 0.
(a) YS=-rho*(1-cos(A)) translated, non-rotated BEND,
                                                              .1
   followed by A Z-rotation of frame
                                                              1 0. 0.
                                                               'CHANGREF'
 'CHANGREF
                                                              ZR
                                                                 -2.86478897565
YS -4.997916927068
 'BEND'
1
99.8750260394 0.
                                                              (c) same as (b), using KPOS=3 instead
0. 0. 0.05
                   ! e1=A/2
0 0. 0. 0. 0. 0. 0.
                                                               'BEND'
0. 0. 0.05
                   ! e2=A/2
                                                              1
0 0. 0. 0. 0. 0. 0.
                                                              100. 0.
                                                                       1.
.1
                                                                               ! e1=0
1 0. 0. 0.
                                                              0. 0. 0.
                                                              0 0. 0. 0. 0. 0. 0.
'CHANGREF'
                                                              0. 0. 0.1
ZB -5.72957795131
                                                                                ! e2=A
                                                              0 0. 0. 0. 0. 0. 0.
                                                              .1
3 0. 0. -0.05
```

Negative bend, vertical bend, tricks : Use *YMY* for the former, *TRAROT* with a $\pm \pi$ X-rotation for the latter. The two can be combined, so that a vertical negative bend can be represented by the sequence *TRAROT*[π], *YMY*, *BEND*[B>0], *YMY*, *TRAROT*[$-\pi$], with positionning methods for *BEND* as discussed above (Fig. 14) still applying.

BETATRON : Betatron core (momentum kick)

BETATRON simulates a betatron yoke, for instance for slow extraction. It just imparts the particle a momentum kick, normally small.

BREVOL : 1-D uniform mesh magnetic field map

1

BREVOL reads a 1-D axial field map from a storage data file, whose content must match the following FORTRAN reading sequence (possible FORMAT updates are to be found in fmapw.f).

```
OPEN (UNIT = NL, FILE = FNAME, STATUS = 'OLD' [,FORM='UNFORMATTED'])
DO 1 I = 1, IX
IF (BINARY) THEN
READ(NL) X(I), BX(I)
ELSE
READ(NL,*) X(I), BX(I)
ENDIF
CONTINUE
```

where IX is the number of nodes along the (symmetry) X-axis, X(I) their coordinates, and BX(I) are the values of the X component of the field. BX is normalized with BNORM factor prior to ray-tracing, as well X is normalized with the coefficient XNORM (useful to convert to centimeters, the working units in **zgoubi**). For binary files, FNAME must begin with 'B₋' or 'b₋', a flag 'BINARY' will thus be set to '.TRUE.' by the FORTRAN.

X-cylindrical symmetry is assumed, resulting in BY and BZ taken to be zero on axis. $\vec{B}(X, Y, Z)$ and its derivatives along a particle trajectory are calculated by means of a 5-point polynomial interpolation followed by second order off-axis extrapolation (see sections 1.3.2, 1.4.1).

Entrance and/or exit integration boundaries may be defined in the same way as in *CARTEMES* by means of the flag *ID* and coefficients *A*, *B*, *C*, etc.

CARTEMES : 2-D Cartesian uniform mesh magnetic field map

CARTEMES was originally dedicated to the reading and processing of the measured median plane field maps of the QDD spectrometer SPES2 at Saclay, assuming mid-plane dipole symmetry. However, it can be used for the reading of any 2-D median plane maps, provided that the format of the field data storage file fits the following *FORTRAN* sequence

where, IX and JY are the number of longitudinal and transverse horizontal nodes of the uniform mesh, and X(I), Y(J) their coordinates. *FNAME* is the name of the file containing the field data. For binary files, *FNAME* must begin with 'B₋' or 'b₋', a flag 'BINARY' will thus be set to '.TRUE.' by the *FORTRAN*.

The measured field BMES is normalized with BNORM,

$$B(I, J) = BMES(I, J) \times BNORM$$

As well the longitudinal coordinate X is normalized with a *XNORM* coefficient (useful to convert to centimeters, the working units in **zgoubi**).

The vector field, \vec{B} , and its derivatives out of the median plane are calculated by means of a second or fourth order polynomial interpolation, depending on the value of the parameter *IORDRE* (*IORDRE* = 2, 25 or 4, see section 1.4.2).

In case a particle exits the mesh, its *IEX* flag is set to -1 (see section 7.12, p. 211), however it is still tracked with the field being *extrapolated* from the closest nodes of the mesh. Note that such extrapolation process may induce erratic behavior if the distance from the mesh gets too large.

Entrance and/or exit integration boundaries (so-called "droite de coupure" in the code) can be defined with the flag ID, as follows (Fig. 15).

If ID = 1: the integration in the field is terminated on a boundary with equation A'X + B'Y + C' = 0, and then the trajectories are extrapolated linearly onto the exit border of the map.

If ID = -1: an entrance boundary is defined, with equation A'X + B'Y + C' = 0, up to which trajectories are first extrapolated linearly from the map entrance border, prior to being integrated in the field.

If $ID \ge 2$: one entrance boundary, and ID-1 exit boundaries are defined, as above. The integration in the field terminates on the last (ID-1) exit boundary. No extrapolation onto the map exit border is performed in this case.



Figure 15: OXY is the coordinate system of the mesh. Integration boundaries may be defined, using $ID \neq 0$: particle coordinates are extrapolated linearly from the entrance face of the map, onto the boundary A'X + B'Y + C' = 0; after ray-tracing inside the map and terminating on the boundary AX + BY + C = 0, coordinates are extrapolated linearly onto the exit face of the map if ID = 2, or terminated on the last (ID - 1)boundary if ID > 2.

CAVITE : Accelerating cavity

CAVITE provides a simulation of a (zero length) accelerating cavity ; it can be used in conjunction with keywords *REBELOTE* and *SCALING* for the simulation of multi-turn tracking with synchrotron or fixed field (FFAG, cyclotron) acceleration (see section 7.11). It can also be used to simulate recirculating linacs and energy-recovery linacs. *CAVITE* must be preceded by *PARTICUL* for the definition of mass M and charge q.

A major effect of CAVITE on optics settings is the following :

The reference rigidity $B\rho_{ref}$ in **zgoubi**, as used for instance when determining optical strengths from field values (see sections 1.2.1-1.2.3), is defined when creating the object by means of *[MC]OBJET*. However, in many cases - options as described below - that reference rigidity will be updated upon crossing a cavity, consistently with the amount of synchronous rigidity increase as induced by the energy change, namely,

$$B\rho_{ref} = BORO \longrightarrow B\rho_{ref} = BORO + \delta B\rho_s \tag{6.3.8}$$

Note as an illustration of the process, that, in this case, a simple way to have the optical elements have their *strengths* maintained constant is to use *SCALING* with the option NTIM = -1.

- If IOPT = 0 : CAVITE is switched off.
- If IOPT = 1 : CAVITE simulates the RF cavity of a synchrotron accelerator : the periodic motion over IP = 1, NPASS + 1 turns (passes through the optical sequence) is obtained using the keyword REBELOTE, option K = 99, while RF and optical elements time dependent functions are simulated by means of SCALING – see section 7.11. CAVITE may conveniently be located at the end of the optical sequence, otherwise its phasing has to be provided. The synchrotron motion of any of the IMAX particles of a beam is obtained from the following mapping

$$\begin{cases} \phi_2 - \phi_1 = 2\pi f_{RF} \left(\frac{\ell}{\beta c} - \frac{\mathcal{L}}{\beta_s c} \right) \\ W_2 - W_1 = q\hat{V} \sin \phi_1 \end{cases}$$

where

- ϕ = RF phase ; $\phi_2 \phi_1$ = variation of ϕ between two traversals
- \hat{V} = peak RF voltage
- W = kinetic energy; $W_2 W_1 =$ energy gain at a traversal of CAVITE
- L = length of the synchronous closed orbit (to be calculated by prior ray-tracing, see 'CLOSED ORBIT COMPUTATION' below)
- $\beta_s c$ = velocity associated with the synchronous energy
- ℓ = particle trajectory length between two traversals
- βc = particle velocity
- c = velocity of light.

The RF frequency f_{RF} is a multiple of the synchronous revolution frequency, and is obtained from the input data, following

$$f_{RF} = \frac{hc}{\mathcal{L}} \frac{q(B\rho)_s}{\sqrt{q^2(B\rho)_s^2 + (Mc)^2}}$$

where $\begin{array}{l} h & = \text{harmonic number of the R.F} \\ B \rho_s & = \text{rigidity associated with the synchronous energy} \end{array}$

The synchronous rigidity $(B\rho)_s$ is obtained from the timing law specified by means of SCALING following $(B\rho)_s = BORO \cdot SCALE(TIMING)$ (see SCALING for the meaning and calculation of the scale factor SCALE(TIMING)). If SCALING is not used, $(B\rho)_s$ is assumed to keep the constant value BORO as given in the object description (see OBJET for instance).

The velocity βc of a particle is calculated from its current rigidity

$$\beta = \frac{q(B\rho)}{\sqrt{q^2(B\rho)^2 + (Mc)^2}}$$

The velocity $\beta_s c$ of the synchronous particle is obtained in the same way from

$$\beta_s = \frac{q(B\rho)_s}{\sqrt{q^2(B\rho)_s^2 + (Mc)^2}}$$

The kinetic energies and rigidities involved in these formulae are related by

$$q(B\rho) = \sqrt{W(W + 2Mc^2)}$$

Finally, the initial conditions for the mapping, at the first turn, are the following

- For the (virtual) synchronous particle

$$\phi_1 = \phi_s = \text{synchronous phase}$$

 $(B\rho)_{1s} = BORO$

- For any of the I = 1, *IMAX* particles of the beam

$$\phi_{1I} = \phi_s = \text{synchronous phase}$$

 $(B_{\rho})_{1I} = BORO * D_I$

where the quantities **BORO** and D_I are given in the object description.

Calculation of the Coordinates

Let $p_I = [p_{XI}^2 + p_{YI}^2 + p_{ZI}^2]^{1/2}$ be the momentum of particle *I* at the exit of the cavity, while $p_{I_0} = [p_{XI_0}^2 + p_{YI_0}^2 + p_{ZI_0}^2]^{1/2}$ is its momentum at the entrance. The kick in momentum is assumed to be fully longitudinal, resulting in the following relations between the coordinates at the entrance (denoted by the index zero) and at the exit

$$p_{XI} = \left[p_I^2 - (p_{I_0}^2 - p_{XI_0}^2) \right]^{1/2}$$

$$p_{YI} = p_{YI_0}, \text{ and } p_{ZI} = p_{ZI_0} \text{ (longitudinal kick)}$$

$$X_I = X_{I_0}, \quad Y_I = Y_{I_0} \text{ and } Z_I = Z_{I_0} \text{ (zero length cavity)}$$

and for the angles (see Fig. 1)

$$T_{I} = \operatorname{Atg}\left(\frac{p_{YI}}{p_{XI}}\right)$$

$$P_{I} = \operatorname{Atg}\left(\frac{P_{ZI}}{(p_{XI}^{2} + p_{YI}^{2})^{1/2}}\right)$$
(damping of the transverse motion)

• If IOPT = 2: the same simulation of a synchrotron RF cavity as for IOPT = 1 is performed, except that the keyword *SCALING* (family *CAVITE*) is not taken into account in this option : the increase in kinetic energy at each traversal, for the synchronous particle, is

$$\Delta W_s = q\hat{V}\,\sin\phi_s$$

where the synchronous phase ϕ_s is part of the input data to *CAVITE*. From this, the calculation of the law $(B\rho)_s$ and the RF frequency f_{RF} follows, according to the formulae given in the *IOPT* = 1 case.

IOPT = 2 can be used for SR loss compensation in *storage ring* mode. (use IOPT=11 for accelerated mode). SR loss is switched on by means of the keyword SRLOSS/KSR=1. In that case \hat{V} and ϕ_s should be given the appropriate value for compensation of SR induced energy loss ($\hat{V} \times \sin \phi_s$ should be equal to the enrgy loss). The same functionning (stationary bucket with SR loss) can be ontained using IOPT=11, which further allows acceleration in the presence of SR energy loss.

IOPT = 2 handles double RF systems. Respective harmonic value and voltage amplitudes are h_1 , h_2 and V_1 , V_2 . It follows CERN ISR-TH-RF/80-26 [50]. In particular, the stable phase ϕ_n of the higher harmonic voltage is taken to be

$$\phi_{\rm n} = \operatorname{atan}(\operatorname{tan}(\phi_{\rm s})/{\rm n})/{\rm n}$$

wherein $n = h_2/h_1$. The synchronous energy gain is

$$\Delta W_s = q\hat{V}\left(\sin(\phi_s) + k\sin(n\phi_n)\right)$$

with $k = V_2/V_1$.

The option IOPT = 2 handles synchrotron radiation energy loss in the case of stationary bucket (see IOPT = 11 for accelerating bucket). Compensation is derived from the synchronous phase ϕ_s , via $\Delta W_{SR} = q\hat{V} \sin \phi_s$, therefore assuming appropriate value

$$\phi_s = \operatorname{asin}(\Delta W_{SR}/q\hat{V})$$

with ΔW_{SR} = the energy loss between passes in the cavity.

• If IOPT = 3 : sine RF law, acceleration without synchrotron motion. Any particle will be given a kick

$$\Delta W = q\hat{V}\,\sin\phi_s$$

where \hat{V} and ϕ_s are input data.

The option IOPT = 3 handles synchrotron radiation energy loss in the case of stationary bucket (as in IOPT = 2).

- If IOPT = 4: to be documented.
- If IOPT = 5: to be documented.
- If IOPT = 6 : allows reading the RF frequency and/or phase law from an external file (wih name normally "zgoubi.freqLaw.In"). See routines cavite.f and scalin.f for details. Was first used for acceleration in scaling FFAG [58].
- If IOPT = 7 : fixed frequency RF, quasi- or isochronous acceleration. Was first used for quasi-isochronous, fixed frequency acceleration in the EMMA prototype linear FFAG [59, 60].
 IOPT = 7 can be used for cyclotron acceleration.
- If IOPT = 8: to be documented.
- If IOPT = 9: to be documented.

• If IOPT = 10: fixed frequency RF. Was first installed/used for CEBAF and eRHIC ERL simulations.

A "*Facility*=CEBAF" flag allows some specifities regarding the management of reference phase and individual particle phase in the case of CEBAF cavities, which includes the following:

- the RF crest voltage is at $\phi_s = \pi/2$ (otherwise, it is at $\phi_s = 0$),
- the RF pahse of any particle is offset by an amount equal to the phase of the bunch centroid.

It is equivalent to set "CEBAF", or to set both "SHIFT_PHO" (with RF in this case $\phi_s = 0$ instead) and "CENTROID" (see below). If "CEBAF" is set, then if overrides the previous two, whatever their state.

Two additionl flags are available with

- "SHIFT_PH0": this causes an offset of particle phases, by $\pi/2$ (it would be equivalent to offset ϕ_s datum, instead),
- "CENTROID": this causes the RF pahse of any particle to be offset by an amount equal to the phase of the bunch centroid. The bunch centroid is computed as an average over the *IMAX* particles launched by *[MC]OBJET*.

A Chambers matrix method is used to get the transverse focusing effect. Particles undergo a longitudinal boost in energy

$$\Delta W = q\hat{V}\,\cos(2\pi f_{RF}t + \phi_s)$$

with t the arrival time at the center of the cavity. The phase datum ϕ_s in this option has two roles, (i) that played in the equation above, (ii) determining the updating of **zgoubi**'s reference rigidity, namely,

$$B\rho_{ref} = BORO \to B\rho_{ref} = BORO + \delta B\rho_s \quad \text{with} \quad \delta B\rho_s = \frac{\Delta(\beta_s(W_s + M))}{qc}, \quad \Delta W_s = q\hat{V}\cos(\phi_s) \tag{6.3.9}$$

The cavity length L as specified in the input data is also used to update the path length of the particles (linearly). An optional 'IOP' flag allows small ΔW approximation of Chambers matrices, as well as removing the longitudinal damping (thus geometrical emittance is conserved), as follows :

- IOP = 0: Default value ; the transverse matrix is that of a drift with length L.
- IOP = 1 : Chambers matrix with $\Delta W/W$ approximation, namely, for both planes,

$$\begin{pmatrix} x \\ x' \end{pmatrix}_{out} = \begin{pmatrix} \sqrt{(W_i/W_o)} & L_{cav} \times \sqrt{(W_i/W_o)} \\ 0. & \sqrt{(W_i/W_o)} \end{pmatrix} \begin{pmatrix} x \\ x' \end{pmatrix}_{in}$$
(6.3.10)

with W_i , W_o respectively the incoming and outgoing kinetic energies.

- IOP = -1 : Same as 1, with matrix in both planes re-normalized to determinant=1 (*i.e.*, $R_{ij} \rightarrow R_{ij}/\sqrt{R_{11}R_{12}-R_{21}R_{22}}$),
- IOP = 2 : Chambers matrix without approximation on $\Delta W/W$, namely, for both planes,

$$\begin{pmatrix} x \\ x' \end{pmatrix}_{out} = \begin{pmatrix} \cos(u) - \sqrt{2}\sin(u)\cos(\phi) & vW_i\sin(u)\cos(\phi) \\ -\frac{\sin(u)}{vW_o}(2\cos(\phi) + \frac{1}{\cos(\phi)}) & \frac{W_i}{W_o}(\cos(u) + \sqrt{2}\sin(u)\cos(\phi)) \end{pmatrix} \begin{pmatrix} x \\ x' \end{pmatrix}_{in}$$
(6.3.11)

with $u = \log(W_o/W_i)/(\sqrt{8}\cos(\phi))$, $v = \sqrt{8}L/(W_o - W_i)$, ϕ the particle phase at the cavity.

- IOP = -2: Same as 2, with matrix in both planes re-normalized to determinant=1.
- If IOPT = 11: under development.

The same simulation of a synchrotron RF cavity as for IOPT = 2 is performed, IOPT = 11 handles synchrotron radiation energy loss as well, yet both stationnary or accelerated bucket.

In the 'CornellSynch' option, the R.F. peak voltage input data is not used, the voltage is hard-coded (in cavite.f), - the acceleration voltage applied is [86]

$$V(t) = 4.4 \sin(2\pi ft) + 8.8 \sin^8(2\pi ft/2), \quad f = 60 \text{ Hz}$$

CAVITE in this option accounts for the Synchrotron radiation energy loss, U_0 , to be recovered at this CAVITE; in particular if only one cavity is used, then U_0 is the energy loss per turn. U_0 adds to the peak voltage (unless 'CornellSynch' is pecified), namely, the actual RF peak voltage voltage follows the evolution of U_0 to provide

$$\hat{V}_{\text{effective}} = \hat{V} + U_0$$

The initial value of the energy to be recovered needs be specified, U_{00} , it is then updated at the subsequent passes using

$$U_0 = U_{00} \left(\frac{E}{E_1}\right)^4$$

with E the current energy, and E_1 the energy at the first pass. If U_{00} is left null whereas the keyword SRLOSS (pp. 185, 327) is set for energy loss (*KSR=1*), then U_{00} is set, at the first pass, in a hard-coded way, using the curvature radius and assuming an iso-field lattice, namely

$$U_0 = 88.46276 \times E_{[MeV]}^4 / \rho_{[m]}$$

This is done in cavite.f, at the moment this setting takes $\rho = 235$ m (case of the US EIC RCS electron injector in RHIC tunnel), this can be changed and the Fortran recompiled.

Positionning of *CAVITE*: knowledge of cavity location azimuth along the actual closed orbit (which may not be null, in the presence of orbit defects for instance) is necessary if the cavity is not located at an end of the periodic optical sequence. In that case a prior run, possibly using *FIT* to find the closed orbit (see Sec. 7.3), will deliver that azimuth.

CLOSED ORBIT COMPUTATION

Due to possible dipole type of optical defects (*e.g.*, fringe fields, straight axis combined function dipoles), the closed orbit may not coincide with the ideal axis of the optical elements and will instead be almost everywhere non-zero (see also Sec. 7.3, p. 206).

One method in order to get the closed orbit at the beginning of the optical sequence (*i.e.*, where the initial particle coordinates or spin coordinates are defined) consists in using the FIT[2] procedure. Use in this case the "3.1" (orbit) or "10.1" (spin) periodicity constraints.

Another method consists in ray-tracing a single particle over a sufficiently large number of turns, starting with initial conditions taken near the reference orbit, so as to obtain statistically well-defined transverse phase-space ellipses. The local closed orbit coincides with the coordinates Y_c , T_c , Z_c , P_c of the center of the ellipses. A few iterations are usually sufficient (avoid near-integer tunes) to ensure accuracy. Next, ray-tracing over one turn a particle starting with the initial condition (Y_c , T_c , Z_c , P_c) will provide the closed orbit along the all optical sequence, and as a sub-product its length \mathcal{L} (the F(6, 1) coordinate in the source FORTRAN).

RECOVERING FROM A CRASH

When accelerating a bunch in a pulsed ring, *SCALING* is used to ramp magnetic fields, so following the rigidity increase by *CAVITE*. *CAVITE* may or may not be part of the *SCALING* argument list, this is discussed in the *SCALING* section, page 181. Now, if the job is stopped - due to computer crash or else - it is possible to resume the tracking from the latest records (in [b_]zboubi.fai storage file), using *OBJET*, *KOBJ*= 3. In the presence of acceleration using *CAVITE*, since there is no reference particle in **zgoubi**, *CAVITE* will read from [b_]zboubi.fai the reference rigidity at the corresponding time/turn when tracking crashed/resumes. See the *SCALING* section for more (page 178) and the examples there, as well as the example page 299.

PRINT : The optional command 'PRINT', following the first argument, '*IOPT*', in *CAVITE* keyword, will cause logging of computational data (synchronous time and momentum, RF phase, and much more) in the file zgoubi.CAVITE.Out.

For software developers

Cavity simulations are done in cavite.f. Management of the reference rigidity $B\rho_{ref}$ is ensured for part in cavite.f, and for part in routines associated with 'SCALING', essentially scaler.f.

CHAMBR : Long transverse aperture limitation

CHAMBR causes the identification, counting and stopping of particles that reach the transverse limits of the vacuum chamber. The chamber can be either rectangular (*IFORM* = 1) or elliptic (*IFORM* = 2). The chamber is centered at *YC*, *ZC* and has transverse dimensions $\pm YL$ and $\pm ZL$ such that any particle will be stopped if its coordinates *Y*, *Z* satisfy

$$(Y - YC)^2 \ge YL^2 \text{ or } (Z - ZC)^2 \ge ZL^2 \text{ if } IFORM = 1$$

 $\frac{(Y - YC)^2}{YL^2} + \frac{(Z - ZC)^2}{ZL^2} \ge 1 \text{ if } IFORM = 2$

The conditions introduced with CHAMBR are valid along the optical sequence until the next occurrence of the keyword CHAMBR. Then, if IL = 1 the aperture is possibly modified by introducing new values of YC, ZC, YL and ZL, or, if IL = 2 the chamber ends and information is printed concerning those particles that have been stopped.

The testing is done in optical elements at each integration step, between the *EFB*s. For instance, in *QUADRUPO* there will be no testing from $-X_E$ to 0 and from *XL* to $XL + X_S$, but only from 0 to *XL*; in *DIPOLE*, there is no testing as long as the *ENTRANCE EFB* is not reached, and testing is stopped as soon as the *EXIT* or *LATERAL EFB*s are passed.

In optical elements defined in polar coordinates, Y stands for the radial coordinate (*e.g.*, *DIPOLE*, see Figs. 3C, p. 31, and 20, p. 96). Thus, centering *CHAMBR* at

YC = RM simulates a chamber curved with radius RM, and having a radial acceptance $RM \pm YL$. In *DRIFT*, the testing is done at the beginning and at the end, and only for positive drifts. There is no testing in *CHANGREF*.

When a particle is stopped, its index *IEX* (see *OBJET* and section 7.12) is set to the value -4, and its actual path length is stored in the array *SORT* for possible further use.

CHANGREF : Transformation to a new reference frame

CHANGREF transports particles from a reference plane (O, Y, Z) at path distance S, to a new one by a combination of translations and/or rotations. It essentially aims at positioning optical elements with respect to one another, as setting a reference frame at the entrance or exit of field maps, or to simulate misalignments (see also KPOS option). CHANGREF can be placed at any location in an optical sequence.

Spin tracking, particle decay and gas-scattering are taken into account in CHANGREF. Energy loss by synchrotron radiation (SRLOSS keyword) is not.

There are two "styles" of CHANGREF, as follows.

The "old style" CHANGREF requires the three data XCE, YCE, ALE and then gets the new particle coordinates Y_2 , T_2 , Z_2 , P_2 and path length S_2 from the old ones Y_1 , T_1 , Z_1 , P_1 and S_1 using

$$T_{2} = T_{1} - ALE$$

$$Y_{2} = \frac{(Y_{1} - YCE)\cos T_{1} + XCE\sin T_{1}}{\cos T_{2}}$$

$$DL^{2} = (XCE - Y_{2}\sin ALE)^{2} + (YCE - Y_{1} + Y_{2}\cos ALE)^{2}$$

$$Z_{2} = Z_{1} + DLtgP_{1}$$

$$S_{2} = S_{1} + \frac{DL}{\cos P_{1}}$$

$$P_{2} = P_{1}$$

Figure 16: Scheme of the CHANGREF procedure.

where, XCE and YCE are shifts in the horizontal plane along, respectively, X- and Y-axis, and ALE is a rotation around the Z-axis. DL is given the sign of $XCE - Y_2 \sin(ALE)$.

EXAMPLE - The example below illustrates the use of CHANGREF. This is a case of symmetric positioning of a combined function dipole+quadrupole magnet in a drift-bend-drift geometry with 12.691 degrees deviation (obtained upon combined effect of a dipole component and of quadrupole axis shifted 1 cm off optical axis).



Zgoubi data file :

```
Using CHANGREF, "Old style"
'OBJET'
51.71103865921708
                         ! Electron, Ekin=15MeV.
2
                          ! One particle, with
1 1
2. 0. 0.0 0.0 0.0 1. 'R' ! Y_0=2 cm.
1 1 1 1 1 1 1
                   .plt ! Print into zgoubi.plt.
'MARKER'
           BEG
'DRIFT'
                         ! 10 cm drift.
10.
'CHANGREF'
0. 0. -6.34165
                         ! 1/ half Z-rotation.
'CHANGREF'
                         ! 2/ Y-shift.
0.1.0.
            ! Combined function dipole + quadrupole.
'MULTIPOL'
                          ! Print into zgoubi.plt.
  2
5 10. 2.064995867082342 2. 0. 0. 0. 0. 0. 0. 0. 0. 0.
0 0 5. 1.1 1.00 1.00 1.00 1.00 1.00 1. 1. 1. 1.
4 .1455 2.2670 -.6395 1.1558 0.0.
0 0 5. 1.1 1.00 1.00 1.00 1.00 1.00 1. 1. 1. 1.
4 .1455 2.2670 -.6395 1.1558 0.0.
0 0 0 0 0 0 0 0 0 0
.1
   step size
1 0. 0. 0.
'CHANGREF'
0. -1. -6.34165! 1/ Y-shift, 2/ nall 2-rocace.'DRIFT' - .plt! 10 cm drift. Print into zgoubi.plt.
'FAISCEAU'
'END'
```



Note : The square markers scheme the stepwise integration in case of ± 5 cm additional fringe field extent upstream and downstream of the 5 cm long multipole.

The "new style" *CHANGREF* allows all 6 degrees of freedom rather than just 3, namely, X-, Y-, Z-shift, X-, Y-, Z-rotation. In addition, *CHANGREF* "new style" allows up to 9 successive such elementary transformations, in arbitrary order. The "old style" example above is transposed into "new style", hereafter.

Zgoubi data file :

```
Using CHANGREF, "New Style"
'OBJET'
51.71103865921708
                       ! Electron, Ekin=15MeV.
2
                         ! One particle, with
1 1
2. 0. 0.0 0.0 0.0 1. 'R' ! Y_0=2 cm.
1 1 1 1 1 1 1
'MARKER'
         BEG
                 .plt ! Print into zgoubi.plt.
'DRIFT'
                         ! 10 cm drift.
10.
'CHANGREF'
                       ! 1/ half Z-rotate, 2/ Y-shift.
ZR -6.34165 YS 1.
'MULTIPOL' ! Combined function dipole + quadrupole.
  2
                        ! Print into zgoubi.plt.
5 10. 2.064995867082342 2. 0. 0. 0. 0. 0. 0. 0. 0.
0 0 5. 1.1 1.00 1.00 1.00 1.00 1.00 1. 1. 1. 1.
4 .1455
         2.2670 -.6395 1.1558 0. 0.
0 0 5. 1.1 1.00 1.00 1.00 1.00 1.00 1. 1. 1. 1.
4 .1455 2.2670 -.6395 1.1558 0.0.
0 0 0 0 0 0 0 0 0 0
.1 step size
1 0. 0. 0.
'CHANGREF'
                        ! 1/ Y-shift, 2/ half Z-rotate.
YS -1. ZR -6.34165
'DRIFT'
                       ! 10 cm drift. Print into zgoubi.plt.
          - .plt
10.
'FAISCEAU'
'END'
```

SCALING can be used to scale positionning parameters in CHANGREF.

CIBLE or TARGET : Generate a secondary beam following target interaction

The reaction is $1 + 2 \longrightarrow 3 + 4$ with the following parameters

Laboratory momentum	$p_1 \equiv 0$	p_2	p_3	p_4
Rest mass	M_1	M_2	M_3	M_4
Total energy in laboratory	$M_1 c^2$	W_2	W_3	W_4

The geometry of the interaction is shown in Fig. 17.

The angular sampling at the exit of the target consists of the NT coordinates $0, \pm TS, \pm 2 * TS... \pm (NT - 1) * TS/2$ in the median plane, and the NP coordinates $0, \pm PS, \pm 2 * PS... \pm (NP - 1) * PS/2$ in the vertical plane.

The position of B downstream is deduced from that of A upstream by a transformation equivalent to two transformations using CHANGREF, namely

$$CHANGREF(XCE = YCE = 0, ALE = \beta)$$

followed by

$$CHANGREF(XCE = YCE = 0, ALE = \theta - \beta)$$

Particle 4 is discarded, while particle 3 continues. The energy loss Q is related to the variable mass M_4 by

 $Q = M_1 + M_2 - (M_3 + M_4)$ and $dQ = -dM_4$

The momentum sampling of particle 3 is derived from conservation of energy and momentum, according to

$$M_1c^2 + W_2 = W_3 + W_4$$

$$p_4^2 = p_2^2 + p_3^2 - 2p_2p_3\cos(\theta - T)$$



Figure 17: Scheme of the principles of CIBLE (TARGET)

A, T = position, angle of incoming particle 2 in the entrance reference frame P = position of the interaction

B, T = position, angle of the secondary particle in the exit reference frame θ = angle between entrance and exit frames

 β = tilt angle of the target

COLLIMA : Collimator

COLLIMA acts as a mathematical aperture of zero length. It causes the identification, counting and stopping of particles that reach the aperture limits.

Physical Aperture

A physical aperture can be either rectangular (*IFORM* = 1) or elliptic (*IFORM* = 2). The collimator is centered at *YC*, *ZC* and has transverse dimensions $\pm YL$ and $\pm ZL$ such that any particle will be stopped if its coordinates *Y*, *Z* satisfy

$$(Y - YC)^2 \ge YL^2$$
 or $(Z - ZC)^2 \ge ZL^2$ if *IFORM* = 1
$$\frac{(Y - YC)^2}{YL^2} + \frac{(Z - ZC)^2}{ZL^2} \ge 1$$
 if *IFORM* = 2

Longitudinal Collimation

COLLIMA can act as a longitudinal phase-space aperture, coordinates acted on are selected with *IFORM.J.* Any particle will be stopped if its horizontal (h) and vertical (v) coordinates satisfy

$$(h \leq h_{min} \text{ or } h \geq h_{max}) \text{ or } (v \leq v_{min} \text{ or } v \geq v_{max})$$

wherein, h is either path length S if *IFORM*=6 or time if *IFORM*=7, and v is either 1+DP/P if J=1 or kinetic energy if J=2 (provided mass and charge have been defined using the keyword *PARTICUL*).

Phase-Space Elliptical Collimation

COLLIMA can act as a phase-space elliptical aperture. Any particle will be stopped if its coordinates satisfy

$$\gamma_Y Y^2 + 2\alpha_Y YT + \beta_Y T^2 \ge \epsilon_Y / \pi$$
 if *IFORM* = 11 or 14
 $\gamma_Z Z^2 + 2\alpha_Z ZP + \beta_Z P^2 \ge \epsilon_Z / \pi$ if *IFORM* = 12 or 15
 $\gamma_S S^2 + 2\alpha_S SD + \beta_S D^2 \ge \epsilon_S / \pi$ if *IFORM* = 13 or 16 (under development)

If *IFORM*=11 (respectively 12, 13) then ϵ_Y/π (respectively ϵ_Z/π , ϵ_S/π) is to be specified by the user as well as $\alpha_{Y,Z,S}$, $\beta_{Y,Z,S}$. If *IFORM*=14 (respectively 15, 16) then α_Y and β_Y (respectively $\alpha_{Z,S}$, $\beta_{Z,S}$) are determined by **zgoubi** by prior computation of the matched ellipse to the particle population, so only $\epsilon_{Y,Z,S}/\pi$ need be specified by the user.

When a particle is stopped, its index *IEX* (see *OBJET* and section 7.12) is set to the value -4, and its actual path length is stored in the array *SORT* for possible further use (*e.g.*, by *HISTO*, or for loss studies, etc.).

CYCLOTRON : Spiral setor cyclotron

CYCLOTRON provides a model of a sector dipole, or a N-tuple of neighboring sector dipoles, with straight or spiraled EFBs [36, Appendix C, p. 149] [37]. The source code has been derived from *FFAG-SPI*, derived itself from *DIPOLES*, thus there is many similarities in the capabilities and operation of these keywords. The field model assumes mid-plane symmetry, with mid-plane normal field component writting

$$B_Z = BN \sum_{i=1}^{N \text{ dipoles}} \mathcal{F}_i(R,\theta) \mathcal{R}_i(R)$$
(6.3.12)

with

- R the distance to the geometrical center of the cyclotron, θ the azimuthal angle,
- BN a normalization coefficient,
- $\mathcal{R}_i(R) = B_{0,i} + B_{1,i} \times R + B_{2,i} \times R^2 + B_{3,i} \times R^3 + \dots$ (up to R^{20})
- $\mathcal{F}(R,\theta)$ the flutter, which accounts in particular for fringe fields.

The field along a particle trajectory is computed as the particle motion proceeds: at any position (R,θ) along the trajectory (Fig 18), the flutter is calculated from the distance to the effective field boundaries of the i=1, N magnet(s), in the following way.

$$\mathcal{F}(R,\theta) = \mathcal{F}_{entr}(R,\theta) \times \mathcal{F}_{exit}(R,\theta) = \frac{1}{1 + \exp(P_{entr}(d_{entr}))} \times \frac{1}{1 + \exp(P_{exit}(d_{exit}))}$$
(6.3.13)

where

$$P(d) = C_0 + C_1 \left(\frac{d}{g}\right) + C_2 \left(\frac{d}{g}\right)^2 + C_3 \left(\frac{d}{g}\right)^3 + C_4 \left(\frac{d}{g}\right)^4 + C_5 \left(\frac{d}{g}\right)^5 + C_6 \left(\frac{d}{g}\right)^6 + C_7 \left(\frac{d}{g}\right)^7$$
(6.3.14)

and d is the distance from the Effective Field Boundary (EFB) either at the entrance or at the exit of the magnet (d_{entr} and d_{exit} as shown in Fig 18).



Figure 18: Definition of the EFB in CYCLOTRON: the trajectory of the moving particle (anti-clockwise motion, here) is in green while the EFB are in red.

An EFB is either straight or spiraled. In the latter case it is modelled by a logarithmic spiral for which the angle ξ is allowed to increase radially, namely:

$$R = R_0 \times \exp\left(\frac{\theta + \omega}{\tan\xi(R)}\right) \tag{6.3.15}$$

where $\xi(R) = \xi_0 + \xi_1 \times R + \xi_2 \times R^2 + \xi_3 \times R^3$, θ is the azimuthal angle and ω is a parameter used to position the EFB with respect to the azimuthal position $\theta=0$.

(page 248 in PART B)

In this model, the magnet gap is also allowed to vary with R, following

$$g(R) = g_0 + g_1 \times R + g_2 \times R^2$$
(6.3.16)

and this determines a radial dependence of the fringe field extent, as follows from P(d) model, Eq. 6.3.14. The field is then extrapolated off median plane by means of Taylor series: for that, the median plane antisymmetry is assumed and Maxwell's equations are accounted for.

CYCLOTRON allows the overlapping of up to N=5 such dipole fields. This follows the method described in [51]. Strictly speaking, the dipoles may even be superimposed (to the point, for instance, that a single dipole (N=1) in an AT sector, with some plateau field value B_{Z0} , can be simulated by superimposing N ≤ 5 identical dipoles, with identical positioning within AT and field B_{Z0}/N each).

In the case of a cyclotron machine, the isochronicity is a crucial point: Because the revolution time has to be constant $(f_{rev} = \frac{qB}{2\pi\gamma m_0})$, this implies that the radial dependence of the field must be proportional to γ , so that $\mathcal{R}(\overline{R}) \propto \gamma(\overline{R})$, where \overline{R} is the average radius of the orbit. Since $f_{rev} = \frac{v}{C}$, where C is the path length of the particle for one closed orbit, one obtains, with a good approximation, that $R \propto \beta$. Thus,

$$\mathcal{R}(R) \approx \frac{1}{\sqrt{1 - (\frac{R}{R_0})^2}}$$
 (6.3.17)

EXAMPLE - An example of the set up and use of CYCLOTRON is given in PART. B, p. 249.

DECAPOLE : Decapole magnet (Fig. 19)

The meaning of parameters for DECAPOLE is the same as for QUADRUPO.

In fringe field regions the magnetic field $\vec{B}(X, Y, Z)$ and its derivatives up to fourth order are derived from the scalar potential expressed to the 5th order in Y and Z

$$\begin{split} V(X,Y,Z) &= G(X)\left(Y^4Z-2Y^2Z^3+\frac{Z^5}{5}\right)\\ \text{with } G_0 &= \frac{B_0}{R_0^4} \end{split}$$

The modelling of the fringe field form factor G(X) is described under QUADRUPO, p. 133.

Outside fringe field regions, or everywhere in sharp edge decapole ($\lambda_E = \lambda_S = 0$), $\vec{B}(X, Y, Z)$ in the magnet is given by

$$B_X = 0$$

$$B_Y = 4G_0(Y^2 - Z^2)YZ$$

$$B_Z = G_0(Y^4 - 6Y^2Z^2 + Z^4)$$



Figure 19: Decapole magnet

DIPOLE : Dipole magnet, polar frame

DIPOLE provides a model of a dipole field, and allows transverse indices. The field along a particle trajectory is computed as the particle motion proceeds, straightforwardly from the dipole geometrical boundaries. Field simulation in *DIPOLE* is the same as used in *DIPOLE-M* and *AIMANT* for computing a field map (Fig. 20); the essential difference in *DIPOLE* is in its skipping that intermediate stage of field map generation found in the former two.

DIPOLE is available in a alternate version, *DIPOLES*, that allows overlapping of fringe fields in a configuration where several neighboring magnets are comprised within the AT angular extent (such as in Fig. 21).



Figure 20: Parameters used to define the geometry of a dipole magnet with index, using DIPOLE[S]

The dimensioning of the magnet is defined by (Fig. 20

AT : total angular aperture

RM : mean radius used for the positioning of field boundaries

The 2 or 3 effective field boundaries (EFB), from which the dipole field is drawn, are defined from geometric boundaries, the shape and position of which are determined by the following parameters.

ACENT	: arbitrary inner angle, used for EFBs positioning
ω	: azimuth of an EFB with respect to ACENT
θ	: angle of an EFB with respect to its azimuth (wedge angle)
R_1, R_2	: radius of curvature of an EFB
U_1, U_2	: extent of the linear part of an EFB.

The magnetic field is calculated in polar coordinates. At any position (R, θ) along the particle trajectory the value of the vertical component of the mid-plane field is calculated using

$$B_Z(R,\theta) = \mathcal{F}(R,\theta) * B_0 * \left(1 + N * \frac{R - RM}{RM} + B * \left(\frac{R - RM}{RM}\right)^2 + G * \left(\frac{R - RM}{RM}\right)^3\right)$$
(6.3.18)

where N, B and G are respectively the first, second and third order field indices and $\mathcal{F}(R,\theta)$ is a fringe field factor (it determines the "flutter" in periodic structures).

Calculation of the Fringe Field Factor

With each EFB a realistic extent of the fringe field, λ (normally equal to the gap size), is associated and a fringe field factor F is calculated. In the following λ stands for either λ_E (Entrance), λ_S (Exit) or λ_L (Lateral EFB).

F is an exponential type fringe field (Fig. 10, p. 72) given by [46]

$$F = \frac{1}{1 + \exp P(s)}$$

wherein s is the distance to the EFB and depends on (R, θ) , and

$$P(s) = C_0 + C_1 \left(\frac{s}{\lambda}\right) + C_2 \left(\frac{s}{\lambda}\right)^2 + C_3 \left(\frac{s}{\lambda}\right)^3 + C_4 \left(\frac{s}{\lambda}\right)^4 + C_5 \left(\frac{s}{\lambda}\right)^5$$

It is also possible to simulate a shift of the *EFB*, by giving a non zero value to the parameter *shift*. s is then changed to s-shift in the previous equation. This allows small variations of the magnetic length.

Let F_E (respectively F_S , F_L) be the fringe field factor attached to the entrance (respectively exit, lateral) EFB. At any position on a trajectory the resulting value of the fringe field factor (eq. 6.3.18) is

$$\mathcal{F}(R,\theta) = F_E * F_S * F_L$$

In particular, $F_L \equiv 1$ if no lateral EFB is requested.



Figure 21: Interpolation method. m_0 and m_1 are the projections in the median plane of particle positions M_0 and M_1 and separated by δs , projection of the integration step.

Calculation of the Mid-plane Field Derivatives

 $B_Z(R,\theta)$ in Eq. 6.3.18 is computed at the $n \times n$ nodes (n = 3 or 5 in practice) of a "flying" interpolation grid in the median plane centered on the projection m_0 of the actual particle position M_0 as schemed in Fig. 21. A polynomial interpolation is involved, of the form

$$B_Z(R,\theta) = A_{00} + A_{10}\theta + A_{01}R + A_{20}\theta^2 + A_{11}\theta R + A_{02}R^2$$

that yields the requested derivatives, using

$$A_{kl} = \frac{1}{k!l!} \frac{\partial^{k+l} B_Z}{\partial \theta^k \partial r^l}$$

Note that, the source code contains the explicit analytical expressions of the coefficients A_{kl} solutions of the normal equations, so that the operation *is not* CPU time consuming.

Extrapolation Off Median Plane

From the vertical field \vec{B} and derivatives in the median plane, first a transformation from polar to Cartesian coordinates is performed, following eqs (1.4.9 or 1.4.10), then, extrapolation off median plane is performed by means of Taylor expansions, following the procedure described in section 1.3.3.

DIPOLE-M : Generation of dipole mid-plane 2-D map, polar frame

DIPOLE-M is a simpler and improved version of AIMANT.

The keyword *DIPOLE-M* provides an automatic generation of a dipole field map in polar coordinates. The extent of the map is defined by the following parameters, as shown in Figs. 9A and 9B.

AT	:	total angular aperture
RM	:	mean radius used for the positioning of field boundaries
RMIN, RMAX	:	minimum and maximum radii

The 2 or 3 effective field boundaries (EFB) inside the map are defined from geometric boundaries, the shape and position of which are determined by the following parameters.

ACENT	:	arbitrary inner angle, used for EFBs positioning
ω	:	azimuth of an EFB with respect to ACENT
θ	:	angle of an EFB with respect to its azimuth (wedge angle)
R_1, R_2	:	radius of curvature of an EFB
U_1, U_2	:	extent of the linear part of an EFB.

At any node of the map mesh, the value of the field is calculated as

$$B_Z(R,\theta) = \mathcal{F}(R,\theta) * B_0 * \left(1 + N * \left(\frac{R - RM}{RM}\right) + B * \left(\frac{R - RM}{RM}\right)^2 + G * \left(\frac{R - RM}{RM}\right)^3\right)$$
(6.3.19)

where N, B and G are respectively the first, second and third order field indices and \mathcal{F} is the fringe field factor.

Calculation of the Fringe Field Factor

With each EFB a realistic extent of the fringe field, λ (normally equal to the gap size), is associated and a fringe field factor F is calculated. In the following λ stands for either λ_E (Entrance), λ_S (Exit) or λ_L (Lateral EFB).

F is an exponential type fringe field (Fig. 10) given by [46]

$$F = \frac{1}{1 + \exp P(s)}$$

where s is the distance to the EFB, and

$$P(s) = C_0 + C_1\left(\frac{s}{\lambda}\right) + C_2\left(\frac{s}{\lambda}\right)^2 + C_3\left(\frac{s}{\lambda}\right)^3 + C_4\left(\frac{s}{\lambda}\right)^4 + C_5\left(\frac{s}{\lambda}\right)^5$$

It is also possible to simulate a shift of the *EFB*, by giving a non zero value to the parameter *shift*. s is then changed to s-*shift* in the previous equation. This allows small variations of the total magnetic length.

Let F_E (respectively F_S , F_L) be the fringe field factor attached to the entrance (respectively exit, lateral) EFB. At any node of the map mesh, the resulting value of the fringe field factor (eq. 6.3.19) is

$$\mathcal{F}(R,\theta) = F_E * F_S * F_L$$

In particular, $F_L \equiv 1$ if no lateral EFB is requested.

The Mesh of the Field Map

The magnetic field is calculated at the nodes of a mesh with polar coordinates, in the median plane. The radial step is given by

$$\delta R = \frac{RMAX - RMIN}{IRMAX - 1}$$

and the angular step by

$$\delta\theta = \frac{AT}{IAMAX - 1}$$

where RMIN and RMAX are the lower and upper radial limits of the field map, and AT is its total angular aperture (Fig. 9B). IRMAX and IAMAX are the total number of nodes in the radial and angular directions.

Simulating Field Defects and Shims

Once the initial map is calculated, it is possible to modify it by means of the parameter *NBS*, so as to simulate field defects or shims.

If NBS = -2, the map is globally modified by a perturbation proportional to $R - R_0$, where R_0 is an arbitrary radius, with an amplitude $\Delta B_Z/B_0$, so that B_Z at the nodes of the mesh is replaced by

$$B_Z * \left(1 + \frac{\Delta B_Z}{B_0} \frac{R - R_0}{RMAX - RMIN} \right)$$

If NBS = -1, the perturbation is proportional to $\theta - \theta_0$, and B_Z is replaced by

$$B_Z * \left(1 + \frac{\Delta B_Z}{B_0} \frac{\theta - \theta_0}{AT} \right)$$

If NBS \geq 1, then NBS shims are introduced at positions $\frac{R_1 + R_2}{2}$, $\frac{\theta_1 + \theta_2}{2}$ (Fig. 12) [47] The initial field map is modified by shims with second order profiles given by

$$\theta = \left(\gamma + \frac{\alpha}{\mu}\right) \beta \frac{X^2}{\rho^2}$$

where X is shown in Fig. 10, $\rho = \frac{R_1 + R_2}{2}$ is the central radius, α and γ are the angular limits of the shim, β and μ are parameters.

At each shim, the value of B_Z at any node of the initial map is replaced by

$$B_Z * \left(1 + F\theta * FR * \frac{\Delta B_Z}{B_0} \right)$$

where $F\theta = 0$ or FR = 0 outside the shim, and $F\theta = 1$ and FR = 1 inside.

Extrapolation Off Median Plane

The vector field \vec{B} and its derivatives in the median plane are calculated by means of a second or fourth order polynomial interpolation, depending on the value of the parameter *IORDRE* (*IORDRE*=2, 25 or 4, see section 1.4.2). The transformation from polar to Cartesian coordinates is performed following eqs (1.4.9 or 1.4.10). Extrapolation off median plane is then performed by means of Taylor expansions, following the procedure described in section 1.3.3.

DIPOLES : Dipole magnet *N*-tuple, polar frame [51, 52]

(page 256 in PART B)

DIPOLES works much like DIPOLE as to the field modelling, yet with the particularity that it allows positioning up to 5 such dipoles within the angular sector with full aperture AT thus allowing accounting for overlapping fringe fields. This is done in the following way⁸.

The dimensioning of the magnet is defined by

- AT : total angular aperture
- RM: mean radius used for the positioning of field boundaries

For each one of the N = 1 to 5 dipoles of the N-tuple, the 2 effective field boundaries (entrance and exit EFBs) from which the dipole field (eqs. 6.3.20, 6.3.22) is drawn are defined from geometrical boundaries, the shape and position of which are determined by the following parameters (in the same manner as in DIPOLE, DIPOLE-M) (see Fig. 20, p. 96, and Fig. 22)

ACN_i	: arbitrary inner angle, used for EFBs positioning
ω	: azimuth of an EFB with respect to ACN
θ	: angle of an EFB with respect to its azimuth (wedge angle)
R_1, R_2	: radius of curvature of an EFB
U_1, U_2	: extent of the linear part of an EFB

Calculation of the Field From a Single Dipole

The magnetic field is calculated in polar coordinates. At all (R, θ) in the median plane (Z = 0), the magnetic field due a single one (index *i*) of the dipoles of a *N*-tuple magnet can take one of the forms below, upon option,

(i)
$$B_{Zi}(R,\theta) = B_{Z0,i} \mathcal{F}_i(R,\theta) (1 + b_{1i}(R - RM_i)/RM_i + b_{2i}(R - RM_i)^2/RM_i^2 + ...)$$
(6.3.20)

(*ii*)
$$B_Z(R,\theta) = B_{Z0,i} + \sum_{i=1}^N \mathcal{F}_i(R,\theta) \left(b_{1_i}(R - RM_i) + b_{2_i}(R - RM_i)^2 + \ldots \right)$$
 (6.3.21)

wherein $B_{Z0,i}$ is a reference field, at reference radius RM_i , and $\mathcal{F}_i(R, \theta)$ is a fringe field factor, see below. This field model is proper to simulate for instance chicane dipoles, cyclotron or FFAG magnets, etc.



Figure 22: Definition of a dipole triplet using the *DIPOLES* or *FFAG* procedures. m is the projection of the particle position in the median plane, the red curve is the projected trajectory

Calculation of the Fringe Field Factor

In a dipole, a realistic extent of the fringe field, g, is associated with each EFB, and a fringe field factor F is calculated.

F is an exponential type fringe field (Fig. 10, page 72) given by [46]

$$F = \frac{1}{1 + \exp P(d)}$$

wherein d is the distance to the EFB and depends on (R, θ) , and

$$P(d) = C_0 + C_1 \left(\frac{d}{g}\right) + C_2 \left(\frac{d}{g}\right)^2 + C_3 \left(\frac{d}{g}\right)^3 + C_4 \left(\frac{d}{g}\right)^4 + C_5 \left(\frac{d}{g}\right)^5$$

In addition, g is made dependent of R (a way to simulate the effect of variable gap size on fringe field extent), under the form

$$g(R) = g_0 \left(RM/R \right)^{\kappa}$$

This dependence is accounted for rigorously if the interpolation method (see below) is used, or else to order zero (derivatives of g(R) are not considered) if the analytic method (below) is used.

Let F_E (respectively F_S) be the fringe field factor attached to the entrance (respectively exit) EFB ; at any position on a trajectory the resulting value of the fringe field factor is taken to be

$$\mathcal{F}_i(R,\theta) = F_E * F_S \tag{6.3.22}$$

Calculation of the Field Resulting From all N Dipoles

Now, accounting for N neighboring dipoles in an N-tuple, the mid-plane field and field derivatives are obtained by addition of the contributions of the N dipoles taken separately, namely

 $^{^{8}}FFAG$ can be referred to as another instance of a procedure based on such method.

$$B_Z(R,\theta) = \sum_{i=1,N} B_{Zi}(R,\theta)$$
 (6.3.23)

$$\frac{\partial^{k+l}\vec{B_Z}(R,\theta)}{\partial\theta^k\partial r^l} = \sum_{i=1,N} \frac{\partial^{k+l}\vec{B_Z}_i(R,\theta)}{\partial\theta^k\partial r^l}$$
(6.3.24)

Note that, in doing so it is not meant that field superposition does apply in reality, it is just meant to provide the possibility of obtaining a realistic field shape, that would for instance closely match (using appropriate $C_0 - C_5$ sets of coefficients) 3-D field simulations obtained from magnet design codes.

Calculation of the Mid-plane Field Derivatives

Two methods have been implemented to calculate the field derivatives in the median plane (Eq. 6.3.23), based on either analytical expressions derived from the magnet geometrical description, or classical numerical interpolation.

The first method has the merit of insuring best symplecticity in principle and fastest tracking. The interest of the second method is in its facilitating possible changes in the mid-plane magnetic field model $B_Z(R, \theta)$, for instance if simulations of shims, defects, or special R, θ field dependence need to be introduced.

Analytical method [53]:

The starting ingredients are, on the one hand distances to the EFBs,

$$d(R,\theta) = \sqrt{(x(R,\theta) - x_0(R,\theta))^2 + (y(R,\theta) - y_0(R,\theta))^2}$$

to be computed for the two cases d_{Entrance} , d_{Exit} , and on the other hand the expressions of the coordinates of particle position M and its projection P on the EFB in terms of the magnet geometrical parameters, namely

$$\begin{array}{rcl} x(R,\theta) &=& \cos(ACN-\theta) - RM \\ y(R,\theta) &=& R\sin(ACN-\theta) \\ x_P(R,\theta) &=& \sin(u) \left(y(R,\theta) - y_b \right)/2 + x_b \sin^2(u) + x(R,\theta) \cos^2(u) \\ y_P(R,\theta) &=& \sin(u) \left(x(R,\theta) - x_b \right)/2 + y_b \cos^2(u) + y(R,\theta) \sin^2(u) \end{array}$$

with x_b , y_b , u parameters drawn from the magnet geometry (sector angle, wedge angle, face curvatures, etc.).

These ingredients allow calculating the derivatives $\frac{\partial^{u+v}x(R,\theta)}{\partial\theta^u\partial r^v}, \frac{\partial^{u+v}y(R,\theta)}{\partial\theta^u\partial r^v}, \frac{\partial^{u+v}x_0(R,\theta)}{\partial\theta^u\partial r^v}, \frac{\partial^{u+v}y_0(R,\theta)}{\partial\theta^u\partial r^v}, \frac{\partial^{u+v}y_0(R,\theta)}{\partial\theta^u\partial r^v}, \frac{\partial^{u+v}p(R,\theta)}{\partial\theta^u\partial r^v}, \frac{\partial^{u+v}p(R,\theta)}{\partial\theta^v\partial r^v}, \frac{\partial^{u+v}p(R,\theta$

Interpolation method :

The expression $B_Z(R, \theta)$ in Eq. 6.3.23 is, in this case, computed at the $n \times n$ nodes (n = 3 or 5 in practice) of a "flying" interpolation grid in the median plane centered on the projection m_0 of the actual particle position M_0 as schemed in Fig. 23. A polynomial interpolation is involved, of the form



Figure 23: Interpolation method. m_0 and m_1 are the projections in the median plane of particle positions M_0 and M_1 and separated by δs , projection of the integration step.

$$B_Z(R,\theta) = A_{00} + A_{10}\theta + A_{01}R + A_{20}\theta^2 + A_{11}\theta R + A_{02}R^2$$

that yields the requested derivatives, using

$$A_{kl} = \frac{1}{k!l!} \frac{\partial^{k+l}B}{\partial \theta^k \partial r^l}$$

Note that, the source code contains the explicit analytical expressions of the coefficients A_{kl} solutions of the normal equations, so that the operation *is not* CPU time consuming.

Extrapolation Off Median Plane

From the vertical field \vec{B} and derivatives in the median plane, first a transformation from polar to Cartesian coordinates is performed, following eqs (1.4.9 or 1.4.10), then, extrapolation off median plane is performed by means of Taylor expansions, following the procedure described in section 1.3.3.

Sharp Edge

Sharp edge field fall-off at a field boundary can only be simulated if the following conditions are fulfilled : - entrance (resp. exit) field boundary coincides with entrance (resp. exit) dipole limit (it means in particular, see Fig. 20, $\omega^+ = ACENT$ (resp. $\omega^- = -(AT - ACENT)$), together with $\theta = 0$ at entrance (resp. exit) EFBs),

- analytical method for calculation of the mid-plane field derivatives is used.

DODECAPO : Dodecapole magnet (Fig. 24)

The meaning of parameters for DODECAPO is the same as for QUADRUPO.

In fringe field regions the magnetic field $\vec{B}(X, Y, Z)$ and its derivatives up to fourth order are derived from the scalar potential approximated to the 6th order in Y and Z

$$\begin{split} V(X,Y,Z) &= G(X) \left(Y^4 - \frac{10}{3} Y^2 Z^2 + Z^4 \right) YZ \\ \text{with} \ G_0 &= \frac{B_0}{R_0^5} \end{split}$$

The modelling of the fringe field form factor G(X) is described under QUADRUPO, p. 133.

Outside fringe field regions, or everywhere in sharp edge dodecapole ($\lambda_E = \lambda_S = 0$), $\vec{B}(X, Y, Z)$ in the magnet is given by

$$B_X = 0$$

$$B_Y = G_0 (5Y^4 - 10Y^2 Z^2 + Z^4) Z$$

$$B_Z = G_0 (Y^4 - 10Y^2 Z^2 + 5Z^4) Y$$



Figure 24: Dodecapole magnet

DRIFT or ESL : Field free drift space

DRIFT or *ESL* allow introduction of a drift space with length *XL* with positive or negative sign, anywhere in an optical sequence. This is an exact transport: the associated equations of motion are (Fig. 25)

$$Y_{2} = Y_{1} + XL * tgT$$
$$Z_{2} = Z_{1} + \frac{XL}{\cos T} tgP$$
$$SAR_{2} = SAR_{1} + \frac{XL}{\cos T * \cos P}$$

whereas the velocity vector is left unchanged.



Figure 25: Transport of particles in a drift space.

The flag '.plt' can be added as a *LABEL2* (second label) following *DRIFT* keyword. It causes local coordinates to be logged to zgoubi.res or to zgoubi.plt (in the same manner as IL=1, or 2, respectively, does in the case optical elements).

A drift can be split into pieces, using the 'split' flag. This may be used for graphic prurposes for instance: a sub-product of 'split' is its allowing using the IL flag, so logging coordinates to either zgoubi.res or to zgoubi.plt (in the same manner as IL=1 or 2, respectively, does in optical elements, step by step).

EBMULT : Electro-magnetic multipole

EBMULT simulates an electro-magnetic multipole, by addition of electric (\vec{E}) and magnetic (\vec{B}) multipole components (dipole to 20-pole). \vec{E} and its derivatives $\frac{\partial^{i+j+k}\vec{E}}{\partial X^i \partial Y^j \partial Z^k}$ $(i+j+k \leq 4)$ are derived from the general expression of the multipole scalar potential (eq. 1.3.5), followed by a $\frac{\pi}{2n}$ rotation (n = 1, 2, 3, ...)(see also *ELMULT*). \vec{B} and its derivatives are derived from the same general potential, as described in section 1.3.7 (see also *MULTIPOL*).

The entrance and exit fringe fields of the \vec{E} and \vec{B} components are treated separately, in the same way as described under *ELMULT* and *MULTIPOL*, for each one of these two fields. Wedge angle correction is applied in sharp edge field model if \vec{B} 1 is non zero, as in *MULTIPOL*. Any of the \vec{E} or \vec{B} multipole field component can be X-rotated independently of the others.

Use PARTICUL prior to EBMULT, for the definition of particle mass and charge.



Figure 26: An example of \vec{E} , \vec{B} multipole : the achromatic quadrupole (known for its allowing null second order chromatic aberrations [54]).

EL2TUB : Two-tube electrostatic lens

The lens is cylindrically symmetric about the X-axis.

The length and potential of the first (resp. second) electrode are X1 and V1 (X2 and V2). The distance between the two electrodes is D, and their inner radius is R_0 (Fig. 27). The model for the electrostatic potential along the axis is [55]

$$V(X) = \frac{V_2 - V_1}{2} \operatorname{th} \frac{\omega x}{R_0} \left[+ \frac{V_1 + V_2}{2} \right] \qquad \text{if } D = 0$$
$$V(X) = \frac{V_2 - V_1}{2} \frac{1}{2\omega D/R_0} \ln \frac{\operatorname{ch} \omega \frac{x + D}{R_0}}{\operatorname{ch} \omega \frac{x - D}{R_0}} \left[+ \frac{V_1 + V_2}{2} \right] \qquad \text{if } D \neq 0$$

(x = distance from half-way between the electrodes ; $\omega = 1.318$; th = hyperbolic tangent ; ch = hyperbolic cosine) from which the field $\vec{E}(X, Y, Z)$ and its derivatives are derived following the procedure described in section 1.3.1 (note that they don't depend on the constant term $\left[\frac{V_1 + V_2}{2}\right]$ which disappears when differentiating).

Use PARTICUL prior to EL2TUB, for the definition of particle mass and charge.



Figure 27: Two-electrode cylindrical electric lens.
ELCYLDEF : Electrostatic cylindrical deflector

TO BE DOCUMENTED.

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ELMIR : Electrostatic N-electrode mirror/lens, straight slits

The device works as mirror or lens, horizontal or vertical. It is made of N 2-plate electrodes and has mid-plane symmetry.

Electrode lengths are *L*1, *L*2, ..., *LN*. *D* is the mirror/lens gap. The model for the *Y*-independent electrostatic potential is (after Ref. [56, p.412])

$$V(X,Z) = \sum_{i=2}^{N} \frac{Vi - Vi}{\pi} \arctan \frac{\sinh(\pi (X - Xi)/D)}{\cos(\pi Z/D)}$$

where Vi are the potential at the N electrodes (and normally V1 = 0 refers to the incident beam energy), Xi are the locations of the zero-length slits, X is the distance from the origin taken at the first slit (located at $X1 \equiv 0$ between the first and second electrodes). From V(X, Z) the field $\vec{E}(X, Y, Z)$ and derivatives are deduced following the procedure described in section 1.3.7 (page 28).

The total X-extent of the mirror/lens is $L = \sum_{i=1}^{N} Li$.

In the mirror mode (option MT = 11 for vertical mid-plane or MT = 12 for horizontal mid-plane) stepwise integration starts at X = -L1 (entrance of the first electrode) and terminates either when back to X = -L1or when reaching X = L - L1 (end of the N - th electrode). In the latter case particles are stopped with their index *IEX* set to -8 (see section 7.12 on page 211). Normally X1 should exceed 3D (enough that V(X < X1) have negligible effect in terms of trajectory behavior).

In the lens mode (option flag MT = 21 for vertical mid-plane or MT = 22 for horizontal mid-plane) stepwise integration starts at X = -L1 (entrance of the first electrode) and terminates either when reaching X = L - L1 (end of the N - th electrode) or when the particle deflection exceeds $\pi/2$. In the latter case the particle is stopped with their index *IEX* set to -3.

Use PARTICUL prior to ELMIR, for the definition of particle mass and charge.



Figure 28: Electrostatic N-electrode mirror/lens, straight slits, in the case N = 3, in horizontal mirror mode (MT = 11). Possible non-zero entrance quantities YCE, ALE should be specified using CHANGREF, or using KPOS=3 with YCE and ALE=half-deviation matched to the reference trajectory.

ELMIRC : Electrostatic N-electrode mirror/lens, circular slits [56]

The device works as mirror or lens, horizontal or vertical. It is made of N 2-plate electrodes and has mid-plane symmetry⁹.

Electrode slits are circular, concentric with radii R1, R2, ..., R_{N-1} , D is the mirror/lens gap. The model for the mid-plane (Z = 0) radial electrostatic potential is (after Ref. [56, p.443])

$$V(r) = \sum_{i=2}^{N} \frac{Vi - Vi}{\pi} \arctan\left(\sinh\frac{\pi(r - Ri)}{D}\right)$$

where Vi are the potential at the N electrodes (and normally V1 = 0 refers to the incident beam energy). r is the current radius.

The mid-plane field $\vec{E}(r)$ and its *r*-derivatives are first derived by differentiation, then $\vec{E}(r, Z)$ and derivatives are obtained from Taylor expansions and Maxwell relations. Eventually a transformation to the rotating frame provides $\vec{E}(X, Y, Z)$ and derivatives as involved in eq. 1.2.15.

Stepwise integration starts at entrance (defined by RE, TE) of the first electrode and terminates when rotation of the reference rotating frame (RM, X, Y) has reached the value AT. Normally, R1 - RE and R1 - RS should both exceed 3D (so that potential tails have negligible effect in terms of trajectory behavior).

Positioning of the element is performed by means of KPOS (see section 7.9).

Use PARTICUL prior to ELMIRC, for the definition of particle mass and charge.



Figure 29: Electrostatic N-electrode mirror/lens, circular slits, in the case N = 3, in horizontal mirror mode.

ELMULT : Electric multipole

The simulation of multipolar electric field \vec{M}_E proceeds by addition of the dipolar $(\vec{E}1)$, quadrupolar $(\vec{E}2)$, sextupolar $(\vec{E}3)$, etc., up to 20-polar $(\vec{E}10)$ components, and of their derivatives up to fourth order, following

$$\vec{M}_E = \vec{E}1 + \vec{E}2 + \vec{E}3 + \dots + \vec{E}10$$
$$\frac{\partial \vec{M}_E}{\partial X} = \frac{\partial \vec{E}1}{\partial X} + \frac{\partial \vec{E}2}{\partial X} + \frac{\partial \vec{E}3}{\partial X} + \dots + \frac{\partial \vec{E}10}{\partial X}$$
$$\frac{\partial^2 M_E}{\partial X \partial Z} = \frac{\partial^2 \vec{E}1}{\partial X \partial Z} + \frac{\partial^2 \vec{E}2}{\partial X \partial Z} + \frac{\partial^2 \vec{E}3}{\partial X \partial Z} + \dots + \frac{\partial^2 \vec{E}10}{\partial X \partial Z}$$
etc.

The independent components $\vec{E}1$ to $\vec{E}10$ and their derivatives up to the fourth order are calculated by differentiating the general multipole potential given in eq. 1.3.5 (page 29), followed by a $\frac{\pi}{2n}$ rotation about the X-axis, so that the so defined right electric multipole of order n, and of strength [54, 57]

$$K_n = \frac{1}{2} \frac{\gamma}{\gamma^2 - 1} \frac{V_n}{R_0^n}$$

 $(V_n = \text{potential at the electrode}, R_0 = \text{radius at pole tip}, \gamma = \text{relativistic Lorentz factor of the particle})$ has the same focusing effect as the right magnetic multipole of order n and strength $K_n = \frac{B_n}{R_0^{n-1}B\rho}$ (B_n = field at pole tip, $B\rho$ = particle rigidity, see *MULTIPOL*).

The entrance and exit fringe fields are treated separately. They are characterized by the integration zone X_E at entrance and X_S at exit, as for *QUADRUPO*, and by the extent λ_E at entrance, λ_S at exit. The fringe field extents for the dipole component are λ_E and λ_S . The fringe field extent for the quadrupolar (sextupolar, ..., 20-polar) component is given by a coefficient E_2 (E_3 , ..., E_{10}) at entrance, and S_2 (S_3 , ..., S_{10}) at exit, such that the fringe field extent is $\lambda_E * E_2$ ($\lambda_E * E_3$, ..., $\lambda_E * E_{10}$) at entrance and $\lambda_S * S_2$ ($\lambda_S * S_3$, ..., $\lambda_S * S_{10}$) at exit.

If $\lambda_E = 0$ ($\lambda_S = 0$) the multipole lens is considered to have a sharp edge field at entrance (exit), and then, $X_E(X_S)$ is forced to zero (for the mere purpose of saving computing time).

If $E_i = 0$ ($S_i = 0$) (i = 2, 10), the entrance (exit) fringe field for multipole component i is considered as a sharp edge field.

Any multipole component $\vec{E}i$ can be rotated independently by an angle RXi around the longitudinal X-axis, for the simulation of positioning defects, as well as skew lenses.

Use PARTICUL prior to ELMULT, for the definition of particle mass and charge.



Figure 30: An electric multipole combining skew-quadrupole $(\vec{E}2 \neq \vec{0}, \vec{R}2 = \pi/4)$ and skew-octupole $(\vec{E}4 \neq \vec{0}, \vec{R}4 = \pi/8)$ components $(\vec{E}1 = \vec{E}3 = \vec{E}5 = \dots = \vec{E}10 = \vec{0})$ [57].

ELREVOL : 1-D uniform mesh electric field map

ELREVOL reads a 1-D axial field map from a storage data file, whose content must fit the following FORTRAN reading sequence

```
OPEN (UNIT = NL, FILE = FNAME, STATUS = 'OLD' [,FORM='UNFORMATTED'])
DO 1 I=1, IX
    IF (BINARY) THEN
        READ(NL) X(I), EX(I)
    ELSE
        READ(NL,*) X(I), EX(I)
    ENDIF
    1 CONTINUE
```

where IX is the number of nodes along the (symmetry) X-axis, X(I) their coordinates, and EX(I) are the values of the X component of the field. EX is normalized with ENORM prior to ray-tracing. As well the longitudinal coordinate X is normalized with a XNORM coefficient (useful to convert to centimeters, the working units in **zgoubi**).

X-cylindrical symmetry is assumed, resulting in EY and EZ taken to be zero on axis. $\vec{E}(X, Y, Z)$ and its derivatives along a particle trajectory are calculated by means of a 5-points polynomial interpolation followed by second order off-axis extrapolation (see sections 1.3.1 and 1.4.1).

Entrance and/or exit integration boundaries may be defined in the same way as in *CARTEMES* by means of the flag ID and coefficients A, B, C, A', B', C'.

Use PARTICUL prior to ELREVOL, for the definition of particle mass and charge.

EMMA : 2-D Cartesian or cylindrical mesh field map for EMMA FFAG

EMMA is dedicated to the reading and treatment of 2-D or 3-D Cartesian mesh field maps representing the EMMA FFAG cell quadrupole doublet¹⁰ [60, 61].

EMMA can sum up independent field maps of each of the two quadrupoles, with each its scaling coefficient. The two maps can be radially positioned independently of one another at Y_F , Y_D respectively, just like the actual *EMMA* quadrupoles. In particular,

MOD: operational and map *FORMAT* reading mode; $MOD \le 19$: Cartesian mesh; $MOD \ge 20$: cylindrical mesh.

MOD=0 : two 2D maps, one representing QF, one representing QD. A single map, superimposition of both, is built prior to tracking and used for tracking.

MOD=1: two 2D maps, one representing QF, one representing QD, a resulting single map is devised in the following way: QF_new is interpolated from QF with dr=xF, QD_new is interpolated from QD with dr=xD. A single map, superimposition of both, is built prior to tracking and used for tracking.

The parameters that move/position the maps, as (Y_F, Y_D) , are accessible from the FIT, allowing to adjust the cell tunes.

EMMA works much like TOSCA. Refer to that keyword, and to the FORTRAN file emmac.f, for details.

FFAG : FFAG magnet, N-tuple [51, 52]

(page 270 in PART B)

smallskip

FFAG works much like *DIPOLES* as to the field modelling, apart from the radial dependence of the field, $B = B_0(r/r_0)^k$, so-called "scaling". Note that *DIPOLES* does similar job by using a Taylor *r*-expansion of $B_0(r/r_0)^k$.

smallskip

The *FFAG* procedure allows overlapping of fringe fields of neighboring dipoles, thus simulating in some sort the field in a dipole N-tuple - as for instance in an FFAG doublet or triplet. A detailed application, with five dipoles, can be found in Ref. [51]. This is done in the way described below.

smallskip

The dimensioning of the magnet is defined by

smallskip

AT : total angular apertureRM : mean radius used for the positioning of field boundaries

smallskip

For each one of the N = 1 to (maximum) 5 dipoles of the *N*-tuple, the two effective field boundaries (entrance and exit EFBs) from which the dipole field is drawn are defined from geometric boundaries, the shape and position of which are determined by the following parameters (in the same manner as in *DIPOLE*, *DIPOLE-M*) (see Fig. 20 page 96, and Fig. 31)

- ACN_i : arbitrary inner angle, used for EFBs positioning
- ω : azimuth of an EFB with respect to ACN
- θ : angle of an EFB with respect to its azimuth (wedge angle)
- R_1, R_2 : radius of curvature of an EFB
- U_1, U_2 : extent of the linear part of an EFB



Figure 31: Definition of a dipole *N*-tuple (N = 3, a triplet here) using the *DIPOLES* or *FFAG* procedures. m is the projection of the particle position in the median plane, the red curve is the projected trajectory

Calculation of the Field From a Single Dipole

The magnetic field is calculated in polar coordinates. At all (R, θ) in the median plane (z = 0), the magnetic field due a single one (index *i*) of the dipoles of a *N*-tuple FFAG magnet is written

$$B_{Zi}(R,\theta) = B_{Z0,i} \mathcal{F}_i(R,\theta) \left(R/R_M \right)^{K_i}$$
(6.3.25)

wherein $B_{Z0,i}$ is a reference field, at reference radius RM_i , whereas $\mathcal{F}(R,\theta)$ is calculated as described below.

Calculation of $\mathcal{F}_i(R, \theta)$

The fringe field factor $\mathcal{F}_i(R,\theta)$ associated with a dipole is computed as in the procedure *DIPOLES* (eq. 6.3.22), including (rigorously if the interpolation method is used, see page 103, or to order zero if the analytic method is used, see page 103) radial dependence of the gap size

$$g(R) = g_0 \, (RM/R)^{\kappa} \tag{6.3.26}$$

so to simulate the effect of gap shaping on $B_{Zi}(R, \theta)|_R$ field fall-off, over the all radial extent of a scaling FFAG dipole (with normally - but not necessarily in practice - $\kappa \approx K_i$).

Calculation of the Field Resulting From All ${\it N}$ Dipoles

For the rest, namely, calculation of the full field at particle position from the N dipoles, analytical calculation or numerical interpolation of the mid-plane field derivatives, extrapolation off median plane, etc., things are performed exactly as in the case of the *DIPOLES* procedure (see page 102).

Sharp Edge

Sharp edge field fall-off at a field boundary can only be simulated if the following conditions are fulfilled :

- entrance (resp. exit) field boundary coincides with entrance (resp. exit) dipole limit (it means in particular, see Fig. 20, $\omega^+ = ACENT$ (resp. $\omega^- = -(AT - ACENT)$), together with $\theta = 0$ at entrance (resp. exit) EFBs),

- analytical method for calculation of the mid-plane field derivatives is used.

FFAG-SPI : Spiral FFAG magnet, N-tuple [52, 58]

FFAG-SPI works much like FFAG as to the field modelling, with essentially a different axial dependence.

The *FFAG-SPI* procedure allows overlapping of fringe fields of neighboring dipoles, thus simulating in some sort the field in a dipole *N*-tuple (similar to Fig. 31, page 117). This allows for instance accounting for fringe field effects, or clamps, as schemed in Fig. 32.

The dimensioning of the magnet is defined by

AT : total angular aperture*RM* : mean radius used for the positioning of field boundaries

For each one of the N = 1 to (maximum) 5 dipoles of the *N*-tuple, the two effective field boundaries (entrance and exit EFBs) from which the dipole field is drawn are defined from geometric boundaries, the shape and position of which are determined by the following parameters

ACN_i	:	arbitrary inner angle, used for EFBs positioning
ω	:	azimuth of an EFB with respect to ACN
ξ	:	spiral angle

with ACN_i and ω as defined in Fig. 32 (similar to what can be found in Figs. 31 and 20).



Figure 32: A *N*-tuple spiral sector FFAG magnet (N = 3 here, simulating active field clamps at entrance and exit side of a central dipole).

Calculation of the Field From a Single Dipole

The magnetic field is calculated in polar coordinates. At all (R, θ) in the median plane (Z = 0), the magnetic field due a single one (index *i*) of the dipoles of a *N*-tuple spiral FFAG magnet is written

$$B_{Zi}(R,\theta) = B_{Z0,i} \mathcal{F}_i(R,\theta) \left(\frac{R}{R_M} \right)^{K_i}$$
(6.3.27)

wherein $B_{Z0,i}$ is a reference field, at reference radius RM_i , whereas $\mathcal{F}(R,\theta)$ is calculated as described below.

Calculation of $\mathcal{F}_i(R,\theta)$

The fringe field factor $\mathcal{F}_i(R, \theta)$ associated with a dipole is computed as in the procedure *DIPOLES* (eq. 6.3.22), including radial dependence of the gap size

$$g(R) = g_0 \, (RM/R)^{\kappa} \tag{6.3.28}$$

so to simulate the effect of gap shaping on $B_{Zi}(R, \theta)|_R$ field fall-off, over the all radial extent of the dipole (with normally - yet not necessarily in practice - $\kappa \approx -1$).

In the case $\kappa = -1$, the scaling condition for sector spiral rings is satisfied. In that case the fringe field function may be transformed to

$$\mathcal{F}(R,\theta) = \mathcal{F}(\psi)$$

where

$$\psi = \theta - \tan \xi ln \frac{R}{RM}$$

is the *generalised* azimuthal angle. The distance between spirals is constant in terms of ψ . The fringe field extent g(R) can be converted into an angular extent $\Delta \psi_g$ via,

$$\Delta \psi_g = \frac{g_0}{RM \cos\xi}$$

Then the fringe field dependence is given by $P(\Delta \psi_d / \Delta \psi_g)$ where $\Delta \psi_d$ is evaluated at the current particle location, replacing the P(d/g) described in the **DIPOLES** procedure. On the other hand, if $\kappa \neq -1$, the scaling condition is not fulfilled and so the distance to the magnet edge d must be found numerically. At the moment, the generalised azimuthal angle approach is applied in the code only if the flying mesh interpolation method is used. The numerical method can be forced by including the DNEWT flag (see page 271).

Calculation of the Full Field From All N Dipoles

For the rest, namely calculation of the full field at particle position, as resulting from the N dipoles, calculation of the mid-plane field derivatives, extrapolation off median plane, etc., things are performed in the same manner as for the *DIPOLES* procedure (see page 102).

HALBACH : Halbach style permanent magnet

HALBACH generates magnetic field from a Halbach style permanent magnet [63].

Fig. 3 is an example of a cross section of a focusing quadrupole on the left, and a defocusing combined function dipole on the right (combined quadrupole + dipole components) [65]. The black lines on the figures are the equipotential vector lines. QF is made of 16 wedges and its quadrupole component is given by [66]

$$2B_{rm}\cos^2\left(\frac{\pi}{M}\right)\frac{\sin\left(\frac{2\pi}{M}\right)}{\frac{2\pi}{M}}\left(\frac{1}{r_i}-\frac{1}{r_0}\right) \tag{6.3.29}$$

with B_{rm} is the remnant magnetization, r_i and r_o the inner and outer radii of the annulus made by the wedges, and M the number of magnetized wedges. The magnetization direction α of each of the wedges is given by $\alpha = 3\theta + \pi/2$, where θ is the azimuthal angle of each wedge.

HELIX : Helical dipole

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HELIX provides magnetic field from a helical dipole [64]. It can be used for instance to simulate light source helical wigglers, or siberian snakes in polarized beam accelerators.

The field components are computed following

$$\begin{cases} B_Y/B_0 = -(1 + \frac{k^2}{8}(3Y^2 + Z^2))\sin(kX) + \frac{k^2}{4}YZ\cos(kX) \\ B_Z/B_0 = (1 + \frac{k^2}{8}(Y^2 + 3Z^2))\cos(kX) - \frac{k^2}{4}YZ\sin(kX) \\ B_X/B_0 = -k(1 + \frac{k^2}{8}(Y^2 + Z^2))(Y\cos(kX) + Z\sin(kX)) \end{cases}$$
(6.3.30)

wherein

$$k = \epsilon \frac{2\pi}{\lambda}$$

$$\lambda \qquad \text{the pitch}$$

$$\epsilon = \pm 1 \qquad \text{the helicity (+ for right-handed)}$$
(6.3.31)

X is the distance along the helix axis, B_0 is the peak transverse field value.

Two techniques are avalabe to compute the field and derivatives:

- the field is computed from Eq. 6.3.30, its derivatives are hard-coded, up to the second order in the coordinates
- the field at particle location and at the 26 neighboring nodes of a cubic mesh (Fig. 4) are computed from Eq. 6.3.30, numerical values of the derivatives are obtained by interpolation from that mesh (see Sec. 1.4.4).

MAP2D : 2-D Cartesian uniform mesh field map - arbitrary magnetic field [62]

MAP2D reads a 2-D field map that provides the three components B_X , B_Y , B_Z of the magnetic field at all nodes of a 2-D Cartesian uniform mesh in an (X, Y) plane. No particular symmetry is assumed, which allows the treatment of any type of field (*e.g.*, solenoidal, or dipole, helical dipole, at arbitrary Z elevation - the map needs not be a mid-plane map).

The field map data file has to be be filled with a format that satisfies the *FORTRAN* reading sequence below (in principle compatible with *TOSCA* code outputs), details and possible updates are to be found in the source file ' fmapw.f' :

```
OPEN (UNIT = NL, FILE = FNAME, STATUS = 'OLD' [,FORM='UNFORMATTED'])

DO 1 J=1,JY

DO 1 I=1,IX

IF (BINARY) THEN

READ(NL) Y(J), Z, X(I), BY(I,J), BZ(I,J), BX(I,J)

ELSE

READ(NL,100) Y(J), Z, X(I), BY(I,J), BZ(I,J), BX(I,J)

100

FORMAT (1X, 6E11.4)

ENDIF

1

CONTINUE
```

IX (JY) is the number of longitudinal (transverse horizontal) nodes of the 2-D uniform mesh, Z is the considered Z-elevation of the map. For binary files, FNAME must begin with 'B₋' or 'b₋', a flag 'BINARY' will thus be set to '.TRUE.'. The field $\vec{B} = (B_X, B_Y, B_Z)$ is next normalized with BNORM, prior to ray-tracing. As well the coordinates X, Y are normalized with X-, Y-NORM coefficients (useful to convert to centimeters, the working units in **zgoubi**).

At each step of the trajectory of a particle, the field and its derivatives are calculated using a second or fourth degree polynomial interpolation followed by a Z extrapolation (see sections 1.3.4 page 28, 1.4.3 page 33). The interpolation grid is 3*3-node for 2nd order (option *IORDRE = 2*) or 5*5 for 4th order (option *IORDRE = 4*).

Entrance and/or exit integration boundaries may be defined, in the same way as for CARTEMES.

MAP2D-E: 2-D Cartesian uniform mesh field map - arbitrary electric field

MAP2D-E reads a 2-D field map that provides the three components E_X , E_Y , E_Z of the electric field at all nodes of a 2-D Cartesian uniform mesh in an (X, Y) plane. No particular symmetry is assumed, which allows the treatment of any type of field (*e.g.*, field of a parallel-plate mirror with arbitrary Z elevation - the map needs not be a mid-plane map).

The field map data file has to be be filled with a format that satisfies the *FORTRAN* reading sequence below (in principle compatible with *TOSCA* code outputs), details and possible updates are to be found in the source file ' fmapw.f' :

```
OPEN (UNIT = NL, FILE = FNAME, STATUS = 'OLD' [,FORM='UNFORMATTED'])

DO 1 J=1,JY

DO 1 I=1,IX

IF (BINARY) THEN

READ(NL) Y(J), Z, X(I), EY(I,J), EZ(I,J), EX(I,J)

ELSE

READ(NL,100) Y(J), Z, X(I), EY(I,J), EZ(I,J), EX(I,J)

100 FORMAT (1X, 6E11.4)

ENDIF

1 CONTINUE
```

IX (JY) is the number of longitudinal (transverse horizontal) nodes of the 2-D uniform mesh, Z is the considered Z-elevation of the map. For binary files, FNAME must begin with 'E₋' or 'b₋', a flag 'BINARY' will thus be set to '.TRUE.'. The field $\vec{E} = (E_X, E_Y, E_Z)$ is next normalized with ENORM, prior to ray-tracing. As well the coordinates X, Y are normalized with X-, Y-NORM coefficients (useful to convert to centimeters, the working units in **zgoubi**.

At each step of the trajectory of a particle, the field and its derivatives are calculated using a second or fourth degree polynomial interpolation followed by a Z extrapolation (see sections 1.3.4 page 28, 1.4.3 page 33). The interpolation grid is 3*3-node for 2nd order (option *IORDRE = 2*) or 5*5 for 4th order (option *IORDRE = 4*).

Entrance and/or exit integration boundaries may be defined, in the same way as for CARTEMES.

MARKER : Marker

MARKER does nothing. Just a marker. No data.

As any other keyword, *MARKER* is allowed two *LABELs*. Using '.plt' as a second *LABEL* will cause storage of current coordinates into zgoubi.plt.

MULTIPOL : Magnetic multipole

The simulation of multipolar magnetic field \vec{M} by *MULTIPOL* proceeds by addition of the dipolar $(\vec{B}1)$, quadrupolar $(\vec{B}2)$, sextupolar $(\vec{B}3)$, etc., up to 20-polar $(\vec{B}10)$ components, and of their derivatives up to fourth order, following

$$\dot{M} = \vec{B}1 + \vec{B}2 + \vec{B}3 + \dots + \vec{B}10$$
$$\frac{\partial \vec{M}}{\partial X} = \frac{\partial \vec{B}1}{\partial X} + \frac{\partial \vec{B}2}{\partial X} + \frac{\partial \vec{B}3}{\partial X} + \dots + \frac{\partial \vec{B}10}{\partial X}$$
$$\frac{\partial^2 \vec{M}}{\partial X \partial Z} = \frac{\partial^2 \vec{B}1}{\partial X \partial Z} + \frac{\partial^2 \vec{B}2}{\partial X \partial Z} + \frac{\partial^2 \vec{B}3}{\partial X \partial Z} + \dots + \frac{\partial^2 \vec{B}10}{\partial X \partial Z}$$
etc.

The independent components $\vec{B}_1, \vec{B}_2, \vec{B}_3, ..., \vec{B}_{10}$ and their derivatives up to the fourth order are calculated as described in section 1.3.7.

The entrance and exit fringe fields are treated separately. They are characterized by the integration zone X_E at entrance and X_S at exit, as for QUADRUPO, and by the extent λ_E at entrance, λ_S at exit. The fringe field extents for the dipole component are λ_E and λ_S . The fringe field for the quadrupolar (sextupolar, ..., 20-polar) component is given by a coefficient E_2 (E_3 , ..., E_{10}) at entrance, and S_2 (S_3 , ..., S_{10}) at exit, such that the extent is $\lambda_E * E_2$ ($\lambda_E * E_3$, ..., $\lambda_E * E_{10}$) at entrance and $\lambda_S * S_2$ ($\lambda_S * S_3$, ..., $\lambda_S * S_{10}$) at exit.

If $\lambda_E = 0$ ($\lambda_S = 0$) the multipole lens is considered to have a sharp edge field at entrance (exit), and then, $X_E(X_S)$ is forced to zero (for the mere purpose of saving computing time). If $E_i = 0$ ($S_i = 0$) (i = 2, 10), the entrance (exit) fringe field for the multipole component i is considered as a sharp edge field. In sharp edge field model, the wedge angle vertical first order focusing effect (if $\vec{B}1$ is non zero) is simulated at magnet entrance and exit by a kick $P_2 = P_1 - Z_1 \tan(\epsilon/\rho)$ applied to each particle (P_1, P_2 are the vertical angles upstream and downstream of the EFB, Z_1 is the vertical particle position at the EFB, ρ the local horizontal bending radius and ϵ the wedge angle experienced by the particle ; ϵ depends on the horizontal angles T).

Any multipole component $\vec{B}i$ can be rotated independently by an angle RXi around the longitudinal X-axis, for the simulation of positioning defects, as well as skew lenses.

Magnet (mis-)alignment is assured by *KPOS*. *KPOS* also allows some degrees of automatic alignment useful for periodic structures (section 7.9).

OCTUPOLE : Octupole magnet (Fig. 33)

(page 301 in PART B)

The meaning of parameters for OCTUPOLE is the same as for QUADRUPO. In fringe field regions the magnetic field $\vec{B}(X, Y, Z)$ and its derivatives up to fourth order are derived from the scalar potential approximated to the 8-th order in Y and Z

$$V(X, Y, Z) = \left(G(X) - \frac{G''(X)}{20} \left(Y^2 + Z^2\right) + \frac{G''''(X)}{960} \left(Y^2 + Z^2\right)^2\right) \left(Y^3 Z - Y Z^3\right)$$

with $G_0 = \frac{B_0}{R_0^3}$

The modelling of the fringe field form factor G(X) is described under QUADRUPO, p. 133.

Outside fringe field regions, or everywhere in sharp edge dodecapole ($\lambda_E = \lambda_S = 0$), $\vec{B}(X, Y, Z)$ in the magnet is given by

$$B_X = 0$$

 $B_Y = G_0(3Y^2 - Z^2) Z$
 $B_Z = G_0(Y^2 - 3Z^2) Y$



Figure 33: Octupole magnet

POISSON : Read magnetic field data from POISSON output

This keyword allows reading a field profile B(X) from *POISSON* output. Let *FNAME* be the name of this output file (normally, *FNAME* = outpoi.lis); the data are read following the *FORTRAN* statements here under

where X(I) is the longitudinal coordinate, and B(I) is the Z component of the field at a node (I) of the mesh. Ks and Rs are dummy variables appearing in the *POISSON* output file outpoi.lis but not used here.

From this field profile, a 2-D median plane map is built, with a rectangular and uniform mesh; mid-plane symmetry is assumed. The field at each node (X_i, Y_j) of the map is $B(X_i)$, independent of Y_j (*i.e.*, the distribution is uniform in the Y direction).

For the rest, POISSON works in a way similar to CARTEMES.

POLARMES : 2-D polar mesh magnetic field map

medskip

Similar to *CARTEMES*, apart from the polar mesh frame : IX is the number of angular nodes, JY the number of radial nodes ; X(I) and Y(J) are respectively the angle and radius of a node (these parameters are similar to those entering in the definition of the field map in *DIPOLE-M*).

PS170 : Simulation of a round shape dipole magnet

PS170 is dedicated to a 'rough' simulation of CERN PS170 spectrometer dipole.

The field B_0 is constant inside the magnet, and zero outside. The pole is a circle of radius R_0 , centered on the X axis. The output coordinates are generated at the distance XL from the entrance (Fig. 34).



Figure 34: Scheme of the PS170 magnet simulation.

QUADISEX, SEXQUAD : Sharp edge magnetic multipoles

SEXQUAD defines in a simple way a sharp edge field with quadrupolar, sextupolar and octupolar components. QUADISEX adds a dipole component. The length of the element is XL. The vertical component $B \equiv B_Z(X, Y, Z = 0)$ of the field and its derivatives in median plane are calculated at each step using the following expressions

$$B = B_0 \left(U + \frac{N}{R_0} Y + \frac{B}{R_0^2} Y^2 + \frac{G}{R_0^3} Y^3 \right)$$
$$\frac{\partial B}{\partial Y} = B_0 \left(\frac{N}{R_0} + 2\frac{B}{R_0^2} Y + 3\frac{G}{R_0^3} Y^2 \right)$$
$$\frac{\partial^2 B}{\partial Y^2} = B_0 \left(2\frac{B}{R_0^2} + 6\frac{G}{R_0^3} Y \right)$$
$$\frac{\partial^3 B}{\partial Y^3} = 6B_0 \frac{G}{R_0^3}$$

and then extrapolated out of the median plane by Taylor expansion in Z (see section 1.3.3). With option SEXQUAD, U = 0, while with QUADISEX, U = 1.

QUADRUPO : Quadrupole magnet (Fig. 35)

The length of the magnet XL is the distance between the effective field boundaries (EFB), Fig. 36. The field at the pole tip R_0 is B_0 .

The extent of the entrance (exit) fringe field is characterized by $\lambda_E(\lambda_S)$. The distance of ray-tracing on both sides of the EFBs, in the field fall off regions, will be $\pm X_E$ at the entrance, and $\pm X_S$ at the exit (Fig. 36), by prior and further automatic change of frame.

In the fringe field regions $[-X_E, X_E]$ and $[-X_S, X_S]$ on both sides of the EFBs, $\vec{B}(X, Y, Z)$ and its derivatives up to fourth order are calculated at each step of the trajectory from the analytical expressions of the three components B_X , B_Y , B_Z obtained by differentiation of the scalar potential (see section 1.3.7) expressed to the 8th order in Y and Z.

$$V(X,Y,Z) = \left(G(X) - \frac{G''(X)}{12} \left(Y^2 + Z^2\right) + \frac{G''''(X)}{384} \left(Y^2 + Z^2\right)^2 - \frac{G'''''(X)}{23040} \left(Y^2 + Z^2\right)^3\right) YZ$$

$$\left(-G^{(n)}(X) = d^n G(X)/dX^n, etc.\right)$$

where G(X) is the gradient on axis [46] :

$$G(X) = \frac{G_0}{1 + \exp P(d(X))}$$
 with $G_0 = \frac{B_0}{R_0}$

and,

$$P(d) = C_0 + C_1 \left(\frac{d}{\lambda}\right) + C_2 \left(\frac{d}{\lambda}\right)^2 + C_3 \left(\frac{d}{\lambda}\right)^3 + C_4 \left(\frac{d}{\lambda}\right)^4 + C_5 \left(\frac{d}{\lambda}\right)^5$$

where d(X) is the distance to the field boundary and λ stands for λ_E or λ_S (normally, $\lambda \simeq 2 * R_0$). When fringe fields overlap inside the magnet ($XL \le X_E + X_S$), the gradient G is expressed as

$$G = G_E + G_S - 1$$

where, G_E is the entrance gradient and G_S is the exit gradient.

If $\lambda_E = 0$ ($\lambda_S = 0$), the field at entrance (exit) is considered as sharp edged, and then $X_E(X_S)$ is forced to zero (for the mere purpose of saving computing time).

Outside of the fringe field regions (or everywhere when $\lambda_E = \lambda_S = 0$) $\vec{B}(X, Y, Z)$ in the magnet is given by

$$B_X = 0$$
$$B_Y = G_0 Z$$
$$B_Z = G_0 Y$$



Figure 35: Quadrupole magnet



Figure 36: Scheme of the longitudinal field gradient G(X).

(OX) is the longitudinal axis of the reference frame (0, X, Y, Z) of **zgoubi**. The length of the element is XL. Trajectories are ray-traced from $-X_E$ to $XL + X_S$, by means of respectively prior and final automatic change of frame.

SEPARA : Wien Filter - analytical simulation

Note : SEPARA is an analytical transport: simulation by stepwise integration may use WIENFILTER.

SEPARA provides an analytic simulation of an electrostatic separator. Input data are the length L of the element, the electric field E and the magnetic field B. The mass m and charge q of the particles are entered by means of the keyword PARTICUL.

The subroutines involved in *SEPARA* solve the following system of three equations with three unknown variables S, Y, Z (while $X \equiv L$), that describe the cycloidal motion of a particle in \vec{E} , \vec{B} static fields (Fig. 37).

$$X = -R\cos\left(\frac{\omega S}{\beta c} + \epsilon\right) - \frac{\alpha S}{\omega \beta c} + \frac{C_1}{\omega}$$
$$Y = R\sin\left(\frac{\omega S}{\beta c} + \epsilon\right) - \frac{\alpha}{\omega^2} - \frac{C_2}{\omega} + Y_0$$
$$Z = S\sin(P_0) + Z_0$$

where, S is the path length in the separator, $\alpha = -\frac{Ec^2}{\gamma}$, $\omega = -\frac{Bc^2}{m\gamma}$, $C_1 = \beta \sin(T_0) \cos(P_0)$ and $C_2 = 1$

 $\beta c \cos(T_0) \cos(P_0)$ are initial conditions. c = velocity of light, $\beta c =$ velocity of the particle, $\gamma = (1 - \beta^2)^{-2}$ and $\tan \epsilon = (C_2 + \frac{\alpha}{\omega})/C_1$. Y_0, T_0, Z_0, P_0 are the initial coordinates of the particle in the **zgoubi** reference frame. Here βc and γ are assumed constant, which is true as long as the change of momentum due to the electric field remains negligible all along the separator.

The option index IA in the input data allows switching to inactive element (thus equivalent to ESL), horizontal or vertical separator. Normally, E, B and the value of β_W for wanted particles are related by

$$B_{[T]} = -\frac{E_{[V/m]}}{\beta_W \cdot c_{[m/s]}}$$



Figure 37: Horizontal separation between a wanted particle, (W), and an unwanted particle, (U). (W) undergoes a linear motion while (U) undergoes a cycloidal motion.

SEXTUPOL : Sextupole magnet (Fig. 38)

The meaning of parameters for SEXTUPOL is the same as for QUADRUPO.

In fringe field regions the magnetic field $\vec{B}(X, Y, Z)$ and its derivatives up to fourth order are derived from the scalar potential approximated to 7th order in Y and Z

$$\begin{split} V(X,Y,Z) &= \left(G(X) - \frac{G''(X)}{16} \left(Y^2 + Z^2\right) + \frac{G'''(X)}{640} \left(Y^2 + Z^2\right)^2\right) \left(Y^2 Z - \frac{Z^3}{3}\right) \\ \text{with } G_0 &= \frac{B_0}{R_0^2} \end{split}$$

The modelling of the fringe field form factor G(X) is described under QUADRUPO, p. 133.

Outside fringe field regions, or everywhere in sharp edge sextupole ($\lambda_E = \lambda_S = 0$), $\vec{B}(X, Y, Z)$ in the magnet is given by

$$B_X = 0$$

$$B_Y = 2G_0 Y Z$$

$$B_Z = G_0 (Y^2 - Z^2)$$



Figure 38: Sextupole magnet

SOLENOID : Solenoid (Fig. 39)

The solenoidal magnet has an effective length XL and a mean radius R_0 (Fig. 39). Its asymptotic field is $B_0 = \mu_0 NI/XL$, namely,

$$\int_{-\infty}^{\infty} B_X(X, r) \, dX \xrightarrow{R_0/XL \to 0} \mu_0 NI, \quad \forall r < R_0$$

In this expression, NI = number of ampere-turn, $\mu_0 = 4\pi 10^{-7}$.



Figure 39: Solenoidal magnet. Note that in **zgoubi** the origin is takan at the entrance EFB, whereas Eq. 6.3.32 is for origin taken at the center.

Field fall-off extents:

The distance of ray-tracing beyond the effective length XL, is X_E upstream of the entrance effective field boundary (located at X = 0 in **zgoubi** reference frame), and X_S downsteam of the exit field boundary (located at $X = X_L$ in **zgoubi** frame). This adding entrance and exit integration extents is transparent to the user, namely, prior to being pushed, a particle is first moved back to $X = -X_E$ by a CHANGREF style change of frame; it is then pushed all the way to $X = X_L + X_S$, whereafter a second change of frame brings it back to the exit effective field boundary at $X = X_L$.

Two methods are available for the computation of the field $\vec{B}(X, r)$ and its derivatives.

Method 1

This is the classical on-axis field model [10]

$$B_X(X, r=0) = \frac{B_0}{2} \left[\frac{XL/2 - X}{\sqrt{(XL/2 - X)^2 + R_0^2}} + \frac{XL/2 + X}{\sqrt{(XL/2 + X)^2 + R_0^2}} \right]$$
(6.3.32)

with origin X = r = 0 taken at the center of the solenoid. This model assumes that the coil thickness is small compared to its mean radius R_0 . The effective magnetic length is

$$L_{mag} \equiv \frac{\int_{-\infty}^{\infty} B_X(X, r < R_0) dX}{B_X(X = r = 0)} = XL \sqrt{1 + \frac{4R_0^2}{XL^2}} > XL$$
(6.3.33)

with in addition

$$B_X(\text{center}) \equiv B_X(X = r = 0) = \frac{\mu_0 NI}{XL\sqrt{1 + \frac{4R_0^2}{XL^2}}} \xrightarrow{R_0 \ll XL} \frac{\mu_0 NI}{XL}$$

The field $\vec{B}(s)$ and its derivatives $d^n \vec{B}(s)/ds^n$ at all (X, Y, Z), as required for pushing a particle (Eqs. 1.2.4, 1.2.8) and possibly its spin (Eqs. 2.1.5, 2.2.2), are extrapolated from eq. 6.3.32, following the method described in section 1.3.1. Note that the model validity limit is $\sqrt{Y^2 + Z^2} = r < R_0$.

(page 321 in PART B)

Method 2

The computation of the radial, $B_r(X, r)$, and axial $B_X(X, r)$ components of the field vector $\vec{B}(X, r)$ (with $r = (Y^2 + Z^2)^{1/2}$) follows the technique described in Ref. [67]. Summarizing: $B_r(X, r)$, and $B_X(X, r)$ are constructed from respectively

$$b_X(X,r) = \frac{\mu_0 NI}{4\pi} \frac{ck}{r} \mathcal{X} \left[K + \frac{r_0 - r}{2r_0} (\Pi - K) \right]$$

$$b_r(X,r) = -\mu_0 NI \frac{1}{k} \sqrt{\frac{r_0}{r}} \left[2(K - E) - k^2 K \right]$$
(6.3.34)

wherein K, E and Π are the three complete elliptic integrals, \mathcal{X} is an X- and XL-dependent quantity, and

$$k = 2\sqrt{r_0 r} / \sqrt{(r_0 + r)^2 + \mathcal{X}^2}; \ c = 2\sqrt{r_0 r} / (r_0 + r)$$

K, E and Π are computed using fast converging algorithms proposed in that very Ref. [67]. Their derivatives are obtained from recursive relations [68], as needed in order to derive the field derivatives at all (X, Y, Z) (up to second order in the present version of the code).

For software developers

Solenoid parameters are read from zgoubi.dat by rsolen.f. Initializations prior to tracking are done in soleno.f. Field computation during tracking is by solenf.f. The initial $\delta X = -X_E$ (prior to pushing a particle) and final $\delta X = -X_S$ (once that particle has reached $X = X_L + X_S$) change of frames to account for field fall-offs, transparent to the user, are performed in transf.f.

SPINR : Spin rotation [69]

SPINR causes spin precession, a local transformation on the spin vector of the particles, as, *e.g.*, in a local helical spin rotator. Two options are available, as follows.

IOPT = 0 inhibits the keyword.

If IOPT = 1 : the precession is defined by its axis, at angle ϕ with respect to **zgoubi**'s X-axis and assumed in the horizontal plane, and by its value, μ .

If IOPT = 2: given the spin precession axis direction ϕ in the (X,Y) plane, the spin precession angle follows a function of the *reference* Lorentz factor :

$$\mu(\gamma) = \left(\frac{B}{B_0}\right)^2 \times \left(C_0 + \frac{C_1}{\gamma} + \frac{C_2}{\gamma^2} + \frac{C_3}{\gamma^3}\right)$$

with B and B_0 normally a nominal and a reference magnetic field value, and C_i empirical coefficients. The reference Lorentz factor corresponds to the reference rigidity *BORO*, as defined for instance with *[MC]OBJET*, possibly updated in the presence of acceleration (see section 7.2, page 206).

SCALING can be used to scale the precession angle μ .

TOSCA : 2-D and 3-D Cartesian or cylindrical mesh field map

TOSCA is dedicated to the reading and treatment of

- 2-D Cartesian or cylindrical mesh mid-plane field maps (mid-plane is assumed anti-symmetry plane, as in an upright multipole),

- 3-D Cartesian or cylindrical mesh field maps.

TOSCA was first installed to read *TOSCA* magnet computer code style of fieldmap output and formatting, hence the name. However the actual origin of the fieldmap, TOSCA or other computer code, does not matter.

TOSCA has been developed over the years to allow reading many different input formats, including 3-D maps given under the form of a series of files, partial 3-D maps with particular symmetry plane(s), etc. In order to select between the many possibilities, two input data, IZ and MOD.MOD2, are used. This is addressed in the following, and table 1, page 142, lists all possibilities as a function of the values given to IZ and MOD.MOD2.

A double-flag, *MOD[.MOD2]*, determines whether a Cartesian mesh (Fig. 40-A or -B) or a Z-axis cylindrical mesh (Fig. 40-C) is used, and the nature and/or form of the field map data set.



Figure 40: Principle 2-D field map mesh as used by TOSCA, and the (O;X,Y) particle coordinate frame. (A), (B): Cartesian mesh in the (X,Y) plane, the mesh increments are ΔX and ΔY ; (A) illustrates a 9-point interpolation grid and (B) a 25-point interpolation grid. (C) : Polar mesh and moving Cartesian frame (O;X,Y) along a reference arc with radius RM, as used during stepwise integration; the mesh increments are $\Delta \alpha$ and ΔR ; In all three cases, during integration the interpolation grid is centered on the mesh node closest to particle location

The total number of field data files to be read is determined by the MOD[.MOD2] flag (see below) and by the parameter IZ that appears in the data list following the keyword. Each of these files contains the field components B_X , B_Y , B_Z on an (X, Y) mesh. IZ = 1 for a 2-D map, and in this case B_X and B_Y are assumed zero all over the map¹¹. For a 3-D map with mid-plane symmetry, described with a set of 2-D maps at various Z, then MOD=0 and $IZ \ge 2$, and thus, the first data file whose name follows in the data list is supposed to contain the median plane field (assuming Z = 0 and $B_X = B_Y = 0$), while the remaining IZ - 1 file(s) contain the IZ - 1 additional planes in increasing Z order. For arbitrary 3-D maps, no symmetry assumed, then MOD=1 and the total number of maps (whose names follow in the data list) is IZ, such that map number [IZ/2] + 1 is the Z = 0 elevation one.

The field map data file has to be filled with a format that fits the *FORTRAN* reading sequence. The following is an instance, details and possible updates are to be found in the source file ' fmapw.f':

```
DO 1 K = 1, KZ

OPEN (UNIT = NL, FILE = FNAME, STATUS = 'OLD' [,FORM='UNFORMATTED'])

DO 1 J = 1, JY

DO 1 I = 1, IX

IF (BINARY) THEN

READ(NL) Y(J), Z(K), X(I), BY(J,K,I), BZ(J,K,I), BX(J,K,I)

ELSE

READ(NL,100) Y(J), Z(K), X(I), BY(J,K,I), BZ(J,K,I), BX(J,K,I)

100

FORMAT(1X,6E11.2)

ENDIF

1 CONTINUE
```

IX (JY, KZ) is the number of longitudinal (transverse horizontal, vertical) nodes of the 3-D uniform mesh. For letting **zgoubi** know in case these are binary files, FNAME must begin with 'B_' or 'b_'.

Other *MOD[.MOD2]* cases in addition to the above, are listed in table 1. The *FORTRAN* subroutine fmapw.f and its entries FMAPR, FMAPR2 can be looked up for more details, in particular regarding the formatting of the field map data file(s).

Once the field map(s) reading is completed, the field $\vec{B} = (B_X, B_Y, B_Z)$ is normalized by means of *BNORM* in a similar way as in *CARTEMES*. As well the coordinates X and Y (and Z in the case of 3-D field maps) are normalized by the X-[, Y-, Z-]NORM coefficient (useful to convert to centimeters, the working units in **zgoubi**).

At each step of the trajectory of a particle inside the map, the field and its derivatives are calculated as follows :

- in the case of a 2-D map, by means of a second or fourth order polynomial interpolation, depending on *IORDRE (IORDRE = 2, 25 or 4)*, as for *CARTEMES*,

- in the case of a 3-D map, by means of a second order polynomial interpolation with a $3 \times 3 \times 3$ -point parallelepipedic grid, as described in section 1.4.4.

In the Cartesian mesh case, entrance and/or exit integration boundaries between which the trajectories are integrated in the field may be defined, in the same way as in *CARTEMES*.

A '*TITL*' (a line of comments) is part of the arguments of the keyword *TOSCA*. It allows introducing necessary field map handling data, or some options, for instance :

 \diamond including 'HEADER N' allows specifying the number of header lines (N) at the top of the field map file. In the case of cylindrical field maps one line is necessary ($N \ge 1$) to indicate the reference radius in particular (but also the mesh size, etc., lookup 'HEADER' in fmapw.f in case of doubt),

◊ including 'FLIP' in TITL causes the field map to be X-flipped,

 \diamond including 'ZroBXY' forces $B_X = B_Y = 0$ at all Z=0 nodes of the field map mesh (only applies with MOD=15 and MOD=24),

¹¹Use MAP2D in case non-zero B_X , B_Y are to be taken into account in a 2-D map.

Table 1: The various IZ, MOD and MOD2 possibilities, when using TOSCA.

IZ : number of nodes of the *complete* field map along the Z direction (IZ=1 for 2-D)

MOD, MOD2 : determine the coordinate system, symmetries, reading format and column sequence, etc.

NF : number of field map input data files to be declared. Always include mid-plane map.

Expected columns : formatting of the coordinates and field data columns in the field map data file(s)

'Exemple' example folder : examples of zgoubi runs using field maps can be found in the subfolders of

zgoubi-code/exemples/KEYWORDS/TOSCA/cartesian (case MOD≤19) or

 $zgoubi-code/exemples/KEYWORDS/TOSCA/cylindrical \ (case \ MOD{\geq}20).$

The rightmost column below indicates the subfolder of concern, following (IZ, MOD, MOD2) options of interest.

$\text{MOD} \leq 19$: Cartesian mesh

IZ	MOD	.MOD2		NF	Expected columns	Example folder
1	0, 1	none or .1, .2, .3	2-D map. File contains $B_Z(X, Y) _{Z=0}$, mid-plane antisymmetry assumed. Several different reading formats (see fmapw.f/fmapr3).	1	Y, Z, X, BY, BZ, BX	IZ-MODMOD2_1-0-none/ (GSI KAOS spectrometer)
1	3	none or .1	2-D map. Used for AGS main magnet. If MOD2=1, $B_Z(X, Y, Z = 0)$ field is perturbed by $(1 + n_1 Y + n_2 Y^2 + n_3 Y^3)$ factor.	1	Special - see example	AGS/usingMainMagnetsMaps (AGS with main magnet maps)
1	15	.1 – .4	2-D map. Up to 4 files to be combined linearly into a new map : field at all node of new map is $\vec{B} = \sum_{i=1}^{i=MOD2} a_i \vec{B}_i$. Mid-plane antisymmetry is assumed : each file has to contain $B_Z(X, Y, Z = 0)$.	1 to 4	Y, Z, X, BY, BZ, BX	IZ-MODMOD2_1-1514 (EMMA FFAG cell)
>1	0	none	3-D map. Files span upper half of magnet, one per $(X,Y) _{0 \le Z \le Z_{max}}$ plane including median plane, mid-plane antisymmetry assumed.	1+IZ/2	Y, Z, X, BY, BZ, BX	IZ-MODMOD2_gt1-0-none/ (GSI KAOS spectrometer)
$\overset{\text{odd,}}{\geq 3}$	1	none	3-D map. Files span full magnet volume, one file per (X,Y) plane, no symmetry assumed.	IZ	Y, Z, X, BY, BZ, BX	IZ-MODMOD2_gt1-1-none/ (AGS warm helix snake)
>1	12	none	3-D map. Single file, upper half of magnet, mid-plane antisymmetry assumed.	1		
>1	12	.1	3-D map. Single file, whole magnet volume, no symmetry assumed.	1	Y, Z, X, BY, BZ, BX	IZ-MODMOD2_gt1-121/ (AGS warm helix snake)
>1	12	.2	3-D map. Single file, 1/8th of the magnet, symmetry wrt. $(X, Y)_{Z=0}, (X, Z)_{Y=0}, (Y, Z)_{X=0}$ planes.	1		
odd, ≥ 3	15	.1 – .4	3-D map. Up to 4 files to be combined linearly into a new map, field at all node of new map is $\vec{B} = \sum_{i=1}^{i=MOD2} a_i \vec{B}_i$. Each file has to contain $B_{X_i,Y_iZ}(X, Y, Z)$ data over <i>IZ</i> equally <i>Z</i> -spaced (<i>X</i> , <i>Y</i>) planes (no symmetry assumed).	1 to 4		
odd, ≥ 3	16	.1 – .4	3-D map. Fields from up to 4 maps to be combined linearly into a new field value at particle location, $\vec{B} = \sum_{i=1}^{i=MOD2} a_i \vec{B}_i$. Each file has to contain $B_{X,Y,Z}(X, Y, Z)$ data over <i>IZ</i> equally <i>Z</i> -spaced (X, Y) planes.	1 to 4	UNDER DEVELOPMENT	
MOD	≥ 20 : Cyli	ndrical mesh				
IZ	MOD	.MOD2				
1	25	.1 – .4	2-D map. Up to 4 files to be combined linearly into a new map : at all node of new map $\vec{B} = \sum_{i=1}^{i=MOD^2} a_i \vec{B}_i$. Each file contains mid-plane $B_Z(X, Y, Z = 0)$ data, mid-plane antisymmetry is assumed.	1 to 4	Y, Z, X, BY, BZ, BX	IZ-MODMOD2.1-1514 (EMMA FFAG cell)
>1	20, 21		3-D map. Single file. MOD=20 : $1/4$ magnet, cylindrical symmetry with respect to (Y,Z) plane and antisymmetry wrt (X,Y) plane. MOD=21 : another type of symmetry (to be documented - see fmapw.f).	1	$Y(r, \theta), Z, X(r, \theta),$ BY, BZ, BX	IZ-MODMOD2_gt1-20 (KEK 150 MeV FFAG)
odd, ≥ 1	22, 23	.1 – .4	2-D or 3-D map. Mid-plane antisymmetry assumed. Up to 4 files can be combined linearly into a new one; each file is $Z \ge 0$ half-magnet. Field at all node of new map is $\vec{B} = \sum_{i=1}^{i=MOD2} a_i \vec{B}_i$. Each file has to contain $B_{X,Y,Z}(X, Y, Z)$ data over (<i>IZ</i> +1)/2 equally <i>Z</i> -spaced (<i>X</i> , <i>Y</i>) planes. MOD=23 : special, test code (see fmapw.f).	1 to 4	$\begin{split} \mathbf{Y}(r,\theta) &= r\cos\theta, \mathbf{Z}, \\ \mathbf{X}(r,\theta) &= r\sin\theta, \\ \mathbf{BY}, \mathbf{BZ}, \mathbf{BX} \end{split}$	IZ-MODMOD2.gt1-2214 (ERIT FFAG)
odd, ≥ 3	24		3-D map, full volume. No symmetry assumed. The file contains $B_{X,Y,Z}(X,Y,Z)$ data over <i>IZ</i> equally <i>Z</i> -spaced (X, Y) planes.	1	$\theta, R, Z, B_{\theta}, BR, BZ$	

 \diamond 'RHIC_helix' can be mentionned as part of the 'TITL' string. That concerns RHIC snakes and rotators field maps [70]. In that case BNORM (assuming SCALING is not used, see below) will no longer just be a scaling factor to the field read from the map, instead it will be the coil current (in Amps); the effecive field at particle location will be derived from the OPERA map accounting for a normalization to the measured magnetic field (measured B(I) data used for that are hard-coded in the program toscac.f) [70]. The coefficient a(1) in mode MOD.MOD2=15.1 can be used to normalize the field map (namely, $a(1) = 1/B_{max}$ with B_{max} the maximum field value on helix axis). If SCALING is used, then actually BNORM×SCAL (not just BNORM) has to represent the coil current value, in Amps; note also: in that case, sign (BNORM×SCAL) == sign(BNORM), the sign of SCAL is not taken into account.

An example of the two modes of utilization (with or without "RHIC_helix" flag) is given in PART. B, p. 334.

TRANSMAT : Matrix transfer

TRANSMAT performs a second order transport of the particle coordinates in the following way

$$X_i = \sum_j R_{ij} X_j^0 + \sum_{j,k} T_{ijk} X_j^0 X_k^0$$

where, X_i stands for any of the current coordinates Y, T, Z, P, path length and momentum dispersion, and X_i^0 stands for any of the initial coordinates. $[R_{ij}]$ ($[T_{ijk}]$) is the first order (second order) transport matrix as usually involved in second order beam optics [40]. Second order transport is optional. The length of the element represented by the matrix may be introduced for the purpose of path length updating.

Note : *MATRIX* delivers $[R_{ij}]$ and $[T_{ijk}]$ matrices in a format suitable for straightforward use with *TRANS-MAT*.
TRAROT : Translation-Rotation of the reference frame

UNDER DEVELOPMENT. Check before use.

This procedure performs translation and rotation of the local **zgoubi** frame. It can be used for instance for skewing multipoles.

Relationship to spin tracking, particle decay or gas-scattering may not be fully installed, to be checked before use.

UNDULATOR : Undulator magnet

UNDULATOR magnet. UNDER DEVELOPMENT.

UNIPOT : Unipotential cylindrical electrostatic lens

The lens is cylindrically symmetric about the X-axis.

The length of the first (resp. second, third) electrode is X1 (resp. X2, X3). The distance between the electrodes is D. The potentials are V1 and V2. The inner radius is R_0 (Fig. 41). The model for the electrostatic potential along the axis is [71]

$$V(x) = \frac{V2 - V1}{2\omega D} \left[\ln \frac{\frac{\omega \left(x + \frac{X2}{2} + D\right)}{R_0}}{\frac{\omega \left(x + \frac{X2}{2}\right)}{R_0}} + \ln \frac{\frac{\omega \left(x - \frac{X2}{2} - D\right)}{R_0}}{\frac{\omega \left(x - \frac{X2}{2}\right)}{R_0}} \right]$$

(x = distance from the center of the central electrode; $\omega = 1,318$; $\cosh = \text{hyperbolic cosine}$), from which the field $\vec{E}(X, Y, Z)$ and its derivatives are deduced following the procedure described in section 1.3.1.

Use *PARTICUL* prior to *UNIPOT*, for the definition of particle mass and charge.

The total length of the lens is X1 + X2 + X3 + 2D; stepwise integration starts at entrance of the first electrode and terminates at exit of the third one.



Figure 41: Three-electrode cylindrical unipotential lens.

VENUS : Simulation of a rectangular shape dipole magnet

VENUS is dedicated to a 'rough' simulation of SATURNE Laboratory's VENUS dipole. The field B_0 is constant inside the magnet, with longitudinal extent XL and transverse extent $\pm YL$; outside these limits, $B_0 = 0$ (Fig. 42).



Figure 42: A scheme of a few trajectories through VENUS rectangular dipole.

VFFA : Simulation of a VFFA dipole, or series of

VFFA simulates a vertical FFAG dipole, or a series of nearby dipoles (Fig. 43).

TO BE DOCUMENTED FURTHER.

Examples, including input data files, are available at

https://sourceforge.net/p/zgoubi/code/HEAD/tree/trunk/exemples/FFAG/VFFA/



Figure 43: Multiple-dipole VFFA design parameters in zgoubi formalism.

WIENFILT : Wien filter

(page 344 in PART B)

WIENFILT simulates a Wien filter, with transverse and orthogonal electric and magnetic fields \vec{E}_Y , \vec{B}_Z (index KHV=1) or \vec{E}_Z , \vec{B}_Y (index KHV=1) (Fig. 37). It must be preceded by PARTICUL for the definition of particle mass and charge.

The length XL of the element is the distance between its entrance and exit EFBs. The electric and magnetic field intensities E_0 and B_0 in the central, uniform field region, normally satisfy the relation

$$B_0 = -\frac{E_0}{\beta_W c}$$

for the selection of "wanted" particles of velocity $\beta_W c$. Ray-tracing in field fall-off regions extends over a distance $X_E(X_S)$ beyond the entrance (exit) EFB by means of prior and further automatic change of frame. Four sets of coefficients λ , $C_0 - C_5$ allow the description of the entrance and exit fringe fields outside the uniform field region, following the model [46]

$$F = \frac{1}{1 + \exp(P(s))}$$

where P(s) is of the term

$$P(s) = C_0 + C_1\left(\frac{s}{\lambda}\right) + C_2\left(\frac{s}{\lambda}\right)^2 + C_3\left(\frac{s}{\lambda}\right)^3 + C_4\left(\frac{s}{\lambda}\right)^4 + C_5\left(\frac{s}{\lambda}\right)^5$$

and s is the distance to the EFB. When fringe fields overlap inside the element (*i.e.*, $XL \le X_E + X_S$), the field fall-off is expressed as

$$F = F_E + F_S - 1$$

where $F_E(F_S)$ is the fringe field factor for the entrance (exit) EFB.

If $\lambda_E = 0$ ($\lambda_S = 0$) for either the electric or magnetic component, then both are considered as sharp edge fields and $X_E(X_S)$ is forced to zero (for the purpose of saving computing time). In this case, the magnetic wedge angle vertical first order focusing effect is simulated at entrance and exit by a kick $P_2 = P_1 - Z_1 \tan(\epsilon/\rho)$ applied to each particle (P_1 , P_2 are the vertical angles upstream and downstream the EFB, Z_1 the vertical particle position at the EFB, ρ the local horizontal bending radius and ϵ the wedge angle experienced by the particle ; ϵ depends on the horizontal angle T). This is not done for the electric field, however it is advised not to use a sharp edge electric dipole model since this entails non symplectic mapping, and in particular precludes accounting for momentum effects of the non zero longitudinal electric field component.

YMY : Reverse signs of Y and Z reference axes

(page 345 in PART B)

YMY performs a 180° rotation of particle coordinates with respect to the X-axis, as shown in Fig. 44. This is done by means of a change of sign of Y and Z axes, and therefore coordinates, as follows

$$Y2 = -Y1$$
, $T2 = -T1$, $Z2 = -Z1$ and $P2 = -P1$

Also performs 180° X-rotation of spins.



Figure 44: The use of YMY in a sequence of two identical dipoles of opposite signs.

6.4 Functional Options

A series of options are available which allow the control of various of the procedures and functionalities of the code.

Some of these options are normally declared right after the object definition, for instance

- SPNTRK : switch-on spin tracking,

- *PARTICUL* to declare particle mass and charge, if for instance tracking in electric fields, or tracking spin, or in presence of synchrotron radiation energy loss simulations,

some may appear further down in the optical sequence (in zgoubi.dat), for instance

- MCDESINT : switch-on in-flight decay, could be after a target,

- REBELOTE : for multi-turn tracking, including an extraction line section for instance,

others may normally be declared at the end of zgoubi.dat data pile, for instance

- *END* : end of a problem,

- FIT : fitting procedure - can also appear before REBELOTE

GETFITVAL may appear *before* the object definition (keyword [MC]OBJET, normally the first keyword in **zgoubi** optical sequence). This is the case if variables prior saved following a '*FIT*[2]' procedure and then read back using *GETFITVAL*, happen to belong in the [MC]OBJET keyword data list.

SYSTEM as well, may appear anywhere in the optical sequence.

BINARY : BINARY ↔ FORMATTED data converter

This procedure translates field map data files from "BINARY" to "FORMATTED" – in the FORTRAN sense, or the other way.

The keyword is followed by, next data line,

NF[.J], NCOL, NHDR

the number of files to be translated [READ format option, a single digit integer, optional], number of data columns in the file, number of header lines in the file.

Fortran READ format, case of formatted input file :

If J is not given, the NCOL arrangement should be consistent with the following FORTRAN READ statement :

READ (unit=ln,*) (X7(I),I=1,NCOL)

If J = 1, NCOL should be consistent with the following FORTRAN READ statement : READ (unit=ln, fmt='(1x, ncol*E11.2)') (X7(I), I=1, NCOL)

Fortran READ format, case of formatted input file :

Data are expected to have been recorded under the form of Ncol column rows.

Then follow, line by line, the NF names of the files to be translated.

Iff a file name begins with the prefix "B_" or "b_", it is assumed "binary", and hence converted to "formatted", and given the same name after suppression of the prefix "B_" or "b_". Conversely, *iff* the file name does not begin with "B_" or "b_", the file is presumed "formatted" and hence translated to "binary", and is given the same name after addition of the prefix "b_".

In its present state, the procedure *BINARY* only supports a limited number of read/write formats. Details concerning I/O formatting can be found in the *FORTRAN* file 'binary.f'.

END or FIN : End of input data list

The end of a problem, or of a set of several problems stacked in the data file, should be stated by means of the keywords *FIN* or *END*.

Any information following these keywords will be ignored.

In some cases, these keywords may cause some information to be printed in zgoubi.res, for instance when the keyword *PICKUPS* is used.

ERRORS : Injecting errors in optical elements

(page 273 in PART B)

UNDER DEVELOPMENT

The keyword *ERRORS* allows injecting diverse types of errors in optical elements, including field and positionning defects. Uniform and Gaussian distribution laws are available.

Optical elements concerned can be discriminated using one or both of their labels.

ERRORS is under development, functionalities at the moment are the following :

MULTIPOL can be injected the following random defects:

Field defect on any one of its 2-pole (dipole) to 20-pole component. The defect can be relative (to the current field value) or absolute (adds to the current field value);

X-rotation of any of the 20 poles, the defect adds-up to possibly existing skew angle of pole;

Z-offset, independently of KPOS value; the defect adds-up to possibly existing Z-offset.

TOSCA can be injected a field defect that applies to the field map as a whole. The defect can be relative (to the current field value) or absolute (adds to the current field value).

Some rules :

- if *REBELOTE* is used in multi-turn mode (*i.e.*, its K argument value is 99), then the defect series, generated upon first pass, applies at all subsequent passes, by default.

Note: one might want instead to simulate a N-cell ring by repeating N times a cell subset, using *REBELOTE*. In which case defects of random type in that cell subset should be changed at each pass over the first N passes - and that N-cell sequence repeat identically beyond that. This possibility is not implemented, it would require modification in errors.f program.

FIT, FIT2 : Fitting procedure

(page 273 in PART B)

The keywords *FIT*, *FIT2* allow the automatic adjustment of up to 20 variables, for fitting up to 20 constraints.

FIT was implemented in 1985, drawn from the matrix transport code BETA [40]. *FIT2* is a simplex method (Nelder-Mead method), it has been implemented in 2007 [41]. One or the other may converge faster, or may have some advantages/disadvantages, depending on the problem.

Any physical parameter of any element in zgoubi.dat optical sequence may be varied. Examples of available constraints are, amongst others :

- trajectory coordinates in the F(J, I) array, I = particle number, J = coordinate number = 1 to 7 for respectively D, Y, T, Z, P, S =path length, time ;

- spin coordinates ;

- any of the 6×6 coefficients of the first order transport matrix $[R_{ij}]$ as defined in the keyword MATRIX;
- any of the $6 \times 6 \times 6$ coefficients of the second order array $[T_{ijk}]$ as defined in MATRIX;
- any of the 4×4 coefficients of the beam σ -matrix
- transmission efficiency of an optical channel.

- tunes $\nu_{Y,Z}$ and periodic betatron functions $\beta_{Y,Z}$, $\alpha_{Y,Z}$, $\gamma_{Y,Z}$, as computed in the coupled hypothesis [42].

A full list of the constraints available is given in the table page 161.

FIT, FIT2 are compatible with the use of (*i.e.*, can be encompassed in) *REBELOTE* for successive fitting trials using various sets of parameters (see pp. 163 176).

VARIABLES

The first input data in *FIT*[2] is the number of variables *NV*. A variable is defined by a line of data comprised of

IR = number of the varied element in the optical sequence

IP = number of the physical parameter to be varied in this element

XC = coupling parameter. Normally XC = 0. If $XC \neq 0$, coupling will occur (see below) and of the allowed variation range, either under the form

DV = allowed relative range of variation of the physical parameter IP or under the form

[Vmin, Vmax] = allowed interval of variation of the physical parameter IP

Numbering of the Elements (IR) :

The elements (*i.e.*, keywords *DIPOLE*, *QUADRUPO*, etc.) as read by **zgoubi** in the zgoubi.dat sequence are assigned a number. which follows their sequence in the data file. It is that very number, *IR*, that the FIT[2] procedure uses. A simple way to get *IR* once the zgoubi.dat file has been built, is to do a preliminary run, since the first thing **zgoubi** does is copy the sequence from zgoubi.dat into the result file zgoubi.res, with all elements numbered.

Numbering of the Physical Parameters (IP) :

All the data that follow a keyword are numbered - except for SCALING, see below.

With most of the keywords, the numbering follows the principle hereafter :

Input data	Numbering for FIT
'KEYWORD'	
first line	1, 2, 3,, 9
second line	10, 11, 12, 13,, 19
this is a comment	a line of comments is skipped
next line	20, 21, 22,, 29
and so on	

The examples of QUADRUPO (quadrupole) and TOSCA (Cartesian or cylindrical mesh field map) are as follows. Input data Numbering for FIT

L	8
'OUADRUPO'	
IL	1
XL, R_0, B	10, 11, 12
X_E, λ_E	20, 21
NCE, $C_0, C_1, C_2, C_3, C_4, C_5$	30, 31, 32, 33, 34, 35, 36
X_S, λ_S	40, 41
$NCS, C_0, C_1, C_2, C_3, C_4, C_5$	50, 51, 52, 53, 54, 55, 56
XPAS	60
KPOS, XCE, YCE, ALE	70, 71, 72, 73
ıt data	Numbering for FIT
SCA'	
IL	1, 2
ORM, X- [, Y-, Z-]NORM	10, 11 [, 12, 13]
	This is text
IY, IZ, MOD	20, 21, 22, 23
ME	This is text
$A, B, C [A', B', C', \text{etc. if } ID \ge 2]$	30, 31, 32, 33 [34, 35, 36 [, 37, 38, 39] i
DRE	40
S	50

Inpu

'TOSCA'	
IC, IL	1, 2
BNORM, X- [, Y-, Z-]NORM	10, 11 [, 12, 13]
TIT	This is text
IX, IY, IZ, MOD	20, 21, 22, 23
FNAME	This is text
$ID, A, B, C [A', B', C', \text{etc. if } ID \ge 2]$	30, 31, 32, 33 [34, 35, 36 [, 37, 38, 39] if $ID \ge 2$]
IORDRE	40
XPAS	50
if KPOS=1 :	
KPOS, XCE, YCE, ALE	60,61,62,63
if KPOS=2 :	
KPOS	60
KPOS, XCE, YCE, ALE	70,71,72,73

A different numbering, fully sequential, has been adopted in the following elements :

AIMANT, DIPOLE, EBMULT, ELMULT, MULTIPOL.

It is illustrated here after in the case of MULTIPOL and DIPOLE-M.

Input data	Numbering for FIT
'MULTIPOL'	
0	1
365.760 10.0 7.5739 1.4939 0.0 0.0 0.0 0.0 0.0 0.0 0.0 0.0 0.0	2, 3, 4, 5,, 13
10.0 4.0 0.80 0.0 0.0 0.0 0.0 0. 0. 0. 0. 0.	14, 15,, 24
$NC, C_0, C_1, C_2, C_3, C_4, C_5$	25, 26, 27, 28, 29, 30, 31
10.0 4.0 0.80 0.0 0.0 0.0 0.0 0. 0. 0. 0. 0. 0.	32, 33,, 42
$NC, C_0, C_1, C_2, C_3, C_4, C_5$	43, 44,, 49
0. 0. 0. 0. 0. 0. 0. 0. 0. 0. 0.	50, 51,, 59
step size	60 [and 61, 62 reserved]
KPOS, XCE, YCE, ALE	63, 64, 65, 66

Input data	Numbering for FIT
'DIPOLE-M'	
NFACE, IC, IL	1, 2, 3
IAMAX, IRMAX	4, 5
B_0, N, B, G	6, 7, 8, 9
AT, ACENT, RM, RMIN, RMAX	10, 11, 12, 13, 14
λ , ξ	15,16
$NC, C_0, C_1, C_2, C_3, C_4, C_5$, shift	17, 18, 19, 20, 21, 22, 23, 24
$\omega, \theta, R_1, U_1, U_2, R_2$	25, 26, 27, 28, 29, 30
etc.	

Parameters in *SCALING* also have a sequential numbering, yet some positions are skipped, this is illustrated in the example hereafter which covers all possible working modes of *SCALING* (all details regarding the numbering can be found in the *FORTRAN* subroutine rscal.f):

Input data	Numbering in FTT	Quantities to be varied
'SCALING'		(see SCALING for details)
$\begin{bmatrix} 1 & 9 \end{bmatrix}$	1 2	Non relevant
AGSMM *AF *BF	1 2	Keywords concerned, their labels
-1 3 12 1. 13 1. 14 1.	3 4 5	dB1, dB2, dB3 parameters in AGSMM
7 2135	6	Field factor
1	7	Timing
AGSMM *AD *BD	1	Thing
-1 3 12 1. 13 1. 14 1.	8 9 10	
7.2135	11	
1	12	
AGSMM *CF	12	
-1 3 12 1. 13 1. 14 1.	13 14 15	
7.2135	16	
1	17	
AGSOUAD OH_*	1,	
3		
0.605 0.77 0.879	18 19 20	Field factor
1 2000 10000	21 22 23	Timing
AGSQUAD QV_*		-
3		
0.587 0.83 0.83	24 25 26	
1 2000 10000	27 28 29	
MULTIPOL		General rule. Precedes labeled cases if any.
-1	30	(meaningless)
0.72135154291	31	
1	32	(meaningless)
MULTIPOL COH1		
1.10		No numbering if 1.10 type of option
./Csnk3D/bump_centered.scal		
1 2 MULTIPOL COH2		
1.10		
./Csnk3D/bump_centered.scal		
14		
MULTIPOL KICKH KICKV		
2		
0.1 0.3	33 34	Field factor
1 10	35 36	Timing

Coupled Variables (XC)

Coupling a variable parameter to any other parameter in the optical sequence is possible. This is done by giving XC a value of the form *int.jnt* (which can be either negative or positive, see below) where the integer part "int" is the number of the coupled element in the optical sequence (equivalent to IR, see above), and the decimal part "jnt" is the number of its parameter of concern (equivalent to IP, see above). For example, XC = 20.10 or -20.10 is a request for coupling with the parameter number 10 of element number 20 of the optical sequence, XC = 20.100 or -20.100 is a request for coupling with the parameter number 100 of element 20.

An element of the optical sequence which is coupled (by means of $XC \neq 0$) to a variable declared in the data list of the *FIT[2]* keyword, needs not appear as one of the *NV* variables in that data list (this would amount to redundant information).

XC can be either positive or negative:

- if XC > 0, the sum of the two parameters stays constant [for example, two drifts in a quadrupole doublet can be coupled so that their total length stays constant (equal to its value before *FIT[2]* starts), while both drift lengths are varied];

- if XC < 0, the difference between the two parameters stays constant [for example, two homologous quadrupoles in a triplet can be coupled and have their fields stay equal while varied (assuming they are equal before *FIT*[2] starts)].

Coupled Variables using SCALING

Because it applies a scaling factor to families of optical elements (as determined by their keyword and possible *LABEL1*, *LABEL2*), *SCALING* can be used to couple FIT variables.

Variable Variation Range

There are two ways to define the allowed range for a variable, as follows.

(i) DV : For a variable (parameter number IP under some keyword) with initial value v, the FIT[2] procedure is allowed to explore the range $v \times (1 \pm DV)$.

(i) $[v_{min}, v_{max}]$: This specifies the allowed interval of variation.

CONSTRAINTS

The next input data in FIT[2] is the number of constraints, NC. A list of the available constraints is given in the table page 161; adding or changing a constraint resorts to the FORTRAN file ff.f.

Each constraint is defined by the following list of data :

IC[.IC2]	=	type of constraint (see table p. 161).
I, J	=	constraint (<i>i.e.</i> , R_{ij} , determinant, tune ; T_{ijk} ; σ_{ij} ; trajectory $\#I$ and coordinate $\#J$)
IR	=	number of the keyword at the exit of which the constraint applies ; instead of numeral, can also be '#End', so the constraint applies at the last keyword preceeding ' <i>FIT</i> [2]'
V	=	desired value of the constraint
W	=	weight of the constraint (smaller W for higher weight)
NP		number of additional parameters ($NP = 0$ unless otherwise specified in Tab. page 161); NP values PR_{1-NP} follow, defining the constraint

IC=0: The coefficients σ_{11} (σ_{33}) = horizontal (vertical) beta values and σ_{22} (σ_{44}) = horizontal (vertical) derivatives ($\alpha = -\beta'/2$) are obtained by transport of their initial values at line start as introduced using for instance *OBJET*, *KOBJ=5.1*.

IC=0.1: Beam parameters : $\sigma_{11} = \beta_Y$, $\sigma_{12} = \sigma_{21} = -\alpha_Y$, $\sigma_{22} = \gamma_Y$, $\sigma_{33} = \beta_Z$, $\sigma_{34} = \sigma_{43} = -\alpha_Z$, $\sigma_{44} = \gamma_Z$; periodic dispersion : $\sigma_{16} = D_Y$, $\sigma_{26} = D'_Y$, $\sigma_{36} = D_Z$, $\sigma_{46} = D'_Z$, all quantities derived by assuming periodic optical sequence and identifying the first order transport matrix with the form $Icos\mu + Jsin\mu$.

IC=1, 2: The coefficients R_{ij} and T_{ijk} are calculated following the procedures described in *MATRIX*, option *IFOC* = 0. The fitting of the $[R_{ij}]$ matrix coefficients supposes the tracking of particles with paraxial coordinates, normally defined using *OBJET* option *KOBJ* = 5 or 6.

IC=3: If $1 \le I \le IMAX$ then the value of coordinate type J (J = 1, 6 for respectively D, Y, T, Z, P, S) of particle number I ($1 \le I \le IMAX$) is constrained. However I can take special meaning, as follows.

I = -1: the constraint is the average value of coordinate of type J over particles $[I_1, I_2]$,

I = -2: the constraint is the maximum value of coordinate of type J,

I = -3: the constraint is the distance between particles $I_1 - I_2$ (step ΔI).

I = -4: take the average of the F(J, i) coordinate (J=1-7 for D,Y,T,Z,P,S,time) over (I2 - I1 + 1) particles in the range i = I1 - I2, get it at N different pickup locations $PU_1, PU_2, ..., PU_N$. The constraint is, minimizing the distance between these averages, $Dist [< F(J, i) >_{i=I1,I2}]_{PU_{1-N}}$ (Ex. : minimize the difference between PU records, for a series of PUs along a beamline). If the number of locations is 997 (*i.e.*, N+2=999) then all PUs upstream of IR are accounted for. This constraint requires declaring pick-ups using *PICKUPS* keyword, their locations are as numbered in the optical sequence in zgoubi.res.

IC=3.1: Absolute value of the difference between local and initial *J*-coordinate of particle *I* (convenient *e.g.* for closed orbit search).

IC=3.2: Absolute value of the sum of the local and initial J-coordinate of particle number I.

IC=3.4: Absolute value of the difference between local J-coordinates of particles respectively I and K.

IC=3.5: Difference between local J-coordinates of particles respectively I and K, relative to J-coordinate of particle K.

IC=4: The coefficients σ_{11} (σ_{33}) = horizontal (vertical) beta values and σ_{22} (σ_{44}) = horizontal (vertical) derivatives ($\alpha = -\beta'/2$) are derived from an ellipse match of the current particle population (as generated for instance using *MCOBJET*, *KOBJ=3*).

The fitting of the $[\sigma_{ij}]$ coefficients supposes the tracking of a relevant population of particles within an appropriate emittance.

IC=5 : The constraint value is the ratio of particles (over *IMAX*). Three cases possible :

I = -1, ratio of particles still on the run.

I = 1, 2, 3, maximization of the number of particles encompassed within a phase-space ellipse with given emittance value (I=1-3 for respectively Y, Z, D). Then, NP=1, followed by the emittance value. The center and shape of the ellipse are determined by an rms match to the position and shape of the particle distribution.

I = 4, 5, 6, same as previous case, except for the surface of the ellipse, taken to be the surface of *rms* matched ellipse to the distribution. Thus *NP*=0.

IC=7 series : The constraint applies *inside* the optical element with number *IR*. This constraint may be (possibly combinations of) the minimum or maximum values of the coordinates or fields, or the value of field integrals, along the particle trajectory over the extent $[X_0, X_{LIM}]$ of the element (regardless of the transverse trajectory coordinates Y and Z). Parameters $PR_2 = X_1$ and $PR_3 = X_2$ impose that the constraint only be applied within a limited interval $[X_1, X_2] \subset [X_0, X_{LIM}]$ inside the element. Note in that latter case, the element extent $[X_0, X_{LIM}]$, in proper units, can be determined from a preliminary run with *IL*=1 (see Sec. 7.6, p. 207).

IC=7.1: Minimum or maximum value as reached by coordinate J of particle number I.

IC=7.2: Maximum minus minimum of the value of coordinate J of particle number I.

IC=7.3: Maximum plus minimum of the value of coordinate J of particle number I.

IC=7.6: Minimum ($PR_1 = 1$) or maximum ($PR_1 = 2$) value as reached by the X, Y or Z component of the field along the trajectory of particle number I.

IC=7.7: Maximum minus minimum of the values taken by the X, Y or Z component of the field along the trajectory of particle number I.

Type of		Recommended [MC]OBJET					
constraint	IC I J Constraint (all are defined and managed in ff.f)		Constraint (all are defined and managed in ff.f)	Addition NP	nal parameter(s) Param. values, $pr_1 - pr_{NP}$	(not an exclusive list) ; comments	
Transported σ -matrix $(\sigma(s) = T\sigma(0)\tilde{T})$	0	1-6	1-6	$\sigma_{IJ} \ (\sigma_{11} = \beta_Y, \sigma_{21, 12} = \alpha_Y, \text{etc.})$			OBJET[KOBJ=5.1]
Periodic σ -matrix ($\sigma = I \cos \mu + J \sin \mu$), tunes ($N = 1 - 9$ for MATRIX block 1-9)	$\begin{array}{c} 0.\mathrm{N} \\ (N \leq 9) \end{array}$	1-6 7 8 9 10	$1-6 \ [0,1] \ [0,1] \ [-1,1] \ [-1,1]$	$ \begin{array}{c c} 6 & \sigma_{IJ} & (\sigma_{11} = \cos \mu_Y + \alpha_Y \sin \mu_Y, \text{etc.}) \\ 1] & \mu_Y / 2\pi \\ 1] & \mu_Z / 2\pi \\ ,1] & \cos(\mu_Y) \\ ,1] & \cos(\mu_Z) \end{array} $			$OBJET[KOBJ=5] if$ $N = 1,$ $OBJET[KOBJ=5.N]$ $if N \ge 2.$
First order transport coeffs. & determinants.	1	$ \begin{array}{r} 1-6 \\ 7 \\ 8 \end{array} $	1-6 j j	Transport coeff. R_{IJ} $j \neq 8$: YY-determinant ; j=8: YZ-det. $j \neq 7$: ZZ-determinant ; j=7: ZY-det.			OBJET[KOBJ=5]
Chromas.	1.1	7 8	7 8	$dQ_Y / dp/p \ dQ_Z / dp/p$			OBJET[KOBJ=5.2] or KOBJ=5.3
Second order transport coeffs.	2	1 - 6	11-66 Transport coeff. $T_{I,j,k}$ ($j = [J/10], k = J - 10[J/10]$)				OBJET[KOBJ=6]
Trajectory coordinates	3	1 - IMAX -1	$1 - 7 \\ 1 - 7$	$F(J,I) < F(J,i) >_{i=I1,I2}$	[2]	$[I_1, I_2]$	$[MC]OBJET$ none $[1 \le I_1 \le I_2 \le IMAX]$
(I = particle number; J=1-7 for D,Y,T,Z,P,S,time)	3.1 3.2 3.4 3.5	-2 -3 -4 $1 - IMAX$ $1 - IMAX$ $1 - IMAX$ $1 - IMAX$	$ \begin{array}{r} 1 - 7 \\ 1 - 7 \\ 1 - 7 \\ 1 - 7 \\ 1 - 7 \\ 1 - 7 \\ 1 - 7 \\ 1 - 7 \\ 1 - 7 \\ \end{array} $	$ \begin{array}{c c} Sup(F(J,i))_{i=1,IMAX} \\ Dist\left[F(J,I)_{i=I1,I2}\right] \\ Dist\left[PU_i, i=1,N\right] \\ F(J,I) - FO(J,I) \\ F(J,I) + FO(J,I) \\ F(J,I) - F(J,K) \\ F(J,I) - F(J,K) \\ F(J,I) - F(J,K) \\ \end{array} $		$I_1, I_2, \Delta I$ $NOEL_A, NOEL_B$ K K	$1 \le I_1 \le I_2 \le IMAX$ PU range $K \le IMAX$ $K \le IMAX$
Ellipse parameters	4	1 - 6	1 - 6	$\sigma_{IJ} (\sigma_{11} = \beta_Y, \\ \sigma_{12} = \sigma_{21} = \alpha_Y, \text{ etc.})$			OBJET[KOBJ=8] ; MCOBJET[KOBJ=3]
Number of particles	5	$-1 \\ 1 - 3 \\ 4 - 6$	$ \leq 1 \\ \leq 1 \\ \leq 1 $	$\begin{array}{c} N_{survived} / \text{IMAX} \\ N_{in \ \epsilon_{Y,Z,X}} / N_{survived} \\ N_{in \ best \ \epsilon_{Y,Z,X,rms}} / N_{survived} \end{array}$	1	$\epsilon_{Y,Z,X}/\pi$	OBJET MCOBJET MCOBJET
Coordinates & fields, across optical elements $(J=1, 2, 3 \text{ for} B_{X, Y, Z})$	7.1 7.2 7.3 7.6 7.7 7.8 7.9 7.10	1 – IMAX 1 – IMAX 1 – IMAX 1 – IMAX 1 – IMAX 1 – IMAX 1 – IMAX	$ \begin{array}{r} 1-7\\1-7\\1-7\\1-3\\1-3\\1-3\\1-3\\1-7\end{array} $	min. (param.=1) or max. (2) of $F(J, I)$ max $(F(J, I))$ - min $F(J, I)$) min $F(J, I)$) + max $(F(J, I))$ min. or max. value of B_J max (B_J) - min (B_J) min (B_J) + max (B_J) $\int B_J ds$ to be documented	1 [or 3] 0 [or 2] id. 1 [or 3] 0 [or 2] id. id. id.	1 or 2 [, X1, X2] [X1, X2] id. 1 or 2 [, X1, X2] [X1, X2] id. id. id.	[MC]OBJET
Spin	10 10.1 10.2 10.3 10.4 10.5	1–IMAX 1–IMAX 1–IDMAX 1–IDMAX 1–IDMAX 1–IMAX	1 - 4 1 - 3 any 1 - 3 [0, 1] 1 - 3	$S_{X,Y,Z}(I), \vec{S}(I) $ $ S_{X,Y,Z}(I) - SO_{X,Y,Z}(I) $ spin precession angle $([-\pi,\pi])$ X, Y or Z component of precession axis spin tune $\langle S_{X,Y,Z} \rangle_{N=1,I \text{ particles}}$	0 [or 1]	[1]	SPNTRK+ [MC]OBJET OBJET[KOBJ=2] OBJET[KOBJ=1,2] OBJET[KOBJ=2] OBJET[KOBJ=2]

♦ *IMAX*: total number of particles tracked.

 \diamond *F*(*J*,*I*) : particle coordinate array ; J: coordinate (1-7 for respectively D, Y, T, Z, P, S, time, resp. units: none, cm, mrad, cm, mrad, cm, μ s) ; I: particle number.

 \diamond FO(J,I) : initial particle coordinates.

 $\diamond S(J,I)$: spin coordinate array; J: coordinate (1, 2, 3 for respectively X, Y, Z); I: particle number.

 \diamond SO(J,I) : initial spin coordinates.

♦ Constraints 7.1 - 7.9: X1 and X2, optional, define the longitudinal coordinate interval inside the optical element, over which it applies.

◊ Constraints 10.2 - 10.4: I is the number of the concerned 3-particle momentum group, among the *IDMAX* momentum groups defined by *OBJET[KOBJ=2,IDMAX]*;

◊ if only one group needed, OBJET[KOBJ=1,IMAX=3] may be used as well.

 \diamond Constraint 10.3: If NP=1 and pr_{NP} =1, then the absolute value of the X, Y or Z component is accounted for.

IC=7.8: Maximum plus minimum of the values taken by the X, Y or Z component of the field along the trajectory of particle number I.

IC=7.9: Integral of the X, Y or Z component of the field as experienced by particle number I, across the optical element.

IC=7.10: constraint on minimum value of coordinate J of particle I reached inside optical element K, and on maximum value of coordinate J2 of particle I2 inside very optical element K. Example of use: in a linear FFAG quadrupole doublet cell, it allows centering the orbits in the QF quadrupole such that extreme excursions (for instance, coordinate (J,I) [resp. (J2,I2)] reaching extreme negative (resp. positive) value) are equal in absolute value and opposite in sign.

IC=10: If $1 \le I \le IMAX$ then the constrint is the value of coordinate type J (J = 1, 3 for respectively S_X, S_Y, S_Z) of particle number I.

IC=10.1: Difference between final and initial J-spin coordinate of particle I (convenient *e.g.* for \vec{n}_0 spin vector search).

IC=10.2: Constraint on spin rotation angle for particles of momentum group #K. This requires *OBJET/KOBJ=2*, with groups of 3 particles, all particles in a group have the same momentum, and their spins in direction, respectively, X, Y, Z.

IC=10.3 : Constraint on spin rotation axis for particles of momentum group #K. This requires *OB*-*JET/KOBJ*=2, with groups of 3 particles, all particles in a group have the same momentum, and their spins in direction, respectively, X, Y, Z.

Constraining tunes

The example in the left column, Tab. 2, matches the (fractional) tunes in RHIC ring. It requires *OBJET[KOBJ=5]*, which creates a 13-particle sample proper to allow computation of transport coefficients (as done by MATRIX), from what optical functions and tunes are drawn.

Constraining chromaticities

The example in the right column, Tab. 2, matches both the (fractional) tunes and the chromaticities in RHIC ring. It requires OBJET[KOBJ=5.3] to create three 13-particle sets of sample particles, one set centered on the on-momentum closed orbit, the other two centered on respectively $\pm \delta p/p$ chromatic closed orbits (OBJET[KOBJ=5.2] also works and creates two sets only, on-momentum and at $\delta p/p$). Onmomentum as well as off-momentum 1st order transport coefficients are computed from these 13-particle sets (the same way as *MATRIX* does), from what optical functions and tunes are drawn. Chromaticities are given by the difference in the tunes obtained from the on-momentum, 13-particle set and the off-momentum, 13-particle set(s); this interpolation yields better accuracy in the 3-set case (OBJET[KOBJ=5.3]).

OBJECT DEFINITION

Depending on the type of constraint (see table p. 161), constraint calculations are performed either from transport coefficient calculation and in such case require OBJET with either KOBJ = 5 or KOBJ = 6, or from particle distributions and in this case need object definition using for instance OBJET with KOBJ = 8, MCOBJET with KOBJ = 3.

THE FITTING METHODS

The *FIT* procedure was drawn from the matrix transport code BETA [40]. It is a direct sequential minimization of the quadratic sum of all errors (*i.e.*, differences between desired and actual values for the NC constraints), each normalized by its specified weight W (the smaller W, the stronger the constraint).

Table 2: Fitting tunes (left column), or tunes and chromaticities (right column), using *SCALING*. Note the following in the latter case: *OBJET* specifies on-momentum as well as chromatic closed orbit coordinates for the three reference trajectories (respectively D=1, D=1.0001 and D=0.999); however, a different way is to include the search for closed orbit coordinates as part of the FIT request, just specifying the D value for each one of the three references.

	FITting SCALING parameters 'OBJET'
DITL'S CONTING STORES	
CONTERN	5.5 : Create three sets of 15 particles.
555 739008456e3	0 0 0 0 0 1 L Define on-momentum 13-particle set
5 Create one set of 13 particles.	0.022675 0.034243 0. 0. 1. 1.0001 Define dp/p==He-4 off-momentum 13-particle set
.001 .01 .001 .01 .001 .0001	-0.022675 -0.034243 0. 0. 0. 0.9999 ! define dp/p=-le-4 off-momentum 13-particle se
0. 0. 0. 0. 1.	initial coordinates are chromatic coordinates
	'PARTICUL'
'PARTICUL'	HELION
HELION	'FAISCEAU'
'FAISCEAU'	'SCALING'
'SCALING'	1 6
1 6	BEND
BEND	-1
-1	555.739008456
555.739008456	1
1	MULTIPOL
MULTIPOL	-1
-1	555.569221809
555.739008456	1
	MULTIPOL QUADQF ! QF family quads all have LABEL!=QUADQF
MULTIPOL QUADQF ! QF TAMILY quads all have LABEL!=QUADQF	-1 555 560001000 - 1 DIT modeble #10
-1 EEE EC0001000 / FTT warishin #10	555.569221609 : FII Variable #12
1	I MULTIPOL OUADOD I OD family guade all have LARELI-OUADOD
MULTIPOL OUNDOD OD family guade all bave LARELI-OUNDOD	-1
-1	-
554.852506166 ! FIT variable #16	
1	MULTIPOL SEXTSF ! SF family sextus all have LABEL!=SEXTSF
MULTIPOL SEXTSF ! SF family sextus all have LABEL!=SEXTSF	-1
-1	555.739008456 ! FIT variable #20
555.739008456 ! FIT variable #20	1
1	MULTIPOL SEXTSD ! SD family sextus all have LABEL!=SEXTSD
MULTIPOL SEXTSD ! SD family sextus all have LABEL!=SEXTSD	-1
-1	555.739008456 ! FIT variable #24
555.739008456 ! FIT variable #24	1
1	
	'INCLUDE'
'INCLUDE'	1
	./RHICSequence[RHIC\$START:RHIC#END]
./RHICSequence[RHIC\$START:RHIC#END]	
/ FTT/	
2	4 4 12 0 2 Varu OF familu
4 12 0 2 / Vary OF family	4 16 0 2 Vary OF family
4 16 0 .2 ! Vary OD family	4 20 0 .2 Vary SF family
2	4 24 0 .2 Vary SD family
0.1 7 7 #End 0.6850251017 1. 0 ! frac. QY	4
0.1 8 8 #End 0.6730125830 1. 0 ! frac. QZ	0.1 7 7 #End 0.6850251017 1. 0 ! frac. QY
'END'	0.1 8 8 #End 0.6730125830 1. 0 ! frac. QZ
	1.1 7 7 #End 1. 1. 0 ! xi_Y
	1.1 8 8 #End 1. 1. 0 ! xi_Z
	'END'

The step sizes for the variation of the physical parameters depend on their initial values, and cannot be accessed by the user. At each iteration, the optimum value of the step size, as well as the optimum direction of variation, is determined for each one of the *NV* variables. Then follows an iterative global variation of all *NV* variables, until the minimization fails which results in a next iteration on the optimization of the step sizes.

The *FIT2* procedure is based on the Nelder-Mead method, it has various specificities, details can be found in Ref. [41].

The optimization process may be stopped by means of a penalty value, or a maximum number of iterations on the step size or on the call to the function.

COMBINING FIT[2] AND REBELOTE

FIT[2] may be followed by the keyword *REBELOTE*. This allows for instance executing again the fitting procedure, following a change, by *REBELOTE*, in the value of some parameter(s) (about any parameter) in zgoubi.dat optical sequence.

The values of the variables in *FIT[2]* itself (and their weights as well) can be changed by *REBELOTE*. More on that can be found under *REBELOTE*, Sec. 6.4, page 176.

EXAMPLE - Examples are given page 274.

Conversely, *REBELOTE* may be followed by the keyword *FIT[2]*. This allows for instance optimization of constraints that require multi-turn tracking (*e.g.*, optimized tune-jump quadrupole settings for beam acceleration through depolarizing resonances).

AN UPDATED SEQUENCE FILE

When a zgoubi run includes *FIT[2]*, an updated input data file, ready to use, is saved under the name zgoubi.FIT.out.dat at the end of the run.

FIT[2] OPTIONS

FIT and FIT2 accept various options, as follows.

- 'nofinal' option : a request to avoid a final run that would normally follow the completion of the fit, allowing for the variable values as just determined by *FIT[2]*. By default, *i.e.*, if 'nofinal' does not appear in the *FIT[2]* keyword data list, then that final run does occur. The latter is necessary in particular when it is desired to store resulting particle data, in two cases for instance:

- when using FAISTORE, particle data desired at the sole very final pass.

- when using IL=2 in some optical element(s): in that case a final run would allow print out of trajectories with final FIT variable states.

- 'save' [, FileName] option : a request for the variable values as resulting from *FIT*[2] to be saved, by default in zgoubi.FITVALS.out, or in *FileName* file if the latter is specified following the 'save' instruction.

- Penalty : value of the penalty to be reached, following what the *FIT[2]* procedure will be considered completed, and thus stopped.

- ITER : maximum allowed number of "calls to the function" (namely, (recursive) calls to zgoubi). Once that number is reached, *FIT[2]* is stopped, regardless of a possible "penalty" value.

EXAMPLE - An example using all five options, "nofinal", "save [FileName]", "penalty" and "ITER", is given in page 277.

GASCAT : Gas scattering

Modification of particle momentum and velocity vector, performed at each integration step, under the effect of scattering by residual gas.

INSTALLATION IS TO BE COMPLETED.

GETFITVAL : Get values of variables as saved from former FIT[2] run

This keyword allows reading, from a file whose name needs be specified, parameter values to be assigned to optical elements in zgoubi.dat.

That file is expected to contain a copy-paste of the data under the *FIT[2]* procedure as displayed in zgoubi.res, normally under the form

SI	FATUS	OF V.	ARIA	ABLES	(Iterati	lon #	95)						
Ι	LMNT	VAR	PARA	AM MIN	JIMUM	INITIAL	FINAL	MAXIMUM	STEP	NAME		LBL1	LBL2
	145	1	4	-3.	.000E+03	762.	761.9484791	3.000E+03	1.254E-	05 MULTI	POL	HKIC	DHCB02
	182	2	4	-1.	.000E+03	-231.	-230.9846875	1.000E+03	4.182E-	06 MULTI	POL	HKIC	DHCB08
	146	3	4	-1.	.000E+03	-320.	-319.8554171	1.000E+03	4.182E-	06 MULTI	POL	VKIC	DVCB02
	183	4	4	-1.	.000E+03	528.	527.7249064	1.000E+03	4.182E-	06 MULTI	POL	VKIC	DVCB08
	615	5	4	-3.	.000E+03	308.	307.6860565	3.000E+03	1.254E-	05 MULTI	POL	HKIC	DHCF02
	651	6	4	-1.	.000E+03	-114.	-113.8490362	1.000E+03	4.182E-	06 MULTI	POL	HKIC	DHCF08
	616	7	4	-1.	.000E+03	-78.9	-78.88730937	1.000E+03	4.182E-	06 MULTI	POL	VKIC	DVCF02
	652	8	4	-1.	000E+03	212.	211.8789183	1.000E+03	4.182E-	06 MULTI	POL	VKIC	DVCF08
#	STAT	US OF	CON	ISTRAIN	ITS								
#	TYPE	I	J	LMNT#	DESI	IRED	WEIGHT	REACHED		KI2	*	Parame	ter(s)
#	3	1	2	127	0.0000	00E+00	1.0000E+00	1.0068088E	-08 6.	0335E-01	*	0:	
#	3	1	3	127	0.00000	00E+00	1.0000E+00	7.0101405E	-09 2.	9250E-01	*	0 :	
#	3	1	4	127	0.0000	00E+00	1.0000E+00	2.9184383E	-10 5.	0696E-04	*	0:	
#	3	1	5	127	0.0000	00E+00	1.0000E+00	3.1142381E	-10 5.	7727E-04	*	0:	
#	3	1	2	436	0.00000	00E+00	1.0000E+00	3.8438378E	-09 8.	7944E-02	*	0:	
#	3	1	3	436	0.00000	00E+00	1.0000E+00	1.5773011E	-09 1.	4808E-02	*	0 :	
#	3	1	4	436	0.0000	00E+00	1.0000E+00	2.2081272E	-10 2.	9022E-04	*	0:	
#	3	1	5	436	0.00000	00E+00	1.0000E+00	5.7930552E	-11 1.	9975E-05	*	0 :	
#	Fui	nctio	n c	called	1859 t	imes							
#	Xi2 =	=	1.68	3006E-1	6 Busy	/ 							

A '#' at the beginning of a line means it is commented, thus it will not be taken into account. However a copy-paste from zgoubi.res (which is the case in the present example) would not not need any commenting.

Since some of the *FIT*[2] variables may belong in [*MC*]*OBJET*, *GETFITVAL* may appear upstream of [*MC*]*OBJET* in zgoubi.dat, to allow updating the latter.

Once completed, *FIT*[2] will be followed by a final run of zgoubi.dat with variable values updated as resulting from the fit. This can be inhibited by indicating 'nofinal' option in *FIT*[2] (see page 164). For that final run *GETFITVAL* will be inhibited so avoid overridding the updated variable values.

GOTO : Branching statement

TO BE DOCUMENTED FURTHER.

GOTO is a conditional goto, working much like the fortran branching statement. It sends the execution pointer to some keyword (*e.g.*, "*MARKER*") in the optical sequence, characterized by one or two specific labels.

Available options :

- pass number

GOTO accepts GOBACK as an argument, this sends the execution pointer back to the next keyword immediately following the calling GOTO.

GOTO/GOBACK for instance can be used in RLA type of optical sequence, to direct the **zgoubi** amongst the series of spreaders of mergers.

EXAMPLE - An example of an input data file of a recirculating linac, structured using *GOTO* statements, can be found in page 287.

INCLUDE : File include statement

INCLUDE works much like the fortran "include" statement : it allows a fragment of an ancillary input data file to be taken from a separate file : when *INCLUDE* is met, the content of the ancillary file, or part of it as stated, is inserted in the data sequence. That file can be any ascii file, including *e.g.* your latest latex report, from which *INCLUDE* is requested to find a sequence of lines of text (presumably, a zgoubi.dat style sequence of lines).

The INCLUDE statement takes the following arguments :

- the number of ancillary input files to include a fragment from,

- their names, in as many lines, one name per line, and possibly, for each file, a preceding repeat factor - an integer - telling how many times that file has to be INCLUDEd.

The file name may be followed by '[LBL_1A,LBL_2A:LBL_1B,LBL_2B]', with any of these four labels optional, as follows :

- LBL_1A [LBL_2A] identify to the first [and possibly second] label of some keyword in the include file, from which the include process will start (whatever precedes will be ignored). If none of '*LBL_1A*, _2A' is declared, the include process starts from the begining of the include file. Declaring the second label only takes the form '[*,LBL_2A:LBL_1B,LBL_2B*]'.

- LBL_1B [LBL_2B] identify to the first [and second] label of a *MARKER* or some data-less keyword (such as *FAISCEAU*, ...) in the include file, at which the include process will end (whatever follows will be ignored). If none of '*LBL_1B*, *_2B*' is declared, the include file will be included down to its end. Declaring the second label only takes the form '*[LBL_1A,LBL_2A: ,LBL_2B]*'.

Because **zgoubi** uses the reserved name zgoubi.dat as its standard working data file name, and as the presence of *INCLUDE* will cause the input data list to be changed (it is expanded to include the content of all INCLUDed files), the user's input data file is no longer allowed the name zgoubi.dat if it contains *IN-CLUDE* keyword(s) (zgoubi.dat is reserved as the name of the expanded input file to zgoubi). This is overcome by using the command 'zgoubi -fileIn myFile' instead, with myFile \neq zgoubi.dat (see Sec. 1.2 in PART D of the guide, page 371).

An *INCLUDE* file may contain one or more *INCLUDE*. There is a limit in the allowed depth of *INCLUDE* statements within *INCLUDE* files, however high. **zgoubi** will warn the user when it is exceeded. It can be changed in prdata.f.

By contrast with other keywords, *INCLUDE* is not part on the LSTKEY.H keyword list (found in the '*include*' folder). Instead, possible presence of *INCLUDE* in the input data file is dealt with by prdata program (prdata.f source file) in a simple way : the input data file is expanded so eliminating all *INCLUDE* occurences, and the expanded, complete, data list is stored in the standard **zgoubi** input data file zgoubi.dat. Thus **zgoubi** eventually actually works using a regular, complete, data list in a single input file, zgoubi.dat.

EXAMPLE - An example of an input data file of a recirculating linac, structured using *INCLUDE* statements, can be found in page 287.

MCDESINT : Monte-Carlo simulation of in-flight decay

When *MCDESINT*[43] is met in an optical sequence (normally, after *OBJET* or after *CIBLE*), in-flight decay simulation starts. It must be preceded by *PARTICUL* for the definition of mass M_1 and *COM* lifetime τ_1 of the parent particle.

The two-body decay simulated is

$$1 \longrightarrow 2+3$$

The decay is isotropic in the center of mass. 1 is the incoming particle, with mass M_1 , momentum $p_1 = \gamma_1 M_1 \beta_1 c$ (relative momentum $D_1 = \frac{p_1}{q} \frac{1}{BORO}$ with BORO = reference rigidity, defined in [MC]OBJET). 2 and 3 are decay products with respective masses and momenta M_2 , M_3 and $p_2 = \gamma_2 M_2 \beta_2 c$, $p_3 = \gamma_3 M_3 \beta_3 c$. The mean decay distance s_1 is related to the center of mass lifetime τ_1 by

$$s_1 = c\tau_1 \sqrt{\gamma_1^2 - 1}$$

The individual distance $s_d(I)$ to the decay point is calculated for each one of the *I*=1,*IMAX* particles defined by *[MC]OBJET*, from a random number $0 < R_1 \le 1$, using the exponential decay rule

$$_{d}s = -s_{1}\ln R_{1}$$

After decay of the parent particle 1, particle 2 will be ray-traced with assumed positive charge, while particle 3 is discarded. Its scattering angles in the center of mass θ^* and ϕ are generated from two other random numbers $0 < R_2 \le 1$ and $0 < R_3 \le 1$ using

$$\begin{aligned} \theta^* &= \operatorname{acos}(1 - 2R_2) \qquad (0 < \theta^* \le \pi) \\ \phi &= 2\pi R_3 \qquad (0 < \phi \le 2\pi) \end{aligned}$$

 ϕ is a relativistic invariant, and θ in the laboratory frame (Fig. 45) is given by

$$\tan \theta = \frac{1}{\gamma_1} \frac{\sin \theta^*}{\frac{\beta_1}{\beta_2^*} + \cos \theta^*}$$

 β_2^* and momentum p_2 are given by

$$\gamma_{2}^{*} = \frac{M_{1}^{2} + M_{2}^{2} - M_{3}^{2}}{2M_{1}M_{2}}$$
$$\gamma_{2} = \gamma_{1}\gamma_{2}^{*} \left(1 + \beta_{1}\beta_{2}^{*}\cos\theta^{*}\right)$$
$$\beta_{2} = \left(1 - \frac{1}{\gamma_{2}^{2}}\right)^{1/2}$$
$$p_{2} = M_{2}\sqrt{\gamma_{2}^{2} - 1}$$

Finally, θ and ϕ are transformed into the angles T_2 and P_2 in the **zgoubi** frame, and the relative momentum takes the value $D_2 = \frac{p_2}{q} \frac{1}{BORO}$ (where BORO is the reference rigidity, see OBJET), while the starting position of M_2 is the very location of the parent particle decay, (Y_1, Z_1, s_1) .

The decay simulation by **zgoubi** satisfies the following procedures. In optical elements and field maps, after each integration step *XPAS*, the current path length of the particle (F(6, I) in the source code) is compared to decay point location s_d . If s_d is passed, then the particle is considered to have decayed at $F(6, I) - \frac{XPAS}{2}$ (XPAS is the integration step), at a position obtained by a linear translation from the position at F(6, I). Presumably, the smaller *XPAS*, the smaller the error on position and angles at the decay point.

(page 292 in PART B)



Figure 45: At position $M(X_1, Y_1, Z_1)$, particle 1 decays into 2 and 3 ; **zgoubi** then proceeds with the computation of the trajectory of 2, while 3 is discarded. θ and ϕ are the scattering angles of particle 2 relative to the direction of the incoming particle 1 ; they transform to T_2 and P_2 in **zgoubi** frame.

In ESL and CHANGREF, the current path length s = F(6, I) at the end of the element is compared to s_d . If the decay distance s_d happens to be comprised within the element then the particle coordinates at s_d are recomputed by linear translation from s.

The $s_d(I = 1, IMAX)$ values are stored in the array FDES(6, I). For further statistical purposes (*e.g.*, use of *HISTO*) the daughter particle 2 is tagged with an 'S' standing for "secondary". When a particle decays, its coordinates D, Y, T, Z, P, s, time at the decay point are stored in FDES(J, I), J = 1, 7.

A note on negative drifts :

The use of negative drifts with *MCDESINT* is allowed. For instance, negative drifts may occur in an optical structure : for some of the particles when using *CHANGREF* (due for instance to the Z-axis rotation or a negative *XCE*); or when using *DRIFT* with XL < 0. Provision has been made to take it into account during the *MCDESINT* procedure, as follows.

If, due to a negative drift, a secondary particle reaches back the decay location of its parent particle, then the parent particle is "resurrected " with its original coordinates at that location, the secondary particle is discarded, and ray-tracing resumes in a regular way for the parent particle which is again allowed to decay when s_d is reached. This procedure is made possible by prior storage of the coordinates of the parent particles (in array FDES (J, I)) each time a decay occurs.

Negative steps (XPAS < 0) in optical elements are not compatible with MCDESINT.

Backward option:

By default, a particle moving backward upon decay is stopped (its IEX flag (see Sec. 7.12 is set to -11). This can be reversed using the option back=1.

OPTICS : Write out optical functions. Log to zgoubi.OPTICS.out

OPTICS normally appears next to object definition, it normally works in conjunction with element label(s). *OPTICS* causes the transport and write out, in zgoubi.res, of the 6×6 beam matrix, following options *KOPT* and '*label*', below.

IF KOPT=0 : Off

IF *KOPT=1* : Will transport the optical functions with initial values as specified in *OBJET*, option *KOBJ=5.1*. Note that *OPTICS* assumes the first particle of the set of 13 as defined by *OBJET*, to be the reference particle for computation of the transport coefficients.

Note : In the case of a periodic optical sequence, the initial coordinate values in *OBJET[KOBJ=5.1]* may be the periodic ones (as obtained, for instance, from a first run using *MATRIX[IFOC=11]*). Using *TWISS* keyword instead may be considered in that case.

A second argument, 'label', allows

- if *label = all* : printing out, into zgoubi.res, after all keywords of the zgoubi.dat optical sequence,

- otherwise, printing out at all keyword featuring $LABEL1 \equiv label$ as a first label (see section 7.7, page 207, regarding the labelling of keywords).

PRINT : An optional third argument, *IMP=1*, or equivalently the command 'PRINT', will cause saving of the transported optical functions into file zgoubi.OPTICS.out.

About the source code :

The program beamat ensures the transport of the beam matrix along the zgoubi.dat sequence. beamat is called by opticc, itself called after each optical element, in the program zgoubi.

The starting beam matrix value is in the array FI, initialized by *OBJET[KOBJ=5.1]*, program obj5. The array F0 contains the running beam matrix.

The program beaimp prints to zgoubi.res, whereas optimp prints to zgoubi.OPTICS.out. Both are called from opticc.

OPTIONS : Global or special options

(page 303 in PART B)

OPTIONS allows on/off switching of various options.

Available, for now :

- 'WRITE ON or OFF'

Role : inhibit (most of) write statements to zgoubi.res.

Interest : 'WRITE OFF' may allow substantial savings on CPU time. 'WRITE ON' sets back to normal (the 'normal' state of write outs may depend on the status of other commands, such as *REBELOTE*, on-going *FIT[2]*, etc.).

- '.plt -1, 0, 1, 2 or 7'

Role : force IL value (cf. Sec. 7.6, p. 207) in all optical elements.

Interest : avoids changing IL value element by element, a hurdle in long optical sequences.

- 'CONSTY ON or OFF'

Role : force to constant Y and Z coordinates during stepwise integration.

This allows for instance checking fields, or fabricating field maps from **zgoubi**'s analytical models of optical elements, as follows.

Concurrent use with IL = 1, 2, or 7 (*cf.* '.plt' option here, or Sec. 7.6, p. 207) will allow logging \vec{B} and/or \vec{E} field(s) (and their derivatives) experienced across optical elements, in zgoubi.res, zgoubi.plt or zgoubi.impdev.out respectively.

As a consequence, forcing Y and Z to constant values, using 'CONSTY ON', allows checking of fields (and derivatives) at constant Y and Z, as determined by *OBJET*, across (individual or short series of) optical elements. This may be helpful when setting up input data in **zgoubi**. It can be for instance of great help in case of complex geometrical and field data inputs, as in *DIPOLES*, *FFAG*.

Initial coordinates are set in a very regular manner using *OBJET*. The *Y* coordinate will stand for the radius value in the case of optical elements defined in polar coordinates (*e.g.*, *DIPOLES*, polar field maps, etc.).

- 'AGSQUADS ON'

Role : change winding currents in some AGS quadrupole families. The program agsquf.f is resorted to to achieve that.

- 'MONITOR IDLUNI'

Role : monitor zgoubi execution, a sort of debugging tool.

IDLUNI option monitors the IDLUNI counter.

More options can be added to MONITOR, in options.f.

ORDRE : Taylor expansions order

The position \vec{R} and velocity \vec{u} of a particle are obtained from Taylor expansions as described in eq. (1.2.4). By default, these expansions are up to the fifth order derivative of \vec{u} ,

$$\vec{R}_1 \approx \vec{R}_0 + \vec{u}\Delta s + \dots + \vec{u}^{(5)} \frac{\Delta s^6}{6!}$$
$$\vec{u}_1 \approx \vec{u} + \vec{u}'\Delta s + \dots + \vec{u}^{(5)} \frac{\Delta s^5}{5!}$$

which corresponds to fourth order derivatives of fields \vec{B} , eq. (1.2.8). and of \vec{E} , eq. (1.2.13).

However, third or higher order derivatives of fields may be zero in some optical elements, for instance in a sharp edge quadrupole. Also, in several elements, no more than first and second order field derivatives are implemented in the code. One may also wish to save on computation time by limiting the time-consuming calculation of lengthy (while possibly ineffective in terms of accuracy) Taylor expansions.

In that spirit, the purpose of *ORDRE*, option IO = 2 - 5, is to allow for expansions to the $\vec{u}^{(n)}$ term in eq. 1.2.4. Default functioning is IO = 4, stated in *FORTRAN* file block.f.

Note the following : As concerns the optical elements

DECAPOLE, DODECAPO, EBMULT, ELMULT, MULTIPOL, OCTUPOLE, QUADRUPO, SEXTUPOL

field derivatives (see eq. 1.2.10 p. 23, eq. 1.2.15 p. 24,) have been installed in the code according to $\vec{u}^{(5)}$. Taylor development order ; it may not be as complete for other optical elements. In particular, in electric optical elements field derivatives (eq. 1.2.15) are usually provided to no more than second order, which justifies saving on computing time by means of *ORDRE*, so to avoid pushing Taylor expansions as high as $\vec{u}^{(5)}$.

NOTE : see also the option IORDRE in field map declarations (DIPOLE-M, TOSCA, etc.).

PARTICUL : Particle characteristics

Since **zgoubi** works using the rigidity, ("BORO", as declared in [MC]OBJET), the keyword PARTICUL is in general not necessary.

However, it needs be introduced (normally, following [MC]OBJET in the input data file zgoubi.dat) when the definition of some characteristics of the particles (such as mass, charge, gyromagnetic factor, life-time in the center of mass) is needed, as is the case when using the following procedures :

CAVITE	: mass, charge
MCDESINT	: mass, COM life-time
SPNTRK	: mass, gyromagnetic factor
SRLOSS	: mass, charge
SYNRAD	: mass, charge
Electric and Electro-Magnetic elements	: mass, charge

The declaration of PARTICUL must precede these keywords.

If *PARTICUL* is omitted, which is in general the case when ray-tracing ions in purely magnetic optical assemblies, then **zgoubi** only knows the particle rigidity and would thus skip the computation of such quantities as time of flight, spin precession, synchrotron radiation, etc.

The expected attributes under PARTICUL are

mass, charge, gyromagnetic factor, life-time

On the other hand, particle name can be substituted to that parameter list. Known particles are:

ELECTRON POSITRON MUON+ MUON-PION+ PION-PROTON HELION DEUTERON

Actual particle parameters are found listed in zgoubi.res when using *PARTICUL*. They may also be found in rparti.f.

REBELOTE : 'Do it again'

When *REBELOTE* is encountered in the input data file, the code execution jumps,

- either back to the beginning of the data file - the default behavior,

- or, if option *K*=99.1 or *K*=99.2, back to a particular *LABEL*1.

Then NPASS-1 passes (from LABEL1 to REBELOTE) follow.

As to the last pass, number NPASS+1, there are two possibilities :

- either it also encompasses the whole LABEL1 to REBELOTE range,

- or, upon request (option K=99.2), execution may exit that final pass upstream of *REBELOTE*, at a location defined by a second dedicated *LABEL2* placed between the first aforementioned *LABEL1*, and *REBELOTE*. In both cases, following the end of this "multiple-pass" procedure, the execution continues from the keyword which follows *REBELOTE*, until '*END*' is encountered.

Amongst other, these procedures allow for instance raytracing through the following sequence: injection line + multiturn in a ring + extraction line.

The three functionalities of REBELOTE are the following :

1. **Beam lines**: *REBELOTE* can be used for Monte Carlo simulations in beam lines (in which case K = 0), when more than the maximum allowed Max(*IMAX*) particles¹² are to be tracked. In that functioning mode, when procedures such as *HISTO*, MCDESINT, *MCOBJET*, *OBJETA*, SPNTRK[*KSO* = 5] are used, their random seeds are not reset and independent statistics will add up pass after pass.

This allows for instance high statistics Monte Carlo simulations. *NPASS* runs through the optical sequence, from *MCOBJET* to *REBELOTE* will result from the latter, resulting in the calculation of (1 + NPASS) * IMAX trajectories, with as many random sets of initial coordinates.

2. Multiturn tracking: *REBELOTE* can be used for multi-turn ray-tracing in circular machines ; normally K = 99 in that case (or K = 99.2, see below). *NPASS* turns in the optical sequence will follow, resulting in the tracking of *IMAX* particles over 1 + NPASS turns. For the simulation of pulsed power supplies, synchrotron motion, and other Q-jump manipulation, see *SCALING*.

For instance, using option described K=99.2 above, a full "injection line + ring + extraction line" installation can be simulated - kicker firing and other magnet ramping can be simulated using SCAL-ING.

Using the double-LABEL1-2 method discussed above with option K=99.2, it is possible to encompass the ring between an injection line section (namely, with the element sequence of the latter extending from *OBJET* to the first *LABEL1*), and an extraction line (its description will then follow *REBE-LOTE*), whereas the ring description extends from to the first *LABEL1* down to *REBELOTE*, with possible extraction, at the last pass, at the location of the second *LABEL2*, located anywhere between the *LABEL1* and *REBELOTE*, Note : Some *CAVITE* options cause a reset-to-zero of individual particle path length¹³. This is for reasons of cumulated path length accuracy (a delta-path below computer accuracy compared to total path length would not be resolved - it can be for instance bunch length as compared to cumulated multi-turn distance around a large ring). This reset may not be desirable, it depends on the multi-turn problem dealt with using *REBELOTE*, it may be necessary for instance in long-term tracking in large rings, it is not in recirculating linacs. Option K=99 in *REBELOTE* will cause this reset, whereas option K=98 (UNDER DEVELOPMENT, In cavite.f, IN THIS VERSION OF THE CODE) will avoid it everything else left unchanged.

3. **Do-loop**: in that case *IOPT=1*; *REBELOTE* can change the value of arbitrary parameters in zgoubi.dat optical sequence, using the forth argument *IOPT=1* (see page 314). *NPRM* tells the number of parameters to be changed. A series of *NPRM* lists of values, one list per parameter to be changed and each list with *NRBLT* data, tells the values to be taken by each one of these parameters, over the *NRBLT* passes of the *REBELOTE* process.

IOPT=1 is under development. TO BE DOCUMENT FURTHER.

Printouts

Printouts over NPASS+1 passes might result in a prohibitively big zgoubi.res file. They may be switched on/off by means of the option KWRIT = i.j, with i = 1/0 respectively. The j flag allows a printout of the pass number and of some additional information to the video output, every 10^{j-1} turns if j > 0; video output is essentially switched off during REBELOTE execution if j = 0.

REBELOTE also provides information : statistical calculations and related data regarding particle decay (*MCDESINT*), spin tracking (*SPNTRK*), stopped particles (*CHAMBR*, *COLLIMA*), etc.

COMBINING REBELOTE AND FIT[2]

The keyword *REBELOTE* can follow *FIT[2]*. This allows executing again the fit procedure, after changing the value of some parameter(s) in zgoubi.dat using *REBELOTE* with option *IOPT=1*. That's the interest of the game : *REBELOTE* changes that (these) parameter(s), and then sends the zgoubi execution pointer back to the top of zgoubi.dat for a new *FIT[2]* run. Note that parameters in *FIT[2]* itself can be changed, if a parameter scan so requires for instance.

Conversely, *REBELOTE* may be followed by the keyword *FIT[2]*. This allows for instance optimization of constraints that require multi-turn tracking (*e.g.*, optimized tune-jump quadrupole settings for beam acceleration through depolarizing resonances).

EXAMPLES

- An example of the use of REBELOTE loop including data changes is given page 315.
- An example of FIT embedded in a REBELOTE loop is given page 274.

RECOVERING FROM A CRASH

When accelerating a bunch, *REBELOTE* is used to ensure the multi-turn process. Now, if the job is stopped - due to computer crash or else - it is possible to resume the tracking from the latest records (in [b_]zboubi.fai storage file), using *OBJET*, *KOBJ*= 3. *CAVITE* and *SCALING* aspects of the data file modifications necessary to ensure the recovery, in the case of pulsed magnets, are discussed respectively in the *SCALING* section, pp. 178, 181,

EXAMPLE - An example of job resuming is given page 299.

 $^{^{13}}$ For the geek: the "f(6,I)=0.d0" statements in cavite.f.

RESET : Reset counters and flags

Resets counters involved in CHAMBR, COLLIMA, HISTO and INTEG procedures.

Switches off CHAMBR, MCDESINT, SCALING and SPNTRK options.

SCALING : Power supplies and R.F. function generator

SCALING acts as a function generator dedicated to

- varying fields in optical elements, potentials in electrostatic devices, possibly in correlation with the reference rigidity $B\rho_{ref}$ (Sec. 7.2) for instance by *CAVITE*.

- varying one or more parameters (so, not necessarily field values), in an arbitray optical element. This capabilities is developped *on demand*, thus at present available in a limited number of elements (namely, CHANGREF, SPINR, AGSMM, AGSQUAD, a couple more may be...). *TO BE DOCUMENTED FUR-THER*.

SCALING is normally intended to be declared after the object definition. Nothing precludes declaring it later though, it will be taken into account from the moment that it is met within zgoubi.dat optical sequence.

Used in conjunction with *REBELOTE* for the simulation of multi-turn tracking, *SCALING* allows to change fields turn-by-turn in an arbitrary, user defined manner during an acceleration multi-turn. Fields (for instance main magnets fields) may instead be forced to follow a rigidity change caused by *CAVITE*, this can be obtained by simply using NT=-1 as the first argument in *SCALING*, see below.

The latter case (*i.e.*, fields being correlated to *CAVITE*), allows the simulation of a recirculating linac (thus optical elements between cavities are scaled, following the rigidity increase cavity by cavity), or multiple RF stations in a ring.

SCALING acts on families of elements, a family being designated by its name that coincides with the keyword of the corresponding element. For instance, declaring *MULTIPOL* as to be scaled will result in the same timing law being applied to all *MULTIPOLs* in zgoubi.dat optical sequence. Subsets can be selected by labeling keywords in the data file (section 7.7, page 207) and adding the corresponding *LABEL*(s) in the *SCALING* declarations (9 *LABELs* maximum - for the geek: this can be changed in MXFS.H, parameter *MLF*). The family name of concern, as well as the scaling function for that family, are given as input data to the keyword *SCALING*. There is an upper limit to the number *NF* of families that can be declared as subject to a scaling law (this can be changed in the *FORTRAN* include file MXFS.H, parameter *MXF*).

A scaling law can be comprised of up to NT successive timings. NT is thus normally a positive integer, its value tells the number of timings used in simulating a time dependent power supply or RF function. The scaling factor at all turns is obtained by linear interpolation from the so declared timing series, see below. However, NT can also be a real and/or take negative values, being in this case an option switch, see below.

If a family appears more than once in the *SCALING* list (*i.e.*, identical keyword and label list), the following will occur :

- if each instance addresses a different parameter in the optical elements concerned, both scaling rules are applied,

- if two (or more) instances address the same parameter in the optical elements, the last instance will prevail.

If a family addressed is a subset of a previously declared one, the *SCALING* rule will override the previous one, for that subset only.

The following illustrates typical data formatting for the simulation of an acceleration cycle in a circular accelerator:

SCALING		
1 5 QUADRUPO QFA QFB 2		Active. $NF = 5$ families of elements are concerned, as listed below : - QUADRUPO keywords labeled 'QFA' and Quadrupoles labeled 'QFB' NT = 2 timings
18131.E-3	24176.E-3	The field increases (linearly) from $18131E-3*B_0$ to $24176E-3*B_0$
1	6379	from turn 1 to turn 6379
MULTIPOL		- General rule. Precedes labeled cases if any.
2		NT = 2 timings
18131.E-3	24176.E-3	Fields increase from 18131E-3* B_i to 24176E-3* B_i ($\forall i = 1, 10$ poles)
1	6379	from turn 1 to turn 6379
MULTIPOL QDA QDB		- MULTIPOL keywords labeled 'QDA' and Multipoles labeled 'QDB'
2		NT = 2 timings
18131.E-3	24176.E-3	Fields increase from 18131E-3* B_i to 24176E-3* B_i ($\forall i = 1, 10$ poles)
1	6379	from turn 1 to turn 6379
BEND		- All BEND keywords, regardless of any LABEL
2		NT = 2 timings
18131.E-3	24176.E-3	As above
1	6379	
CAVITE		- Accelerating cavity
3		NT = 3 timings
1 1.22	1.33352	The synchronous rigidity $(B\rho)_s$ increases linearly,
1 1200	6379	from $(B\rho)_{s_o}$ to $1.22 * (B\rho)_{s_o}$ from turn 1 to 1200, and
		from $1.22 * (B\rho)_{s_o}$ to $1.33352 (B\rho)_{s_o}$ from turn 1200 to 6379

The timing is in unit of turns. In this example, TIMING = 1 to 6379 (turns). Therefore, at turn number N, B and B_i are updated in the following way. Let SCALE(TIMING = N) be the updating scale factor

$$SCALE(N) = 18.131 \frac{24.176 - 18.131}{1 + 6379 - 1} (N - 1)$$

and then

$$B(N) = SCALE(N)B_0$$

$$B_i(N) = SCALE(N)B_{i0}$$

The RF frequency is computed using

$$f_{RF} = \frac{hc}{\mathcal{L}} \frac{q(B\rho)_s}{(q^2(B\rho)_s^2 + (Mc^2)^2)^{1/2}}$$

where the rigidity is updated in the following way. Let $(B\rho)_{s_o}$ be the initial rigidity (namely, $(B\rho)_{s_o} = BORO$ as defined in the keyword *OBJET* for instance). Then, at turn number N,

if
$$1 \le N \le 1200$$
 then, $SCALE(N) = 1 + \frac{1.22 - 1}{1 + 1200 - 1} (N - 1)$
if $1200 \le N \le 6379$ then, $SCALE(N) = 1.22 + \frac{1.33352 - 1.22}{1 + 6379 - 1200} (N - 1200)$

and then,

$$(B\rho)_s(N) = SCALE(N) \cdot (B\rho)_{s_o}$$

from which value the calculations of $f_{RF}(N)$ follow.

Beyond the regular $NT \ge 1$ (or the short-cut NT = -1), there are coded "values" for NT, as follows.

Case of NT.Int: NT=1 and Int is an integer. This is for special scaling laws and/or reading from external files, as follows:

• NT = 1.10: allows taking the scaling law from an external data file, as in the following example :

MULTIPOL COH1	Scaling applies to all multipole field components, in <i>MULTIPOL</i> keywords having ' <i>COH1</i> ' as first label.
1.10 [,FAC]	Scaling is read from a file, file name <i>e.g.</i> 'scalingFile'; FAC is an additional scaling factor.
scalingFile	File name (file is expected to contain at least N2 columns).
1 n	Column number n lists the scaling factor at rigidity values listed in column number 1; current scaling is obtained by interpolation in this table (and multiplied by <i>FAC</i> if specified).

• NT = 1.11: TO BE DOCUMENTED FURTHER.

someKEYWORD [someLABEL1] 1.11

• NT = 1.12: allows taking the scaling law from an external data file, as in the following example :

AGSQUAD QH_A17 1.12	Scaling applies to AGSQUAD keyword having 'COH1' as first label. Scaling is read from a file, file name e.g. 'scalingFile'.
scalingFile	File name (file is expected to contain at least 2+2*N2 columns).
N1, N2, p11, p12, p21, p22,	N1=number of pairs, see next; N2= ; Scaling is obtained from interpolation in column pi1 and applied to parameter pi2 of $AGSQUAD$.

• NT = 1.13: TO BE DOCUMENTED FURTHER.

```
someKEYWORD [someLABEL1]
1.13
```

NT can take negative values, then acting as a switch for various types of hard-coded function generators, as follows :

• NT = -1: this is convenient for synchrotron acceleration. In this case the next two lines both contain a single data (as for NT = 1), respectively the starting scaling factor value, and 1. The current field scaling factor will then be updated from the energy kick by the cavity if for instance *CAVITE/IOPT=2* is used, namely,

$$SCALE(N) = SCALE(N-1) * \frac{B\rho(N)}{B\rho(N-1)}$$

• NT = -2: allows reading an RF law (voltage, frequency, etc.) for *CAVITE* from an external data file. Useful for acceleration in fixed field rings for instance.

- NT = -60: field scaling follows $B\rho$ change by CAVITE, accounting for some starting value.
- NT = -77: field scaling law for FNAL proton driver to be documented.
- NT = -87: AGS tune-jump quadrupoles to be documented.

• NT = -88: AC dipole function generator. An AC dipole provides a bending field, thus for a magnetic dipole MULTIPOL can be used for instance, or BEND. Four values determine the functioning of this optical element : phase of the AC dipole; AC dipole tune Q1 at the start of the sweep; AC dipole tune Q2 at the end of the sweep; and a scale factor to be applied to the field.

Note that in the case of the previous example (assuming, though, that the ramping of the magnetic fields strictly follows the *CAVITE* kick, which was not strictly the case), the *SCALING* argument list can be simplified, including by suppressing '*CAVITE*' from the list, as follows :
SCALING	- Scaling Active $NF = 3$ families of elements are concerned, as listed below
OUADRUPO OFA OFB	- Ouadrupoles labeled 'OFA' and Ouadrupoles labeled 'OFB'
-1	(
18131.E-3	
1	
MULTIPOL QDA QDB	- Multipoles labeled 'QDA' and Multipoles labeled 'QDB'
-1	
18131.E-3	
1	
BEND	- All BENDs (regardless of any LABEL)
-1	
18131.E-3	
1	

Notes :

1. In causing, via *CAVITE*, a change of the synchronous rigidity, *SCALING* causes a change of the reference rigidity (Sec. 7.2), following (see *CAVITE*, p. 82)

 $B\rho_{ref} = BORO \longrightarrow B\rho_{ref} = BORO + \delta B\rho_s$

2. It may happen that some optical elements won't scale, for source code development or updating reasons. This should be paid attention to by preliminary simulation tests.

SCALING AND THE FIT PROCEDURE

Coupling variables

Because it applies a scaling factor to families of optical elements (as determined by their keyword and possible *LABEL1*, *LABEL2*), *SCALING* can be used to couple FIT variables.

Tunes and chromaticities

FIT can vary any numerical data under *SCALING*, this allows scaling fields in optical element families (by specifying one or more *LABEL1*s to address one or more families as described above). Examples are given in Tab. 2 (p. 163).

RECOVERING FROM A CRASH

When accelerating a bunch in a pulsed ring, *SCALING* is used to ramp magnetic fields, so following the rigidity increase by *CAVITE*. *CAVITE* may or may not be part of the *SCALING* argument list, see the two previous examples. Now, if the job stops during the multiturn tracking - due to computer crash or else - it is possible to resume the tracking from the latest records (in [b_]zboubi.fai storage file), using *OBJET*, *KOBJ*= 3. In the presence of acceleration using *CAVITE*, since there is no reference particle in **zgoubi**, *CAVITE* will read from [b_]zboubi.fai the reference rigidity at the corresponding time/turn when tracking crashed/resumes. Note that, as far as *CAVITE* is concerned, this recovery process in only installed for *CAVITE/Option=2*, a option often used for synchronous acceleration (recovery for additional *CAVITE* options can be added in cavite.f program).

SPACECHARG : Space charge

The keyword *SPACECHARG* enables (or disables) the calculation of space charge effects. It must be preceded by *PARTICUL* for definition of mass and charge values, as they enter in the definition of space charge parameters.

SPACECHARG is supposed to appear a first time at the location where space charge effects should start being taken into account, with the first data *LMNT* set to 'all' or a keyword.

SPACECHARG is supposed to appear a second time at the location where calculations should stop, with *LMNT* set to 'none'. It results in summary outputs in zgoubi.res.

Occurence of *PRINT* amongst *SPACECHARG* arguments results in storage of computational data and other relevant informations in zgoubi.SPACECHARG.out, as space charge computation proceeds.

SPNTRK : Spin tracking switch, and spin coordinate initialization

(page 326 in PART B)

The keyword *SPNTRK* allows switching spin tracking on (index *KSO*=1) or off (*KSO*=0), or resuming (index *KSO*=-1, following an occurrence *KSO*=0).

SPNTRK will also attribute initial spin coordinates to each one of the *IMAX* particles defined by *[MC]OBJET* (unless *OBJET[KOBJ=3]* is used, in which case the latter takes care of spin coordinates initialization). Initial spin coordinates depend on the option index *KSO*.

SPNTRK It must be preceded by PARTICUL for the definition of mass and gyromagnetic factor.

KSO = 1 (respectively 2, 3) : the *IMAX* particles defined with *[MC]OBJET* are given a longitudinal (1,0,0) spin component (respectively transverse horizontal (0,1,0), vertical (0,0,1)).

KSO = 4 : initial spin components are entered explicitly for each one of the *IMAX* particles of the beam.

KSO = 4.1 : three initial spin components S_X , S_Y , S_Z are entered explicitly just once, they are then assigned to each one of the *IMAX* particles of the beam.

KSO = 4.2: under development. Read spin components from a file, file name has to be provided. (that file at present can be zgoubi.res : KSO=4.2 looks for key "(deg) (deg)" that appears at start of the spin coordinates list under the keyword *SPNPRT*).

KSO = 5 : under development - to be completed in spn.f. Random generation of *IMAX* initial spin conditions as sketched in Fig. 46. Given a mean polarization axis (S) defined by its angles T_0 and P_0 , and a cone of angle A with respect to this axis, the *IMAX* spins are sorted randomly in a Gaussian distribution

$$p(a) = \exp\left[-\frac{(A-a)^2}{2\delta A^2}\right]/\delta A\sqrt{2\pi}$$

and within a cylindrical uniform distribution around the (S) axis. Examples of simple distributions available by this mean are given in Fig. 47.



Figure 46: Spin distribution as obtained with option KSO = 5. The spins are distributed within an annular strip δA (standard deviation) at an angle A with respect to the axis of mean polarization (\vec{S}) defined by T_0 and P_0 .



Figure 47: Examples of the use of KSO =5. A : Gaussian distribution around a mean vertical polarization axis, obtained with T_0 = arbitrary, $P_0 = \pi/2$, A = 0 and $\delta A \neq 0$. B : Isotropic distribution in the median plane, obtained with $P_0 = \pm \pi/2$, $A = \pi/2$, and $\delta A = 0$.

SRLOSS : Synchrotron radiation energy loss

The keyword *SRLOSS* allows activating or stopping (option KSR = 1, 0 respectively) stepwise tracking of energy loss by stochastic emission of photons in magnetic fields, following the method described in section 3.1[25].

It can be chosen to allow radiation in the sole dipole fields, or in all types of fields regardless of their multipole composition. It can also be chosen to allow for the radiation induced transverse kick (this is yet to be installed in the code - not done as it is generally considered a negligible effect).

SRLOSS must be preceded by *PARTICUL* for defining mass and charge values as they enter in the definition of SR parameters.

Statistics on SR parameters are computed and updated while tracking, the results of which can be obtained by means of the keyword *SRPRNT*.

SVDOC : SVD orbit correction

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The method is the following :

1. Reference trajectory (case of beam line) or orbit (case of periodic optical sequence - requires FIT[2], see below) : the initial coordinate(s) in OBJET are considered the reference(s) - multiple references are allowed, see below. A reference does not have to be zero, however, FIT can be used do find the reference orbit initial coordinates, in that case FIT should appear before *SVDOC* in the sequence. For instance, (i) in a spectrometer beam line, FIT would allow to determine the necessary initial coordinates (varied by *FIT*) for a particle with a given momentum to acquire some requested radial excursion as some requested location down the line (the constraint(s) in *FIT*); (ii) if the sequence is assumed periodic, *FIT* will find the closed orbit (possibly multiple closed orbits, *e.g.* in the case of a multiple-pass recirculating linac, or a fixed-field ring such as a cyclotron or FFAG). A practical example of periodic orbit finding using *FIT*[2] is given in PART B, page 339.

2. The algorithm computes the A matrix (in $A\vec{x} = \vec{y} - \vec{y_0}$, with x the correctors signal, y the pickups signal, $\vec{y_0}$ a reference PU signal - the reference orbit), by injecting a non-zero signal (angle) in each orbit corrector, one after the other successively, and saving the successive PU readings (as rows of the A matrix). There can be up to 20 different particles tracked (meaning 20 different reference orbits, and 20 times more columns (PUs) in A), each PU is "multiple-beam", capable of discriminating each orbit in the SVD process (case for instace of chromatic orbits, or multiple-pass ERL, or FFAG lattice).

3. The inverse matrix A^{-1} is computed and stored (logged to zgoubi.SVD.out).

4. Optionally, SVDOC can carry on with error trials, in the following way:

(i) apply the compensation signal (the SVD-inverted A^{-1} matrix) on the correctors,

(ii) apply orbit defects,

(iii) find the corrected [multiple-]orbit (logged to zgoubi.SVDOrbit.out),

(iv) repeat (ii)-(iv).

The method is the following for instance in the case of a periodic sequence:

- use *ERRORS* to activate orbit defects. Note that *ERRORS* must be set to OFF in the zgoubi sequence, as (i) the first pass through the sequence is used to determine the \vec{y}_0 reference orbit mentionned earlier (possibly using *FIT[2]*, placed at the end of the sequence), (ii) the ON/OFF switch in *ERRORS* is managed by *SVDOC* in this procedure;

- SVDOC the strength in the correctors that the SVD used is reset to zero;

- FIT[2] finds the orbit resulting from these defects, this orbit is recorded at the PUs that the SVD used;

- SVDOC then sets the strengths in the correctors, using the SVD matrix;

- *FIT[2]* finds the new orbit - presumably improved ! and delivers it (logged to zgoubi.SVDOrbits.out, together with the uncorrected orbit).

A typical way to use the orbit correction algorithm is the following:

```
Title. The 'OPTICAL SEQUENCE', below, is assumed periodic.
 'OBJET'
1000.000000
                            !
                                   reference rigidity (kG.cm)
2
1 1
0.E+00
              0.E+00 0.E+00 0.E+00 0. 1. 'o'
! Start OPTICAL SEQUENCE here
'Some vertical corrector beloging in 'VKIC' family
'MULTIPOL' VKIC
[MULTIPOL data list]
! Some zero-length horizontal BPM beloging in 'HMON' family
  'DRIFT'
                    HMON
0.0000
! End OPTICAL SEQUENCE here
 'FIT'
                    ! This finds the periodic orbit:
4
                    ! Variables:
1 30 0 [-.1,.1]
                               ! Vary Y0
! Vary T0
! Vary Z0
1 31 0 [-.1,.1]
1 32 0 [-.1,.1]
1 33 0 [-.1,.1] ! Vary PO
4 ! Constraints:
                               ! Vary PO
                                                       (default penalty=1e-10)

      3.1
      1
      2
      #End
      0.
      1.
      0
      !
      Yfinal
      =
      Y0

      3.1
      1
      2
      #End
      0.
      1.
      0
      !
      Tfinal
      =
      T0

      3.1 1 2 #End 0. 1. 0
      ! Tfinal = T0

      3.1 1 2 #End 0. 1. 0
      ! Zfinal = Z0

      3.1 1 2 #End 0. 1. 0
      ! Pfinal = P0

 'SVDOC'
1 0 zgoubi.SVDOrbits.out
                       SVDOrbits.out
/{VMON} ! Names of PU-H, -V, -HV families (max each =MPULAB/3=1).
/{VKIC} ! Name of corr-H, -V families; kick (rad).
=-3 ! Kick values for computation of svd matrix (rad).
! "1" triggers ERRORS; "2" data are changed prior to that, following 2 lines; 5 trials.
! parameter 12 in ERRORS: value of HKIC dipole field: will set H orbit,
! parameter 22 in ERRORS: value of VKIC dipole field: will set V orbit.

PUH {HMON } PUV {VMON }
CRH{HKIC} CRV{VKIC}
1.e-3
1 2 5
                   1e-3
ERRORS 12
ERRORS 22
! step 1: A^-1 is applied to correctors.
! Step 2: when back down to FIT (from here), FIT will get the corrected periodic orbit,
```

'END'

TO BE DOCUMENTED FURTHER

SYNRAD : Synchrotron radiation spectral-angular densities

The keyword *SYNRAD* enables (or disables) the calculation of synchrotron radiation (SR) electric field and spectral angular energy density. It must be preceded by *PARTICUL* for defining mass and charge values, as they enter in the definition of SR parameters.

SYNRAD is supposed to appear a first time at the location where SR should start being taken into account, with the first data KSR set to 1. It results in on-line storage of the electric field vector and other relevant quantities in zgoubi.sre, as step by step integration proceeds. The observer position (XO, YO, ZO) is specified next to KSR.

Data stored in zgoubi.sre :

(*ELx*, *ELy*, *ELz*) : electric field vector $\vec{\mathcal{E}}$ (eq. 3.2.1) (*btx*, *bty*, *btz*) = $\vec{\beta} = \frac{1}{c} \times$ particle velocity (*gx*, *gy*, *gz*) = $\frac{d\vec{\beta}}{dt}$ = particle acceleration (eq. 3.2.3) $\Delta \tau$ = observer time increment (eq. 3.2.2) $t' = \tau - r(t')/c$ = retarded (particle) time (*rtx*, *rty*, *rtz*) : $\vec{R}(t)$, particle to observer vector (eq. 3.2.4) (*x*, *y*, *z*) = particle coordinates Δs = step size in the magnet (fig. 2) *NS* = step number *I* = particle number *LET*(*I*) = tagging letter *IEX*(*I*) = stop flag (see section 7.12)

SYNRAD is supposed to appear a second time at the location where SR calculations should stop, with KSR set to 2. It results in the output of the angular energy density $\int_{\nu_1}^{\nu_2} \partial^3 W / \partial \phi \, \partial \psi \, \partial \nu$ (eq. 3.2.11) as calculated from the Fourier transform of the electric field (eq. 3.2.11). The spectral range of interest and frequency sampling (ν_1 , ν_2 , N) are specified next to KSR.

SYSTEM : System call

The keyword *SYSTEM* allows one or a series of system calls. It can appear anywhere, an arbitrary number of times, along the zgoubi.dat optical sequence. It is effective at the very location where it appears.

SYSTEM keyword is followed by the list of the desired system commands. That can be saving zgoubi output files, calling again **zgoubi** at the end of a run so allowing dependent consecutive jobs, etc.

EXAMPLES - Examples of the use of SYSTEM are given in pp. 274, 332.

6.5 Output Procedures

These procedures are dedicated to the storage or printing of particle coordinates, histograms, spin coordinates, etc. They may be called for at any spot in the data pile.

FAISCEAU, FAISCNL, FAISTORE : Print/Store particle coordinates

• FAISCEAU can be introduced anywhere along an optical sequence. It produces a print (into zgoubi.res) of initial and actual coordinates of the *IMAX* particles at the location where it stands, together tagging indices and letters, etc.

• FAISCNL is an older, less performing, version of FAISTORE, see below for the latter. It produces a lot more information on particles at current location, including spin components, decay distance, mass, charge, etc. (see list below), and stores it in a dedicated file FNAME (advised name is FNAME = 'zgoubi.fai' (formatted write) or 'b_zgoubi.fai' (binary write) if post-processing with **zpop** should follow). This file may further on be read by means of OBJET, option KOBJ= 3, or used for other purposes such as graphics (see Part D of the Guide).

The data written to that file are formatted and ordered according to the *FORTRAN* sequence in the subroutine impfai.f, where details and possible updates are to found. The following is an instance :

```
OPEN (UNIT = NL, FILE = FNAME, STATUS = 'NEW')
       IF (BINARY) THEN
         DO 2 I=1.IMAX
              P = BORO * CL9 * F(1, I) * AMQ(2, I)
             ENERG = SQRT (P*P + AMQ(1, I) * AMQ(1, I))
ENEKI = ENERG - AMQ(1, I)
              WRITE (NFAI)
             IEX(I),-1.D0+FO(1,I),(FO(J,I),J=2,MXJ),
-1.D0+F(1,I),F(2,I),F(3,I),(F(J,I),J=4,MXJ),
     1
                                                                                tag, initial D-1,Y,T,Z,P,S,Time
     2
                                                                                current D_i,Y,T,Z,P,S,Time
              (SI(J,I),J=1,4),(SF(J,I),J=1,4),
     >
                                                                                spin components, initial and current
              ENEKI, ENERG,
      >
                                                                                energy
      4
              I, IREP(I), SORT(I), (AMQ(J,I), J=1,5), RET(I), DPR(I), PS,
                                                                                particle#,loss S,mass,Q,G,life time
              BORO, IPASS, NOEL, KLEY, LBL1, LBL2, LET(I)
      5
                                                                                BORO, pass#,element#,keyword,labels
 2
         CONTINUE
      ELSE
         DO 1 I=1, IMAX
           P = BORO * CL9 * F(1, I) * AMQ(2, I)
           ENERG = SQRT (P*P + AMQ(1, I) * AMQ(1, I))
ENEKI = ENERG - AMQ(1, I)
           WRITE (NFAI, 110)
     1
           IEX(I),-1.D0+FO(1,I),(FO(J,I),J=2,MXJ),
           -1.D0+F(1,I),F(2,I),F(3,I),
(F(J,I),J=4,MXJ),
     2
      3
            (SI(J,I), J=1,4), (SF(J,I), J=1,4),
      4
      5
           ENEKI, ENERG,
           I, IREP(I), SORT(I), (AMQ(J,I), J=1,5), RET(I), DPR(I), PS,
      6
           BORO, IPASS, NOEL, KLEY, LBL1, LBL2, LET(I)
INCLUDE "FRMFAI.H"
         CONTINUE
 1
       ENDIF
          FORMAT(1X,
 110
C1
                    KEX,
                               XXXO, (FO(J, IT), J=2, MXJ)
        1P.
                   1X.I2.
                               7(1X,E16.8)
C2
                  XXX,Y,T*1.D3,
                  ,3(1X,E24.16)
C3
          Z,P*1.D3,SAR,TAR
          ,4(1X,E24.16)
      >
          SXO, SYO, SZO, SO, SX, SY, SZ, S
C4
          ,8(1X,E15.7)
C5
           ENEKT, ENERG
          .2(1X,E16.8)
          IT, IREP(IT),
                           SORT(IT), (AMQ(J,I), J=1,5), RET(IT), DPR(IT), PS
С6
                         9(1X,E16.8)
          ,2(1X,I6),
C7
            BORO,
                     IPASS, NOEL
          ,1X,E16.8, 2(1X,I6)
     >
С8
                'KLEY',
                            ('LABEL(NOEL,I)',I=1,2),
                                                                      'LET(IT)'
           ,1X,A1,A10,A1, 2(1X,A1,A,A1),
                                                                        1X, 3A1)
```

The meaning of the main data is the following (see the keyword OBJET)

LET(I)	: one-character string, for tagging particle number I
IEX, I, IREP(I)	: flag, particle number, index
FO(1-6, I)	: coordinates D, Y, T, Z, P and path length at the origin of the optical sequence
F(1-6, I)	: <i>idem</i> at the current position
SORT(I)	: path length at which the particle has possibly been stopped
	(see CHAMBR or COLLIMA)
RET(I), DPR(I)	: synchrotron phase space coordinates ; <i>RET</i> = phase (radian),
	DPR = momentum dispersion (MeV/c) (see CAVITE)
IPASS	: turn number (see REBELOTE)
etc.	:

• FAISTORE has an effect similar to FAISCNL, with more features.

- On the first data line, *FNAME* may be followed by a series of up to 10 *LABELs*. If there is no label, the print occurs by default at the location of *FAISTORE*; if there are labels the print occurs right downstream of all optical elements wearing those labels (and no longer at the *FAISTORE* location).

- The next data line gives a parameter, IP: printing will occur at pass 1 and then at every IP other pass, if using REBELOTE with NPASS $\geq IP - 1$.

For instance the following data list in zgoubi.dat :

FAISTORE zgoubi.fai HPCKUP VPCKUP 12

will result in output prints into zgoubi.fai, at pass 1 and then every 12 other pass, each time elements of the zgoubi.dat optical sequence labeled either *HPCKUP* or *VPCKUP* are encountered.

Case of Binary storage : it can be obtained from *FAISCNL* and *FAISTORE*. This is for the sake of compactness and access speed, for instance in case voluminous amounts of data would have to be manipulated using **zpop**.

This is achieved by giving the storage file a name of the form *b_FNAME* or *B_FNAME* (*e.g.*, 'b_zgoubi.fai'). The FORTRAN WRITE list is the same as in the FORMATTED case above.

This is compatible with the READ statements in **zpop** that will recognize binary storage from that very radical 'b_' or 'B_'.

Case of FIT[2] procedure : it may not be desired to store during the FITting process, but instead only when the FITtinig is completed. It is sufficient for that to (i) put 'AtFITfinal' as the first label following *FAISTORE* keyword, this will inhibit all storage until the final run following a FIT procedure, and (ii) avoid using the 'nofinal' instruction in *FIT[2]* (see p. 164)).

FOCALE, IMAGE[S] : Particle coordinates and beam size ; localization and size of horizontal waist

FOCALE calculates the dimensions of the beam and its mean transverse position, at a longitudinal distance XL from the position corresponding to the keyword FOCALE.

IMAGE computes the location and size of the closest horizontal waist.

IMAGES has the same effect as *IMAGE*, but, in addition, for a non-monochromatic beam it calculates as many waists as there are distinct momenta in the beam, provided that the object has been defined with a classification of momenta (see *OBJET*, *KOBJ*= 1, 2 for instance).

Optionally, for each of these three procedures, **zgoubi** can list a trace of the coordinates in the X, Y and in the Y, Z planes.

The following quantities are calculated for the N particles of the beam (IMAGE, FOCALE) or of each group of momenta (IMAGES)

• Longitudinal position :

FOCALE:
$$X = XL$$

$$IMAGE[S]: X = -\frac{\sum_{i=1}^{N} Y_i * \operatorname{tg} T_i - \left(\sum_{i=1}^{N} Y_i * \sum_{i=1}^{N} \operatorname{tg} T_i\right) / N}{\sum_{i=1}^{N} \operatorname{tg}^2 T_i - \left(\sum_{i=1}^{N} \operatorname{tg} T_i\right)^2 / N}$$

$$Y = Y_1 + X * \operatorname{tg} T_1$$

where Y_1 and T_1 are the coordinates of the first particle of the beam (*IMAGE*, *FOCALE*) or the first particle of each group of momenta (*IMAGES*).

• Transverse position of the center of mass of the waist (*IMAGE[S]*) or of the beam (*FOCALE*), with respect to the reference trajectory

$$YM = \frac{1}{N} \sum_{i=1}^{N} (Y_i + X tgT_i) - Y = \frac{1}{N} \sum_{i=1}^{N} Y M_i$$

• FWHM of the image (IMAGE[S]) or of the beam (FOCALE), and total width, respectively, W and WT

$$W = 2.35 \left(\frac{1}{N} \sum_{i=1}^{N} Y M_i^2 - Y M^2 \right)^{\frac{1}{2}}$$
$$WT = \max(YM_i) - \min(YM_i)$$

FOCALEZ, IMAGE[S]Z : Particle coordinates and beam size ; localization and size of vertical waist

Similar to FOCALE and IMAGE[S], but the calculations are performed with respect to the vertical coordinates Z_i and P_i , in place of Y_i and T_i .

HISTO : 1-D histogram

Any of the coordinates used in **zgoubi** may be histogrammed, namely initial Y_0 , T_0 , Z_0 , P_0 , S_0 , D_0 or current Y, T, Z, P, S, D particle coordinates (S = path length ; D may change in decay process simulation with *MCDESINT*, or when ray-tracing in \vec{E} fields), and also spin coordinates and modulus S_X , S_Y , S_Z and $\|\vec{S}\|$.

HISTO can be used in conjunction with *MCDESINT*, for statistics on the decay process, by means of *TYP*. *TYP* is a onecharacter string. If it is set equal to 'S', only secondary particles (they are tagged with an 'S') will be histogrammed. If it is set equal to 'P', then only parent particles (non-'S') will be histogrammed. For no discrimination between S-econdary and P-arent particles, TYP = 'Q' must be used.

The dimensions of the histogram (number of lines and columns) may be modified. It can be normalized with NORM = 1, to avoid saturation.

Histograms are indexed with the parameter *NH*. This allows making independent histograms of the same coordinate at several locations along an optical sequence. This is also useful when piling up problems in a single input data file (see also *RESET*). *NH* is in the range 1-5.

If *REBELOTE* is used, the statistics on the 1+*NPASS* runs through the optical sequence will add up.

PRINT : The optional command 'PRINT', under *HISTO* keyword, will cause logging of computation outcomes in the file zgoubi.HISTO.Out.

IMAGE[S][Z] : Localization and size of vertical waists

See FOCALE[Z].

MATRIX : Calculation of transfer coefficients, periodic parameters

(page 291 in PART B)

MATRIX allows computation of transport matrices through the optical sequence up to third order, from *OBJET* down to the location(s) where *MATRIX* is introduced in the optical sequence (which can be at arbitrary locations), or, upon option, down to the horizontal focus closest to *MATRIX* keyword. In the latter case the position of the focus is calculated automatically in the same way as the position of the waist in *IMAGE*.

An automatic generation of an appropriate object for the use of *MATRIX* can be obtained from the procedure *OBJET* (pages 61, 297), as follows:

- if IORD = 1, use $OBJET(KOBJ = 5[.N, 2 \le N \le 99])$, that generates up to 99*13 initial coordinate sets (Y, T, Z, P, S, D). Up to 99 transport matrices are computed, each one *wrt*. to the reference trajectory of concern (trajectory number 1, 14, 27, ..., (13 N-12), respectively).

- if IORD = 2, use OBJET(KOBJ = 6) that generates 61 initial coordinate sets.
- if IORD = 3, use OBJET(KOBJ = 6.1) that generates 102 initial coordinate sets.

The different procedures available are as follows:

- If *IORD* = 0, *MATRIX* is inhibited (equivalent to *FAISCEAU*, whatever *IFOC*).
- If IORD = 1, using OBJET, KOBJ = 5[.N], the first order transport matrix $[R_{ij}]$ is calculated, from a third order approximation on the coordinates. For instance

$$Y^{+} = \left(\frac{Y}{T_{0}}\right) T_{0} + \left(\frac{Y}{T_{0}^{2}}\right) T_{0}^{2} + \left(\frac{Y}{T_{0}^{3}}\right) T_{0}^{3} + \mathcal{O}(T_{0}^{4}), \qquad Y^{-} = -\left(\frac{Y}{T_{0}}\right) T_{0} + \left(\frac{Y}{T_{0}^{2}}\right) T_{0}^{2} - \left(\frac{Y}{T_{0}^{3}}\right) T_{0}^{3} + \mathcal{O}(T_{0}^{4})$$

will yield, neglecting third order terms,

$$R_{11} \approx \left(\frac{Y}{T_0}\right) = \frac{Y^+ - Y^-}{2T_0}$$

Matrix computation is repeated N times if OBJET, $KOBJ = 5.N (2 \le N \le 99)$ is used, so delivering a first order transport matrix for each 13-particle subset, with for each subset the reference trajectory being trajectory number $1+(N-1)\times 13$ (FAISCEAU will print out the N×13 particle list in zgoubi.res, if desired).

In the particular case *KOBJ* = 5.1, MATRIX will also transport optical functions:

- this requires the initial optical function values

$$\alpha_{Y,Z}, \alpha_{Y,Z}, D_{Y,Z}, D'_{Y,Z},$$
 at OBJET

to be provided, by OBJET;

- then, using the $[R_{ij}]$ matrix above, optical functions and phase advances ϕ_Y , ϕ_Z are transported following

$$\begin{pmatrix} \beta \\ \alpha \\ \gamma \end{pmatrix}_{at \; MATRIX} = \begin{pmatrix} R_{11}^2 & -2R_{11}R_{12} & R_{12}^2 \\ -R_{11}R_{21} & R_{12}R_{21} & R_{11}R_{12} \\ R_{21}^2 & -2R_{21}R_{22} & R_{22}^2 \end{pmatrix} \begin{pmatrix} \beta \\ \alpha \\ \gamma \end{pmatrix}_{at \; OBJET}$$

$$\phi_{Y} = A \tan \frac{R_{12}}{\frac{R_{12}}{2}} \quad \Delta \phi_{Z} = A \tan \frac{R_{34}}{\frac{R_{34}}{2}} \quad (651)$$

$$\Delta\phi_Y = A \tan \frac{R_{12}}{(R_{11}\beta_{Y,objet} - R_{12}\alpha_{Y,objet})}, \quad \Delta\phi_Z = A \tan \frac{R_{34}}{(R_{33}\beta_{Z,objet} - R_{34}\alpha_{Z,objet})}, \quad (6.5.1)$$

 $\phi_{Y,Z} \rightarrow \phi_{Y,Z} + 2\pi$ if $\phi_{Y,Z} < 0$, given $[0,\pi]$ Atan determination

Outcomes are printed in zgoubi.res, and as well in zgoubi.MATRIX.out ancillary output file *iff PRINT* is part of *MATRIX* arguments.

- If IORD = 2, using OBJET, KOBJ = 6, fifth order Taylor expansions are used for the calculation of the first order transport matrix $[R_{ij}]$ and of the second order matrix $[T_{ijk}]$. Other higher order coefficients are also calculated.
- If *IORD* = 3, using *OBJET*, *KOBJ* = 6.1, transport coefficients up to 3rd order are computed (after routines developed for the RAYTRACE computer code [72, 73]).

The next option, IFOC, acts as follows

- If *IFOC* = 0, the transport coefficients are calculated at the location of *MATRIX*, and with respect to the reference trajectory. For instance, Y^+ and T^+ above are defined for particle number *i* as $Y^+ = Y^+(i) - Y(\text{ref.})$, and $T^+ = T^+(i) - T(\text{ref.})$.
- If *IFOC* = 1, the transport coefficients are calculated at the horizontal focus closest to *MATRIX* (determined automatically), while the reference direction is that of the reference particle. For instance, Y^+ is defined for particle number *i* as $Y^+ = Y^+(i) Y_{\text{focus}}$, while T^+ is defined as $T^+ = T^+(i) T(\text{ref.})$.
- If *IFOC* = 2, no change of reference frame is performed : the coordinates refer to the current frame. Namely, $Y^+ = Y^+(i)$, $T^+ = T^+(i)$, etc.

Periodic Optical Sequences

• If *IFOC* = 10 + *NPeriod*, then, from the 1-turn transport matrix as obtained in the way described above, *MATRIX* calculates periodic parameters characteristic of the optical sequence such as optical functions and tune numbers, assuming that it is *NPeriod*-periodic. In the coupled hypothesis (default), the computation uses the Edwards-Teng method [42]. In non-coupled hypothesis (this requires "*uncoupled*" argument, see below), this is performed by a simple identification

$$[T_{ij}] = I \, \cos \mu + J \, \sin \mu$$

Matrix computation is repeated N times if OBJET, KOBJ = 5.N ($2 \le N \le 99$) is used, so delivering first order data for each of the $N \times 13$ -particle sets.

If IORD = 2 (using OBJET, KOBJ = 6) additional periodic parameters are computed such as chromaticities, momentum dependence of optical functions, etc.

PRINT : Addition of "*PRINT*" following *IORD*, *IFOC* will cause stacking of *MATRIX* output data into zgoubi.MATRIX.out file (convenient for use with *e.g.* gnuplot type of data treatment software).

Addition of "uncoupled" next to IORD, IFOC [, PRINT], in the case of periodic beam matrix request (i.e., IFOC = 10 + NPeriod) will cause use of uncoupled formalism.

About the source code :

The program matric computes the transport matrix coefficients, it is called by zgoubi when the keyword *MATRIX* is met along the zgoubi.dat sequence. matimp, called by matric, ensures the print out of the matrix (and possibly the beam matrix) in zgoubi.res, and upon '*PRINT*' option in zgoubi.MATRIX.out as well.

PICKUPS : Bunch centroid path; orbit

PICKUPS computes the average values of the coordinates of the particles in a bunch (coordinates of the bunch centroid) at one or more keywords specified by their *LABELs*. The list of *LABEL*(s) concerned is specified by the user, as part of the arguments under the keyword *PICKUPS*.

In conjunction with *REBELOTE* in the case of a periodic optical sequence, with *REBELOTE* thus being used to cause multi-turn tracking, *PICKUPS* are reset (their records are zero-ed) at start of each turn.

Pickup data computed during **zgoubi** execution are stored in the file zgoubi.PICKUP.out, usable for further analysis, or for plotting (for instance, using gnuplot).

A summary of the list of pickups and their individual bunch data is listed in the result file zgoubi.res (below the *END* keyword) at the end of **zgoubi** execution. It is concluded with statistics as the *rms*, minimum and maximum values of the bunch centroid data over the ensemble of pickups.

PLOTDATA : Intermediate output for the PLOTDATA graphic software

PLOTDATA was at the origin implemented for the purpose of plotting particle coordinates using the TRIUMF PLOTDATA package [74]. However nothing precludes using it with a different aim.

The *PLOTDATA* keyword can be introduced at up to 20 locations in zgoubi.dat. There, particle coordinates will be stored in a local array, FF. They are overwritten at each pass. Usage of FF is left to the user, see *FORTRAN* subroutine pltdat.f.

SPNPRNL, SPNSTORE : Print/Store spin coordinates

• SPNPRNL has similar effect to SPNPRT (page 202), except that the information is stored in a dedicated file FNAME (should post-processing with **zpop** follow, advised name is FNAME = 'zgoubi.spn' (formatted write) or 'b_zgoubi.spn' (binary write)). The data are formatted and ordered according to the FORTRAN sequence found in the subroutine spnprn.f, with meaning of printed quantities as follows :

LET(I),IEX(I)	: tagging character and flag (see OBJET)
SI(1-4,I)	: spin components SX , SY , SZ and modulus, at the origin
SF(1-4,I)	: <i>idem</i> at the current position
GAMMA	: Lorentz relativistic factor
Ι	: particle number
IMAX	: total number of particles ray-traced (see OBJET)
IPASS	: turn number (see REBELOTE)

• SPNSTORE has an effect similar to SPNPRNL, with two more features.

- On the first data line, *FNAME* may be followed by a series of up to 10 *LABELs* proper to the elements of the zgoubi.dat data file at the exit of which the print should occur; if no label is given, the print occurs by default at the very location of *SPNSTORE*; if labels are given, then print occurs right downstream of all optical elements wearing those labels (and no longer at the *SPNSTORE* location).

- The next data line gives a parameter, IP: printing will occur every IP other pass, when using REBELOTE with NPASS $\geq IP - 1$.

For instance the following data input in zgoubi.dat :

SPNSTORE zgoubi.spn HPCKUP VPCKUP 12

will result in output prints into zgoubi.spn, every 12 other pass, each time elements of the zgoubi.dat optical sequence labeled either *HPCKUP* or *VPCKUP* are encountered.

Note

Binary storage can be obtained from *SPNPRNL* and *SPNSTORE*. This is for the sake of compactness and I/O access speed by zgoubi or zpop, for instance in case voluminous amounts of data should be manipulated.

This is achieved by giving the storage file a name of the form *b_FNAME* or *B_FNAME* (*e.g.*, 'b_zgoubi.spn'). The FORTRAN WRITE output list is the same as in the FORMATTED case above.

SPNPRT : Print spin coordinates

(page 325 in PART B)

SPNPRT can be introduced anywhere in an optical sequence. It produces a print out (to zgoubi.res by default) of various informations such as the initial and actual coordinates and modulus of the spin of the *IMAX* particles, their Lorentz factor γ , the mean values of the spin components, etc., at the location where it is placed in the zgoubi.dat optical sequence.

PRINT : If "*PRINT*" appears after *SPNPRT*, then spin data will be stored in zgoubi.SPNPRT.Out. The latter is opened at the first occurence of "*PRINT*". In particular, if *REBELOTE* is used then data will be stacked in zgoubi.SPNPRT.Out.

MATRIX : If "*MATRIX*" appears after *SPNPRT*, then spin rotation matrix (or matrices) will be computed. This is done assuming that appropriate initial particle and spin sampling has been defined (by respectively *OBJET* and *SPNTRK*), as follows :

- three particles are needed for *SPNPRT* to compute a spin matrix. All three have identical initial coordinates (for instance in a periodic optical sequence, the local stable precession axis coordinates) and rigidity, and their spins are on a direct triedra, for instance, respectively,

$$(S_X, S_Y, S_Z) = (1, 0, 0), (0, 1, 0), (0, 0, 1),$$

- there may be several groups of three particles, each group with a particular rigidity (*i.e.*, the three particles in a group have the same momentum). OBJET with *KOBJ=1* or *KOBJ=2* can be used for instance to generate these particles by groups of like rigidity. *SPNPRT*[*MATRIX*] will thus compute as many matrices.

An example of spin matrix computation is given page 325.

SRPRNT : Print SR loss statistics

SRPRNT may be introduced anywhere in an optical sequence. It allows switching on synchrotron radiation energy loss computation. It produces in addition a print out (to zgoubi.res) of current state of statistics on several parameters related to SR loss presumably activated beforehand with keyword *SRLOSS*.

TWISS : Compute periodic optical parameters. Log to zgoubi.TWISS.out

TWISS causes the calculation of transport coefficients and various other global parameters, in particular periodical quantities as tunes and optical functions, in the coupled hypothesis. *TWISS* is normally placed at the end of the optical sequence ; it causes a succession of up to 5 passes through the sequence (it performs a do-loop indeed, by sending the program execution pointer back to the top of the input data file, up to 4 successive times).

The object necessary for these calculations will be generated automatically if one uses *OBJET* with option *KOBJ*= 5. This requires knowledge of the reference orbit, as coordinates of trajectory number 1 of the 13-set defined by *OBJET[KOBJ=5]* have to be on the periodic orbit (trajectory number 1 is the reference for transport coefficient calculation).

FIT may precede TWISS in case the periodic orbit coordiantes at the begining of the sequence are not known, for an automatic search, see example in PART. B, p. 339.

TWISS works in a way similar to *MATRIX*, iterating the *MATRIX* process wherever necessary, changing for instance the reference trajectory in *OBJET* for dp/p related computations. In particular :

- It assumes that the reference particle (particle #1 of 13, when using *OBJET[KOBJ=5]*) is located on the closed orbit. *This condition has to be satisfied for TWISS to work consistently*, because *TWISS* does not look for the closed orbit by itself. A simple way to first find the orbit is to have *TWISS* preceded by a dedicated *FIT[2]*, see example in PART B, page 338.

- A first pass (the only one if KTW=1) through the optical sequence allows computing the periodic optical functions at the end of the sequence, from the rays.

- The periodic dispersions from the first pass are used to define chromatic closed orbits at $\pm \delta p/p$ (or at $\pm FacD \times \delta p/p$, accounting for a user's parameter $FacD \neq 1$). A second and a third pass (which terminate the process if *KTW=2*) with chromatic objects centered respectively on $\pm \delta p/p$ chromatic orbits will then compute the chromatic first order transport matrices. From these the chromaticities are deduced. Full accuracy on the chromatic orbits can be obtained using *FIT[2]*.

- Anharmonicities need two additional passes (which terminate the process if KTW=3). They are deduced from the difference in tunes for particles tracked on different transverse invariants, horizontal or vertical.

The execution of *TWISS* will cause printout to the file zgoubi.TWISS.out, a MADX type "twiss" file, with similar formatting, including periodic optical data as a header (tunes, chromaticities, etc.) and, in sequence element by element : optical functions, element strength, first order transport coefficients, spin \vec{n}_0 vector (requires 'SPNTRK' request).

SR Integrals, DK Spin Integrals

Presence of "SRINT" in *TWISS* arguments will cause computation of Synchrotron radiation integrals, which will then be added to zgoubi.TWISS.out header. Presence of "DKINT" in *TWISS* arguments will cause computation of Derbenev-Kondratenko integrals, which will then be added to zgoubi.TWISS.out header. In the case SR and/or DK spin integrals are requested, they are computed along particle number 1 trajectory, it is the responsibility of the user to ensure that particle number 1 is on the closed orbit, and the DK spin integrals case to ensure in addition that its initial spin coordinates in *SPNTRK* are on the spin closed orbit.

SR and DK spin integrals are computed step by step; all optical elements contribute (not just dipoles) as long as trajectory number 1 experiences $1/\rho \neq 0$.

About the source code :

The program beamat ensures the transport of the beam matrix along the zgoubi.dat sequence, at the orgin of the content of zgoubi.TWISS.out. beamat is called by opticc, itself called after each optical element, in the program zgoubi.

The starting beam matrix value is in the array FI, initialized by the program twiss when met at the end of the zgoubi.dat sequence. The array F0 contains the running beam matrix.

The program optimp, called from opticc, prints to zgoubi.TWISS.out after each optical element of the zgoubi.dat sequence.

7 COMPLEMENTS REGARDING VARIOUS FUNCTIONALITIES

7.1 Units in zgoubi

Units to be employed in **zgoubi** input data list (in zgoubi.dat) are stated in Part B of this guide. Part B should be carefully referred to about units to be used, when setting up the data list, as some insight in the code indicates :

Working units in **zgoubi** numerical integrator, and as to the normalized fields delivered to the integrator, satisfy to the following (in particular, whatever the units in the input data file, as listed in Part B, quantities of concern end up manipulated as follows) :

- position coordinates (X, Y, Z, S) in centimeter,
- angle coordinates (T, P) in radian,
- time in μ second,
- energy in MeV,
- magnetic field in kG
- electrostatic field in MV/cm
- rigidity $B\rho$ in kG.cm,
- fields delivered to the integration procedure after convertion to strengths, units of $m^{-\rm integer}$, for instance,
 - magnetic dipole strength $(B/B\rho = 1/\rho)$ is in m^{-1} (with B the field),
 - 2(n+1) order magnetic multipol strengths ($(B/R^n)/B\rho$, n=1 (quadrupole), n=2 (sextupole), etc.) are in $m^{-(n+1)}$ (with B the field at pole tip radius R),
 - etc.,
 - 2(n+1) order magnetic multipol strengths $((\Phi/R^{(n+1)})/W)$, n=1 (quadrupole), n=2 (sextupole), etc) are in $m^{-(n+1)}$ (with Φ the potential (in Volt) at pole tip radius R and W the kinetic energy of the particle (in electron-Volt)).

For historical reasons, since **zgoubi** was first developed in 1972, implementation of optical elements (as listed in Part B) has resulted in parameter definition resorting to a wide variety of units. For instance :

- element lengths in meter or centimeter,
- positioning angles in rad, mrad, degree,
- magnetic fields in Tesla or kGauss,
- electrostatic potentials in Volt, MVolt,
- electrostatic fields in Volt/m, V/cm, MVolt/m,
- etc.

7.2 Reference Rigidity

zgoubi computes the strengths of optical elements (they are usually defined by their field) from the reference rigidity *BORO* as defined in *[MC]OBJET*. However using *CAVITE*, and indirectly *SCALING*, may affect the reference rigidity, following

$$B\rho_{ref} = BORO \longrightarrow B\rho_{ref} = BORO + \delta B\rho_s \tag{7.2.1}$$

with $\delta B\rho_s$ increase (or decrease) of the reference rigidity. A typical configuration where this would occur is that of multi-turn tracking in a pulsed synchrotron (see section 7.8), where in general optical element strengths have to follow the acceleration so that the orbit and lattice optics remain unchanged.

7.3 Reference Trajectory, Closed Orbit

Various procedures in **zgoubi** assume prior knowledge of a reference orbit. Or the closed orbit, in the case of an optical sequence assumed to be periodic. This is the case for instance for *MATRIX*, for *TWISS*, when searching the spin closed orbit, when multi-turn tracking an initially centered bunch (see also p. 86), etc.

The initial coordinates of that reference trajectory are specified in *[MC]OBJET*. Initial spin coordinates are specified in *SPNTRK*. They may possibly be found by a prior *FIT[2]* (with for instance "3.1" or "10.1" style periodicity constraints, in the case of a periodic sequence or in the case of a closed spin orbit, respectively).

In the case of the *MATRIX* and *TWISS* procedures, both keywords can be preceded with *FIT[2]* for that purpose of prior finding of the reference trajectory or closed orbit, or spin closed orbit.

7.4 Time Varying Fields

Fields can be varied as a function of time (in some cases this may mean as a function of turn number, see section 7.8), by means of the *SCALING* keyword.

Eventually some families of magnets may be given a different timing law for the simulation of special processes (*e.g.*, time varying orbit bump, fast crossing of spin resonances with families of jump quadrupoles).

7.5 Backward Ray-Tracing

For the purpose of parameterization for instance, it may be interesting to ray-trace backward from the image toward the object. This can be performed by first reversing the position of optical elements in the optical sequence, and then reversing the integration step sign in all the optical elements.

An illustration of this feature is given in the following Figure 48.



Figure 48: A. Regular forward ray-tracing, from object to image. B. Same optical sequence, with backward ray-tracing from image to object : negative integration step XPAS is used in the quadrupole.

7.6 Checking Trajectories and Fields Across Optical Elements - the IL, .plt and IC flags

• In all optical elements, an option IL is available. It is normally set to IL = 0 and in this case has no effect. Other possibilities are as follows :

- IL = 1 causes a print in zgoubi.res of particle coordinates, fields and low-order derivatives, spin vector and other data, at each integration step along trajectories across the optical element. In the meantime, a calculation and summation of the values of $\nabla \cdot \vec{B}$, $\nabla \times \vec{B}$ and $\nabla^2 \vec{B}$ (same for \vec{E}) at all integration steps is performed, which allows a check of the behavior of \vec{B} (and/or \vec{E}) in field maps (all these derivatives should normally be zero).

- IL = 2 causes a print of particle data (coordinates, \vec{B} and/or \vec{E} field(s) experienced, RF cavity related data, spin, etc.), particle status (*e.g.*, decay status, whether it is still tracked, etc.), into the dedicated file zgoubi.plt, one line of data per article, at each integration step. This information can further be processed (using **zpop**¹⁴ or gnuplot, for instance). In order to minimize the volume of that storage file (when dealing with small step size, long optical elements, large number of particles, etc.) it is possible to print out every other 10^n integration step by taking $IL = 2 \times 10^n$ instead (for instance, IL = 200 would cause output into zgoubi.plt every 100 other step).

- IL = 7 causes similar outputs to IL = 1, and more, in particular derivatives to higher order, yet into the dedicated file zgoubi.impdev.out, one line of data per particle, at each integration step. This information can be further plotted (*e.g.*, using **zpop**, or gnuplot). An example is given in fig. 49, a plot of the quadrupole and sextupole field indices along the reference orbit in a combined function main dipole pertaining to the AGS lattice [75].

• *IL* can be forced to the aforementioned values, in all optical elements at once, by means of *OPTIONS*.

• The '.plt' flag can be added as a second LABEL in the case of MARKER or DRIFT keywords. It comes in complement to IL = 2 as the latter is not available (actually: IL=2 is available in DRIFT in the presence of the 'split' flag, see page 106), to log local coordinates to zgoubi.plt in the same manner as IL=2 does.

• *IC*: When dealing with field maps (*e.g.*, *CARTEMES*, *ELREVOL*, *TOSCA*), an option index *IC* is available. It is normally set to IC = 0 and in this case has no effect. Other possibilities are as follows :

- IC = 1 causes a print of the field map in zgoubi.res.

- IC = 2 will cause a print of the field map into the file zgoubi.map which can further be processed with **zpop** for plotting, superimposing trajectories, and other data treatment purposes.

7.7 Labeling Keywords: LABEL1, LABEL2

Keywords in **zgoubi** input data file zgoubi.dat can be *LABEL*'ed, for the purpose of the execution of such procedures as *REBE-LOTE*, *PICKUPS*, *FAISCNL*, *FAISTORE*, *SCALING*,. And also for the purpose of particle coordinate storage into zgoubi.plt (see section 7.6, IL = 2 option).

¹⁴See Part D of the Guide.



Figure 49: Typical field and derivatives - here, along the 10 GeV proton orbit across an AGS A-type main magnet. Derivatives are obtained from second degree polynomial interpolation from the magnet measured field map. Left : $dB_Z(s)/dY$ and $dB_Y(s)/dZ$, right : $d^2B_Y(s)/dZdY$, $d^2B_Y(s)/dYdZ$. These data were stored in zgoubi.impdev.out during execution, by stating IL = 7 under TOSCA keyword.

A keyword in zgoubi.dat accepts two *LABELs* normally referred to as *LABEL1*, *LABEL2*. The first one is used for the above mentioned purposes. An instance of the use of the second one is with *MARKER* or with *DRIFT* : it can be set to ".plt" for storage of current particle data into zgoubi.plt. The keyword and its *LABEL*[s] should fit within a 110-character long string on a single line (a quantity set in the *FORTRAN* file prdata.f).

7.8 Multi-turn Tracking in Circular Machines

Multi-turn tracking in circular machines can be performed by means of the keyword *REBELOTE*. *REBELOTE* is introduced in the zgoubi.dat optical sequence with its argument NPASS + 1 being the number of turns to be performed. It will cause a jump of the execution pointer back to (details on page 175), either the beginning of zgoubi.dat data list (default case), or to a particular *LABEL* in that list. From there on, tracking resumes down to *REBELOTE* again, and so forth until the requested number of passes has been reached. At that point, the execution simply continues beyond *REBELOTE* down to the *END* keyword.

Note : Some *CAVITE* options cause a reset-to-zero of individual particle path length¹⁵. This is for reasons of cumulated path length accuracy (a delta-path below computer accuracy compared to total path length would not be resolved - it can be for instance bunch length as compared to cumulated multi-turn distance around a large ring). This reset may not be desirable, it depends on the multi-turn problem dealt with using *REBELOTE*, it may be necessary for instance in long-term tracking in large rings, it is not in recirculating linacs. Option K=99 in *REBELOTE* will cause this reset, whereas option K=98 (UNDER DEVELOPMENT, IN cavite.f, IN THIS VERSION OF THE CODE) will avoid it, with everything else the same as with K=99.

Possible magnet timing laws B(T) during the multi-turn process (with T = 1 to NPASS+1 counted in number of turns) can be introduced by means of SCALING.

In order that the *IMAX* particles of the beam start a new pass with the coordinates they had reached at the end of the previous one, the option K = 99 has to be specified in *REBELOTE*.

Synchrotron acceleration can be simulated, using following the procedure :

- CAVITE appears in the zgoubi.dat optical sequence (normally before REBELOTE), with option $IOPT \neq 0$,
- the RF frequency of the cavity may be given a timing law $f_{RF}(T)$ by means of SCALING, family CAVITE,
- the magnets are given a field timing law B(T), (with T = 1 to NPASS+1 counted in number of turns) by means of SCALING.

Eventually some families of magnets may be given a different timing law for the simulation of special processes (*e.g.*, time varying orbit bump, fast crossing of spin resonances with families of jump quadrupoles).

7.9 KPOS : Positioning, (Mis-)Alignment, of Optical Elements and Field Maps

The last record in most optical elements and field maps is the positioning option KPOS. KPOS is followed by the positioning parameters.

In most optical elements it operates as follows:

- either XCE, YCE for translation and ALE for Z-rotation, if the optical element is defined in a Cartesian frame (O; X, Y, Z),

- or *RE*, *TE* entrance radius and Z-rotation (E stands for the French "Entree") and similar *RS*, *TS* at exit (S stands for the French "Sorti e"), if the optical element is defined in a cylindrical frame $(O; R, \theta, Z)$.

¹⁵For the geek: the "f(6,I)=0.d0" statements in cavite.f.

The positioning works in two different ways, depending whether the element is defined in Cartesian (X, Y, Z) coordinates (*e.g.*, *QUADRUPO*, *TOSCA*[*MOD* \leq 19]), or polar (*R*, θ , *Z*) coordinates (*e.g.*, *DIPOLE*, *TOSCA*[*MOD* \geq 20], *POLARMES*).

ERRORS allows random misaligmenet of some magnets¹⁶.

Additional possibilities are available in some other optical elements, see below.

Cartesian Coordinates :

If KPOS = 1, the optical element is moved (shifted by XCE, YCE and Z-rotated by ALE) with respect to the incoming reference frame. Trajectory coordinates after traversal of the element refer the element frame.

If KPOS= 2, the shifts XCE and YCE, and the tilt angle ALE are taken into account, for mis-aligning the element with respect to the incoming reference, as shown in Fig. 50. The effect is equivalent to a CHANGREF(XCE, YCE, ALE) upstream of the optical element, followed by CHANGREF(XCS, YCS, ALS = -ALE) downstream of it, with computed XCS, YCS values as schemed in Fig. 50.

KPOS = 3 option is available for some optical elements defined in a Cartesian frame (*e.g.*, *BEND*, *MULTIPOL*, *AGSMM*); it is effective only if a non zero dipole component B1 is present, or if *ALE* is non-zero. It positions automatically the magnet in a symmetric manner with respect to the incoming and outgoing reference axis, convenient for periodic optical sequences, as follows (Fig 51).

Both incoming and outgoing reference frames are tilted w.r.t. the magnet,

• either, by an angle ALE if ALE $\neq 0$,

• or, if ALE=0 by half the Z-rotation $\alpha_Z/2$ such that $L = 2 \frac{BORO}{B1} \sin(\alpha_Z/2)$, wherein L = geometrical length, BORO = reference rigidity as defined in [MC]OBJET.

Next, the optical element is Y-shifted by $\delta Y = YCE$ (*XCE* is not used) in a direction orthogonal to the new magnet axis (*i.e.*, at an angle $ALE + \pi/2$ wrt. the X axis of the incoming reference frame).



Figure 50: Case of Cartesian frame optical element. Left : positioning an optical element using KPOS = 1. Right : Mis-aligning an optical element using KPOS = 2. (X_E, Y_E) and (X_S, Y_S) are respectively the incoming and outgoing reference frames.

KPOS = 4 is UNDER DEVELOPMENT. It has been introduced for AGSMM keyword (AGS main magnet), it is used in the on-line AGS model at BNL. It also applies to MULTIPOL. It orients the magnet in a way similar to KPOS = 3, with reference frame Z-rotated by $\alpha_Z/2$ as drawn from $L = 2 \frac{BORO}{B1} \sin(\alpha_Z/2)$.

However it provides additional magnet mis-alignments (alignment errors) (Fig. 52) : Z-rotation θ_Z , Z-shift δZ , Y-rotation θ_Y . Rotations apply at the center of the magnet.

Note that some of these features may not be properly operational due to on-going developments: check before use.

KPOS = 5 is UNDER DEVELOPMENT. It is similar to KPOS = 4, with a different ordering of the offset data list. It allows X-, Y- and Z-offset, as well as X-, Y- and Z-rotation in that order. Note that some of these features may not be properly operational due to on-going developments: check before use.



Figure 51: Alignment in *BEND* by half the deviation, $\alpha_Z/2$, using *KPOS* = 3. (X_E, Y_E) and (X_S, Y_S) are respectively the incoming and outgoing reference frames. Trajectory coordinates inside the magnet are defined in the magnet frame, (X_{ME}, Y_{ME}) .



Figure 52: Additional magnet mis-alignement with KPOS=4.

Polar Coordinates

If KPOS = 1, the element is positioned automatically in such a way that a particle entering with zero initial coordinates and $1 + DP = B\rho/BORO$ relative rigidity will reach position $(RM, \frac{AT}{2})$ in the element with T = 0 angle with respect to the moving frame in the polar coordinates system of the element; see *DIPOLE-M* and *POLARMES*).

If KPOS = 2, the map is positioned in such a way that the incoming reference frame is presented at radius RE with angle TE. The exit reference frame is positioned in a similar way with respect to the map, by means of the two parameters RS (radius) and TS (angle) (see Fig. 20 page 96).

7.10 Coded Integration Step

In several optical elements (*e.g.*, all multipoles, *BEND*) the integration step (in general noted *XPAS*) can be coded under the form XPAS = #E | C | S, with E, C, S integers, E is the number of steps in the entrance fringe field region, C is the number of steps in the magnet body, and S is the number of steps in the exit fringe field region.

7.11 Ray-tracing of an Arbitrarily Large Number of Particles

Monte Carlo multi-particle simulations involving an arbitrarily large number of particles can be performed using *MCOBJET* together with *REBELOTE*, put at the end of the optical sequence, with its argument *NPASS* being the number of passes through *REBELOTE*, and (*NPASS*+1) * *IMAX* the number of particles to be ray-traced. In order that new initial conditions (D, Y, T, Z, P, X) be generated at each pass, K = 0 has to be specified in *REBELOTE*.

Statistics on coordinates, spins, and other histograms can be performed by means of such procedures as *HISTO*, *SPNTRK*, etc. that stack the information from pass to pass.

7.12 Stopped Particles : The IEX Flag

As described in *OBJET*, each particle I = 1, *IMAX* is attached a value IEX(I) of the *IEX* flag. Normally, IEX(I) = 1. Under certain circumstances, *IEX* may be changed to a negative value by **zgoubi**, as follows.

- -1: the trajectory happened to wander outside the limits of a field map
- -2: too many integration steps in an optical element (a quantity controlled in MXSTEP. H include file)
- -3: deviation happened to exceed $\pi/2$ in an optical element not designed to allow that
- -4 : stopped by walls (procedures CHAMBR, COLLIMA)
- -5 : too many iterations in subroutine depla.f
- -6 : energy loss exceeds particle energy
- -7~ : field discontinuities larger than 50% within a field map
- -8 : reached field limit in an optical element
- -9 : particle not accounted for
- -10 : secondary particle has decayed (whatever that means...)
- -11 : particle moves backward upon decay

Only in the case IEX = -1 will the integration not be stopped since in this case the field outside the map is extrapolated from the map data, and the particle may possibly get back into the map (see section 1.4.2 on page 30). In all other cases the particle will be stopped.

7.13 Negative Rigidity

zgoubi can handle negative rigidities $B\rho = p/q$. This is equivalent to considering either particles with negative charge (q < 0) or momentum (p < 0), or reversed fields (*wrt*. the field sign that shows in the zgoubi.dat optical element data list).

Negative rigidities may be specified in terms of BORO < 0 or $D = B\rho/BORO < 0$ when defining the initial coordinates with *OBJET* or *MCOBJET*.

7.14 Fiel maps

Field maps read by dedicated keywords as TOSCA, CARTEMES, POLARMES, etc., may have, and in some cases must have a header. The header is a series of comment ligns, say N lines. The default value is N=8. If a field map with $N \neq 8$ is to be used, this need be specified in the field map title, as part of the "TITL" comment (see TOSCA or other field map keyword about TITL) under the form 'HEADER_N' with $N \geq 0$ placed anywhere within the TITL comment area.

8 ZGOUBI OUTPUT FILES

Running zgoubi always creates a default zgoubi.res file. The name can be changed by resorting to the argument -out (or -fileOut or >). In the same manner that the input data file name can be changed (the default is zgoubi.dat) by means of -in (or -fileIn or <).

Additional output files can be obtained, upon request:

- zgoubi.plt (using *IL=2* in one or more optical elements);
- zgoubi.impdev.out (using *IL*=7 in one or more optical elements);
- a copy of current zgoubi executable (launch zgoubi execution with argument -saveExec);
- a copy of current zpop executable (launch zgoubi execution with argument -saveZpop: this garantees
- availability of a version of zpop compatible with the current formatting of zgoubi outputs which zpop reads).

Some keywords produce, by default, one ore more specific output files, in principle in order to allow subsequent user's data treatment/analysis, namely,

file	KEYWORD[OPTION]	comment
zgoubi.consty.out	OPTIONS[CONSTY]	
zgoubi.fai	FAISCNL or FAISTORE	
zgoubi.FITVALS.out	FIT[SAVE]	name can be different, if specified
zgoubi.FIT.out.dat	FIT	a copy of zgoubi.dat sequence with updated variable values once FIT is over
zgoubi.IDLUNI.out	OPTIONS[MONITOR]	
zgoubi.SVD.out	SVDOC	
zgoubi.SVDOrbits.out	SVDOC	
zgoubi.SVD_PuCoList.out	SVDOC	
zgoubi.TWISS.out	TWISS	has similar content formatting to that of the MADX twiss command output file

- in several keyword cases, a listing specific of the computations undergone in that keyword can be obtained by means of a PRINT comment, or by means of a specific argument in their data list. The idea behind that feature is to allow checks or some level of debugging, and anyway these outputs can readily be used for plotting, with gnuplot for instance (like, particle RF phase, or boost, versus turn number from zgoubi.CAVITE.Out, histograms from zgoubi.HISTO.out, etc., *confer* next sections). The output files name is of the form zgoubi.XXX.out or zgoubi.XXX.Out, "XXX" is in general the keyword itself, or close. Here is a list as of May 2020 (may not be exhaustive, a 'grep "zgoubi.*.out" [pathTo]/zgoubi/*f' or 'grep "zgoubi.*.Out" [pathTo]/zgoubi/*f' would tell):

file	KEYWORD[OPTION]	comment
zgoubi.CAVITE.Out	CAVITE[PRINT]	
zgoubi.COLLIMA.out	COLLIMA [IA=2]	
zgoubi.ERRORS.out	ERRORS[PRINT]	
zgoubi.HISTO.out	HISTO[PRINT]	
zgoubi.MATRIX.out	MATRIX[PRINT]	
zgoubi.OPTICS.out	OPTICS[PRINT]	
zgoubi.PICKUP.out	PICKUPS[PRINT]	
zgoubi.SCALING.Out	SCALING[PRINT]	
zgoubi.SPNPRT.Out	SPNPRT[PRINT]	
zgoubi.SRLOSS.Out	SRLOSS[PRINT]	

8.1 zgoubi.res

Running zgoubi always creates a default zgoubi.res file. This is a listing of the program execution, the listing follows the zgoubi.dat sequence ... in sequence!

It is recommended to keep an eye in zgoubi.res when running a problem, it contains a lot of informations regarding what happened, numerical results, etc. That's the first place to lookup in case of a crash.

8.2 zgoubi.fai

Table 3: A list of the 46 parameters characterizing a particle and the current status of its ray tracing, as printed out to zgoubi.fai when the execution pointer meets *FAISTORE* or *FASICNL*. Zgoubi.fai displays these 46 parameters under the form of as many columns, one line per particle. The particle coordinate frame is the (O;X,Y,Z) Cartesian frame defined in Fig. 1, including T and P angles therein.

column	parameter	unit or	what's that
number	name	nature	
1	KEX	int	IEX flag. Set to 1 by [MC]OBJET. Set to negative value when particle has an accident
2	Do-1	float	$(B\rho - BORO)/BORO$, at [MC]OBJET (BORO: see 37)
3	Yo	cm	horizontal position, at [MC]OBJET
4	То	mrd	horizontal angle, at [MC]OBJET
5	Zo	cm	vertical position, at [MC]OBJET
6	Ро	mrd	vertical angle, at [MC]OBJET
7	So	cm	longitudinal distance, at [MC]OBJET
8	to	$\mu { m s}$	time, at [MC]OBJET
9	D-1	float	$(B\rho - BORO)/BORO$, current
10	Y	cm	horizontal position, current
11	Т	mrd	horizontal angle, current
12	Z	cm	vertical position, current
13	Р	mrd	vertical angle, current
14	S	cm	longitudinal distance, current
15	t	$\mu { m s}$	time, current
16	SXo	float	X spin component, at genesis by SPNTRK
17	SYo	float	Y spin component, at genesis by SPNTRK
18	SZo	float	Z spin component, at genesis by SPNTRK
19	modSo	float	spin vector modulus, at genesis by SPNTRK
20	SX	float	X spin component, current
21	SY	float	Y spin component, current
22	SZ	float	Z spin component, current
23	modS	float	spin vector modulus, current
24	ENEKI	MeV	kinetic energy
25	ENERG	MeV	total energy
26	IT	int	particle number
27	IREP	int	flag - more or less obsolete
28	SORT	cm	distance at which particle got lost
29	М	MeV/c2	mass
30	Q	С	charge
31	G	float	anomalous magnetic moment
32	tau	float	life time
33	unused	float	
34	RET	float	$\phi - \phi_{\text{synch}}$, phi_{synch} = synchronous phase. Set by CAVITE
35	DPR	float	$(p - p_{synch})/p_{synch}$, p_{synch} = synchronous momentum. Set by CAVITE
36	PS	float	synchronous momentum, possibly subject to updating, by CAVITE for intance
37	BORO	kG.cm	BORO \equiv reference $B\rho$, set by [MC]OBJET
38	IPASS	int	pass number (incremented by REBELOTE)
39	NOEL	int	element number in the zgoubi.dat sequence (as shown in zgoubi.res)
40	KLEY	string	previous keyword
41	LABEL1	string	label 1 of the previous keyword
42	LABEL2	string	label 2 of the previous keyword
43	LET	string	particle tag
44	SRloss	MeV	cumulatied synchrotron radiation energy loss
45	DPREF-[DPREF]	MeV	fractional part of the current synchronous momentum p_{synch} (see 36)
46	[DPREF]	MeV	integer part of the current synchronous momentum p_{synch} (see 36)

Examples;

- horizontal phase space (analogous to (x,x') in matrix transport notations): (Y,T), *i.e.*, columns (10,11),

- vertical phase space (analogous to (y,y') in matrix transport notations): (Y,T), *i.e.*, columns (12,13),

- longitudinal phase space (analogous to $(\delta\phi, \delta p/p)$ in matrix transport notations): (RET,DPR), *i.e.*, columns (34,35),

- postion as a function of distance along a beam line, or turn by trun around a ring: horizontal Y(S), *i.e.*, columns (10,14); vertical Z(S), *i.e.*, columns (12,14).

8.3 zgoubi.plt

Table 4: A list of the 50 parameters characterizing a particle and the current status of its ray tracing, during the step by step integration across an optical element, as printed out to zgoubi.plt when the execution pointer meets IL=2. Particles are pushed one by one all the way through, so, if it takes N steps for particle number 1 to cross, then the N first lines all concern particle 1, and so on. Zgoubi.plt displays thes 50 parameters under the form of as many columns, one line at each integration step. The particle coordinate frame (O;X,Y,Z) is (i) either Cartesian as sketched in Figs. 1, 53 (case optical elements defined in a Cartesian frame), (ii) or cylindrical, and in that case with Y the radius and X the polar angle (case of optical elements defined in a cylindrical frame, Fig. 53).

column	parameter	unit or	what's that
number	name	nature	
1	KEX	int	IEX flag. Set to 1 by [MC]OBJET. Set to negative value when particle has an accident
2	Do-1	float	$(B\rho - BORO)/BORO$, at [MC]OBJET (BORO: see 37)
3	Yo	cm	horizontal position, at [MC]OBJET
4	То	mrd	horizontal angle, at [MC]OBJET
5	Zo	cm	vertical position, at [MC]OBJET
6	Ро	mrd	vertical angle, at [MC]OBJET
7	So	cm	longitudinal distance, at [MC]OBJET
8	to	$\mu { m s}$	time, at [MC]OBJET
9	D-1	float	$(B\rho - BORO)/BORO$, current
10	Y-DY	cm	transverse horizontal coordinate if Cartesian frame, radius if cylindrical. Normally DY=0
11	Т	mrd	horizontal angle (in the moving frame if cylindrical), current
12	Z	cm	vertical position, current
13	Р	mrd	vertical angle, current
14	S	cm	longitudinal distance, current
15	time	$\mu { m s}$	time, current
16	beta	-	v/c
17	DS	cm	step size
18	KART	int	current frame either Cartesian (KART=1) or cylindrical (KART=2)
19	IT	int	particle number
20	IREP	int	flag - more or less obsolete
21	SORT	cm	distance at which particle got lost
22	Х	cm	X coordinate if Cartesian frame, polar angle if cylindrical (positive clockwise) (Fig. 53)
23	BX	kG	X component of magnetic field, current
24	BY	kG	Y component of magnetic field, current
25	BZ	kG	Z component of magnetic field, current
26	RET	float	$\phi - \phi_{\text{synch.}}, phi_{\text{synch.}} = \text{synchronous phase. Set by CAVITE}$
27	DPR	float	$(p - p_{\text{synch.}})/p_{\text{synch.}}$, $p_{\text{synch.}}$ = synchronous momentum. Set by CAVITE
28	PS	float	synchronous momentum, possibly subject to updating, by CAVITE for intance
29	SXo	float	X spin component, at genesis by SPNTRK
30	SYo	float	Y spin component, at genesis by SPNTRK
31	SZo	float	Z spin component, at genesis by SPNTRK
32	modSo	float	spin vector modulus, at genesis by SPNTRK
33	SX	float	X spin component, current
34	SY	float	Y spin component, current
35	SZ	float	Z spin component, current
36	modS	float	spin vector modulus, current
37	EX	V/m	X component of electric field, current
38	EY	V/m	Y component of electric field, current
39	EZ	V/m	Z component of electric field, current
40	BORO	kG.cm	BORO \equiv reference $B\rho$, set by [MC]OBJET
41	IPASS	int	pass number (incremented by REBELOTE)
42	NOEL	int	element number in the zgoubi.dat sequence (as shown in zgoubi.res)
43	KLEY	string	current keyword
44	LABEL1	string	label 1 of the current keyword
45	LABEL2	string	label 2 of the current keyword
46	LET	string	particle tag
47	NITR	int	fit procedure: iteration number
48	MXIT	int	fit procedure: max. allowed number of iterations
49	FIT#	int	fit procedure: number
50	FITLST	int	fit procedure: final pass afetr FIT, 0/1 (Y/N)

Examples;

- vertical magnetic field component as a function of distance: BZ(S), columns (25,14),

- vertical position as a function of turn number: Z(IPASS), columns (12,41),

- vertical position as a function of turn distance: Z(S), columns (12,14).

- horizontal position (or radial excursion R-RM) as a function of optical element number in zgoubi.dat sequence: Y(NOEL), columns (10,42).



Figure 53: Coordinates, in zgoubi.plt, of a particle at location M along its trajectory in a (O;X,Y,Z) frame; Z is normal to the (X,Y) plane, pointing out of the page. In these graphs, the dashed curve is the projection of the trajectory in the (X,Y) plane, m is the projection of M. Top: case of an optical element (figured as a rectangular box) in which the field is defined in a Cartesian coordinate system (case for instance of *MULTIPOL*, *BEND*, *TOSCA*[MOD \leq 19]). Bottom: case of an optical element (figured as an angular sector AT, with a reference radius RM) in which the field is defined in a cylindrical coordinate system (case of *DIPOLE* for instance, Fig. 20); in that case X denotes the polar angle, counted positive clockwise

8.4 zgoubi.TWISS.out

column	parameter	unit or	what's that
number	name	nature	
1	alfx	next 6 cols.: Y, Z and s optical functions	
2	btx		
3	alfy		
4	bty		
5	alfl		
6	btl		
7	Dx	next 4 cols.: dispersion function	
8	Dxp		
9	Dy		
10	Dyp		
11	phix/2pi	Y-motion phase advances	
12	phiy/2pi	Z-motion phase advances	
13	sum_s	cumulative length of optical elements (erroneous if field maps used)	
14	#lmnt	lement number	
15	Х	Y orbit	
16	xp	T orbit angle	
17	У	Z orbit	
18	ур	P orbit angle	
19	KEYWORD		
20	label1		
21	label2		
22	FO(6,1)	initial (at [MC]OBJET) path distance of particle 1	
23	K0*L	integrated field of preceding optical element	
24	K1*L	integrated K1 of preceding optical element	
25	K2*L	integrated K2 of preceding optical element	
26	—C—	coupling coefficient	
27	r	coupling coefficient	
28	!		
29	optimp.f		
30	IPASS	pass number	
31	DPREF	integer part of reference dp/p (=PS / P0 -HDPRF)	
32	HDPREF	fractional part of reference dp/p (= INT(PS / P0))	
33	R11	next 13 cols.: first order transport coefficients, from begining of the sequence	
34	R12		
35	R21		
36	R22		
37	R33		
38	R34		
39	R43		
40	R44		
41	R51		
42	R52		
43	R53		
44	R54		
45	R56		
46	F61	path distance of particle 1	
47	SX	X spin components	
48	SY	Y spin components	
49—	SZ	Z spin components	
50	—S—	spin vector modulus	
51	Length	length of preceding optical element	
52	Deviation	orbital deviation by preceding optical element	
Examples;			

Table 5: A list of the parameters characterizing the optics at the exit of optical elements, as produced by TWISS keyword.

- vertical magnetic field component as a function of distance: BZ(S), columns (25,14),

- vertical position as a function of turn number: Z(IPASS), columns (12,41),

- vertical position as a function of turn distance: Z(S), columns (12,14).

- horizontal position (or radial excursion R-RM) as a function of optical element number in zgoubi.dat sequence: Y(NOEL), columns (10,42).
PART B

Keywords and input data formatting

Glossary of Keywords, Part B

Keywords : how to format their input data list

AGSMM	AGS main magnet	. 227
AGSQUAD	AGS quadrupole	228
AIMANT	Generation of dipole mid-plane 2-D map, polar frame	. 229
AUTOREF	Transport beam into a new reference frame	233
BEAMBEAM	Beam-beam lens	234
BEND	Bending magnet, Cartesian frame	235
BETATRON	Betatron core (momentum kick)	237
BINARY	BINARY↔FORMATTED data converter	.238
BREVOL	1-D uniform mesh magnetic field map	. 239
CARTEMES	2-D Cartesian uniform mesh magnetic field map	. 240
CAVITE	Accelerating cavity	. 242
CHAMBR	Long transverse aperture limitation	. 244
CHANGREF	Transformation to a new reference frame	245
CIBLE	Generate a secondary beam following target interaction	246
COLLIMA	Collimator	. 247
CYCLOTRON	Spiral setor cyclotron	248
DECAPOLE	Decapole magnet	. 251
DIPOLE	Dipole magnet, polar frame	252
DIPOLE-M	Generation of dipole mid-plane 2-D map, polar frame	. 254
DIPOLES	Dipole magnet N-tuple, polar frame	.256
DODECAPO	Dodecapole magnet	257
DRIFT	Field free drift space	. 258
EBMULT	Electro-magnetic multipole	. 259
EL2TUB	Two-tube electrostatic lens	261
ELCYLDEF	Electrostatic cylindrical deflector	263
ELMIR	Electrostatic N-electrode mirror/lens, straight slits	262
ELMIRC	Electrostatic N-electrode mirror/lens, circular slits	264
ELMULT	Electric multipole	265
ELREVOL	1-D uniform mesh electric field map	266
EMMA	2-D Cartesian or cylindrical mesh field map for EMMA FFAG	. 267
END	End of input data list	.272
ESL	Field free drift space	. 258
ERRORS	Injecting errors in optical elements	. 268
FAISCEAU	Print particle coordinates	. 269
FAISCNL	Store particle coordinates in file FNAME	269
FAISTORE	Store coordinates every <i>IP</i> other pass at labeled elements	. 269
FFAG	FFAG magnet, N-tuple	270
FFAG-SPI	Spiral FFAG magnet, N-tuple	271
FIN	End of input data list	.272
FIT,FIT2	Fitting procedure	273
FOCALE	Particle coordinates and horizontal beam size at distance XL	. 278
FOCALEZ	Particle coordinates and vertical beam size at distance XL	278
GASCAT	Gas scattering	. 279
GETFITVAL	Get values of variables as saved from former FIT[2] run	. 280
GOTO	Branching statement	. 283

HALBACH	Halbach style permanent magnet	283
HELIX	Helical dipole	283
HISTO	1-D histogram	284
IMAGE	Localization and size of horizontal waist	285
IMAGES	Localization and size of horizontal waists	285
IMAGESZ	Localization and size of vertical waists	285
IMAGEZ	Localization and size of vertical waist	285
INCLUDE	File include statement	.286
MAP2D	2-D Cartesian uniform mesh field map - arbitrary magnetic field	288
MAP2D-E	2-D Cartesian uniform mesh field map - arbitrary electric field	289
MARKER	Marker	290
MATRIX	Calculation of transfer coefficients, periodic parameters	291
MCDESINT	Monte-Carlo simulation of in-flight decay	292
MCOBJET	Monte-Carlo generation of a 6-D object	293
MULTIPOL	Magnetic multipole	296
OBJET	Generation of an object	297
OBJETA	Object from Monte-Carlo simulation of decay reaction	300
OCTUPOLE	Octupole magnet	301
OPTICS	Write out optical functions. Log to zgoubi.OPTICS.out	302
OPTIONS	Global or special options	303
ORDRE	Taylor expansions order	304
PARTICUL	Particle characteristics	305
PICKUPS	Bunch centroid path; orbit	306
PLOTDATA	Intermediate output for the PLOTDATA graphic software	307
POISSON	Read magnetic field data from POISSON output	308
POLARMES	2-D polar mesh magnetic field map	309
PS170	Simulation of a round shape dipole magnet	310
QUADISEX	Sharp edge magnetic multipoles	311
QUADRUPO	Quadrupole magnet	312
REBELOTE	'Do it again'	314
RESET	Reset counters and flags	316
SCALING	Power supplies and R.F. function generator	317
SEPARA	Wien Filter - analytical simulation	318
SEXQUAD	Sharp edge magnetic multipole	319
SEXTUPOL	Sextupole magnet	320
SOLENOID	Solenoid	.321
SPACECHARG	Space charge	.322
SPINR	Spin rotation	323
SPNPRNL	Store spin coordinates into file FNAME	324
SPNSTORE	Store spin coordinates every <i>IP</i> other pass at labeled elements	.324
SPNPRT	Print spin coordinates	325
SPNTRK	Spin tracking switch, and spin coordinate initialization	326
SKLUSS	Synchrotron radiation energy loss	327
SKPKNI	PTINI SK IOSS Statistics	328
SVDUU	Symphratron radiation spactral angular densities	329
51NKAU Svstem	System call	221
SISIENI TADCET	Constants a secondary been following torget interaction	221
IAKGEI TOSCA	2 D and 2 D Cartagian or onlindrical mach field man	240 222
IUSUA TDANGMAT	2-D and 5-D Cartesian of cynnufical mesh field map	220
Ι ΚΑΝΟΙΛΙΑΙ ΤΟ ΔΟΛΤ	IVIAUIA UAIISICI	227
I KAKUI TWISS	Compute pariodia aptical parameters. Log to zeoubi TWICS out	220
1 1/122	Compute periodic optical parameters. Log to zgoubl. 1 w155.001	228

UNDULATOR	Undulator magnet	340
UNIPOT	Unipotential cylindrical electrostatic lens	341
VENUS	Simulation of a rectangular shape dipole magnet	342
VFFA	Simulation of a VFFA dipole, or series of	343
WIENFILT	Wien filter	344
YMY	Reverse signs of Y and Z reference axes	345

Optical Elements Versus Keywords

What can be simulated What keyword(s) can be used for that

This glossary gives a list of keywords suitable for the simulation of common optical elements. These are classified in three categories: magnetic, electric and combined electro-magnetic elements.

Field map procedures are also listed; they provide a means for ray-tracing through measured or simulated electric and/or magnetic fields.

MAGNETIC ELEMENTS

AGS main magnet	AGSMM
Betatron core	BETATRON, CAVITE
Cyclotron magnet or sector	DIPOLE[S], DIPOLE-M, FFAG, FFAG-SPI
Decapole	DECAPOLE, MULTIPOL
Dipole[s], spectrometer dipole	AIMANT, BEND, DIPOLE[S][-M], MULTIPOL, QUADISEX
Dodecapole	DODECAPO, MULTIPOL
FFAG magnets	DIPOLES, FFAG, FFAG-SPI, MULTIPOL
Helical dipole	HELIX
Multipole	MULTIPOL, QUADISEX, SEXQUAD
Octupole	OCTUPOLE, MULTIPOL, QUADISEX, SEXQUAD
Quadrupole	QUADRUPO, MULTIPOL, SEXQUAD, AGSQUAD
Sextupole	SEXTUPOL, MULTIPOL, QUADISEX, SEXQUAD
Skew multipoles	MULTIPOL
Solenoid	SOLENOID
Undulator	UNDULATOR

Using field maps

1-D, cylindrical symmetry	BREVOL
2-D, mid-plane symmetry	CARTEMES, POISSON, TOSCA
2-D, no symmetry	MAP2D
2-D, polar mesh, mid-plane symmetry	POLARMES
3-D, no symmetry	TOSCA
EMMA FFAG quadrupole doublet	EMMA
linear composition of field maps	TOSCA

ELECTRIC ELEMENTS

2-tube (bipotential) lens	EL2TUB
3-tube (unipotential) lens	UNIPOT
Decapole	ELMULT
Dipole	ELMULT
Dodecapole	ELMULT
Multipole	ELMULT
N-electrode mirror/lens, straight slits	ELMIR
N-electrode mirror/lens, circular slits	ELMIRC
Octupole	ELMULT
Quadrupole	ELMULT
R.F. (kick) cavity	CAVITE
Sextupole	ELMULT
Skew multipoles	ELMULT

Using field maps

1D, cylindrical symmetry	ELREVOL
--------------------------	---------

2-D, no symmetry

ELECTRO-MAGNETIC ELEMENTS

DipoleEBMULTDodecapoleEBMULTMultipoleEBMULTOctupoleEBMULTQuadrupoleEBMULTSextupoleEBMULTSkew multipolesEBMULTWien filterSEPARA, WIENFIL	Decapole	EBMULT
DodecapoleEBMULTMultipoleEBMULTOctupoleEBMULTQuadrupoleEBMULTSextupoleEBMULTSkew multipolesEBMULTWien filterSEPARA, WIENFIL	Dipole	EBMULT
MultipoleEBMULTOctupoleEBMULTQuadrupoleEBMULTSextupoleEBMULTSkew multipolesEBMULTWien filterSEPARA, WIENFIL	Dodecapole	EBMULT
OctupoleEBMULTQuadrupoleEBMULTSextupoleEBMULTSkew multipolesEBMULTWien filterSEPARA, WIENFIL	Multipole	EBMULT
QuadrupoleEBMULTSextupoleEBMULTSkew multipolesEBMULTWien filterSEPARA, WIENFIL	Octupole	EBMULT
SextupoleEBMULTSkew multipolesEBMULTWien filterSEPARA, WIENFIL	Quadrupole	EBMULT
Skew multipolesEBMULTWien filterSEPARA, WIENFIL	Sextupole	EBMULT
Wien filter SEPARA, WIENFIL	Skew multipoles	EBMULT
	Wien filter	SEPARA, WIENFILT

INTRODUCTION

Here after is given a detailed description of input data formatting and units. All available keywords appear in alphabetical order.

Keywords are read from the input data file by an unformatted *FORTRAN READ* statement. They be enclosed between quotes (*e.g.*, '*DIPOLE*').

Text string data such as comments or file names, are read by formatted READ statements, no quotes should be used in that case.

Numerical variables and indices are read by unformatted READ. It may therefore be necessary that integer variables be assigned an integer value.

In the following tables

- the first column shows the expected input parameters (actually, their values are expected), indices and text strings,
- the second column gives brief comments regarding their meaning and use,
- the third column gives the units or ranges,
- the fourth column indicates whether the expected parameter types are integer (I), real (E) or text string (A). For example, "I, 3*E" means that one integer followed by 3 reals is expected. "A80" means that a text string of maximum 80 characters is expected.

Keywords and input data formatting

AGSMM	AGS main magnet	(page 67 in PART A	A)
IL	$IL = 1, 2[\times 10^n], 7$: print coordinates, fields, etc., step-by-step, in zgoubi.res (1), zgoubi.plt (2), zgoubi.impdev.out (7).	$0-2[imes 10^n], 7$	Ι
$MOD, dL, R_0, dB1, dB2, dB3$	Type of magnet model ¹ ; unused ; pole tip radius, 10 cm if set to zero ; relative error on dipole, quadrupole, sextupole component.	2*no dim, cm, 3*no dim	I[.I], 5*E
NBLW[.MOD], NBLW times : NW, I	Number of back-leg windings [back-leg winding model ²]; for each back-leg winding : number of windings, current.	≤2, <i>NBLW</i> × (any, Amp.)	I, <i>NBLW</i> × (I, E)
X_E, λ_E, E_2, E_3	Entrance face Integration zone ; fringe field extent : dipole fringe field extent = λ_E ; quadrupole fringe field extent = $\lambda_E * E_2$; sextuppole fringe field extent = $\lambda_E * E_3$ (sharp edge if field extent is zero)	2*cm, 2*no dim	4*E
<i>NCE</i> , $C_0 - C_5$	same as QUADRUPO	0-6, 6*no dim	I, 6*E
X_S, λ_S, S_2, S_3	Exit face Integration zone ; as for entrance	2*cm, 2*no dim	4*E
$NCS, C_0 - C_5$		0-6, 6*no dim	I, 6*E
<i>R</i> 1, <i>R</i> 2, <i>R</i> 3	Skew angles of field components	3*rad	10*E
XPAS	Integration step	cm	Е
If KPOS = 1-3 <i>KPOS, XCE, YCE, ALE</i>	Positioning as follows : KPOS=1 : element aligned ; $KPOS=2$: misaligned ; shifts, tilt ; $KPOS=3$: effective only if $B1 \neq 0$: entrance and exit frames are tilted wrt. the magnet by an angle of • either ALE if ALE $\neq 0$ • or 2 Arcsin($B1 XL / 2BORO$) if ALE=0	1-3, 2*cm, rad	I, 3*E
If KPOS = 4 <i>KPOS</i> , XS, YS, ZR, ZS, YR	X-, Y-shift, Z-rotation, Z-shift, Y-rotation	4. cm. 2*(cm. rad)	L 5*E
11 00, 10, 10, 20, 1K	Automatic ZR-positioning (as for ALE in case <i>KPOS</i> =3).	i, ein, 2 (ein, iau)	1,5 Ц

¹*MOD*=1 : centered multipole model ;

MOD=2 : long-shifted dipole model ;

MOD=3 : short-shifted dipole model.

 $^{2}MOD = 0$ (default): user defined back-leg windings (defined in routine agsblw.f);

MOD = 1: actual AGS data are taken, namely : MM_A16AD : NBLW = 1, SIGN = 1.D0, NW = 10 ; MM_A17CF : NBLW = 1, SIGN = 1.D0, NW = 10 ; MM_A18CF : NBLW = 1, SIGN = -1.D0, NW = 10 ; MM_A19BD : NBLW = 1, SIGN = -1.D0, NW = 12 ; MM_A20BD : NBLW = 1, SIGN = 1.D0, NW = 12 ; MM_B02BF : NBLW = 2, SIGN = 1.D0, NW = 12, SIGN = 1.D0, NW = 6 ; MM_B03CD : NBLW = 1, SIGN = -1.D0, NW = 10 ; MM_B04CD : NBLW = 1, SIGN = -1.D0, NW = 10 ; MM_B05A : NBLW = 1, SIGN = -1.D0, NW = 10 ; MM_K19BD : NBLW = 1, SIGN = 1.D0, NW = 6 ; MM_K20B : NBLW = 1, SIGN = -1.D0, NW = 6 ; MM_K20B : NBLW = 1, SIGN = -1.D0, NW = 6 ; MM_K20B : NBLW = 1, SIGN = -1.D0, NW = 5 ; MM_A07CD : NBLW = 1, SIGN = -1.D0, NW = 5 ; MM_A07CD : NBLW = 1, SIGN = -1.D0, NW = 5 ; MM_A07CC : NBLW = 1, SIGN = -1.D0, NW = 5 ; MM_A14C : NBLW = 1, SIGN = -1.D0, NW = 5 ; MM_A15A : NBLW = 1, SIGN = -1.D0, NW = 5 ; MM_E07CD : NBLW = 1, SIGN = -1.D0, NW = 5 ; MM_E06A : NBLW = 1, SIGN = -1.D0, NW = 5 ; MM_F01BF : NBLW = 1, SIGN = -1.D0, NW = 5 ; MM_F008F : NBLW = 1, SIGN = -1.D0, NW = 5 ; MM_F01BF : NBLW = 1, SIGN = -1.D0, NW = 5 ; MM_G09BF : NBLW = 1, SIGN = -1.D0, NW = 5 ; MM_F15AD : NBLW = 1, SIGN = -1.D0, NW = 5 ; MM_G09BF : NBLW = 1, SIGN = -1.D0, NW = 6.

AGSQUAD	AGS quadrupole			
		dim.	data type	FIT num.
IL	$IL = 1, 2[\times 10^n], 7$: print coordinates, fields, etc., step-by-step, in zgoubi.res (1), zgoubi.plt (2), zgoubi.impdev.out (7).	$0-2[\times 10^n], 7$	Ι	
$\begin{aligned} &XL, R_0, I_{W1}, I_{W2}, I_{W3}, \\ &dI_{W1}, dI_{W2}, dI_{W3} \end{aligned}$	Length of element ; radius at pole tip ; current in windings ; relative error on currents.	2*cm, 3*A 3*no dim	5*E 3*E	10 - 17
X_E, λ_E	Entrance face Integration zone ; fringe field extent. (sharp edge if field extent is zero)	2*cm	11*E	20, 21
<i>NCE</i> , $C_0 - C_5$	Same as QUADRUPO	0-6, 6*no dim	I, 6*E	30 - 36
X_S, λ_S	Exit face Integration zone ; as for entrance	2*cm	11*E	40, 41
<i>NCS</i> , $C_0 - C_5$		0-6, 6*no dim	I, 6*E	50 - 56
R1	Roll angle	rad	Е	60
XPAS	Integration step	cm	Е	70
KPOS, XCE, YCE, ALE	KPOS=1 : element aligned, 2 : misaligned ; shifts, tilt.	1-2, 2*cm, rad	I, 3*E	80 - 83

AIMANT	Generation of dipole mid-plane 2-D map, polar frame		
	$B_Z = \mathcal{F}B_0 \left(1 - N \left(\frac{R - RM}{RM} \right) + B \left(\frac{R - RM}{RM} \right)^2 + G \left(\frac{R - RM}{RM} \right)^2$	$\left(\frac{M}{2}\right)^{3}$	
NFACE, IC, IL	Number of field boundaries IC = 1, 2: print field map $IL = 1, 2[\times 10^n], 7$: print coordinates, fields, etc., step-by-step, in zgoubi.res (1), zgoubi.plt (2), zgoubi.impdev.out (7).	2-3; 0-2; 0-2[$\times 10^n$], 7	73*I
IAMAX, IRMAX	Azimuthal and radial number of nodes of the mesh	$\leq 400, \leq 10^4$	2*I
B ₀ , N, B, G	Field and field indices	kG, 3*no dim	4*E
AT, ACENT, RM, RMIN, RMAX	Mesh parameters : total angle of the map ; azimuth for EFBs positioning ; reference radius ; minimum and maximum radii	2*deg, 3*cm	5*E
	ENTRANCE FIELD BOUNDARY		
λ, ξ	Fringe field extent (normally \simeq gap size); flag: - if $\xi \ge 0$: second order type fringe field with linear variation over distance ξ - if $\xi = -1$: exponential type fringe field : $F = (1 + \exp(P(s)))^{-1}$ $P(s) = C_0 + C_1(\frac{s}{\lambda}) + C_2(\frac{s}{\lambda})^2 + + C_5(\frac{s}{\lambda})^5$	cm, (cm)	2*E
NC, $C_0 - C_5$, shift	NC = 1 + degree of $P(s)$; C_0 to C_5 : see above ; EFB shift (ineffective if $\xi \ge 0$)	0-6, 6*no dim, cm	I, 7*E
$\omega^+, \theta, R_1, U_1, U_2, R_2$	Azimuth of entrance EFB with respect to ACENT; wedge angle of EFB; radii and linear extents of EFB (use $U_{\frac{1}{2}} = \mp \infty$ when $R_{1,2} = \infty$)	2*deg, 4*cm	6*E
	(Note : $\lambda = 0$, $\omega^+ = ACENT$ and $\theta = 0$ for <u>sharp edge</u>)		
	EXIT FIELD BOUNDARY (See ENTRANCE FIELD BOUNDARY)		
$ \begin{array}{l} \lambda,\xi \\ \textit{NC}, C_0-C_5, \textit{shift} \\ \omega^-, \theta, R_1, U_1, U_2, R_2 \end{array} $	Fringe field parameters See above Positioning and shape of the exit EFB	cm, (cm) 0-6, 6*no dim, cm 2*deg, 4*cm	2*E 1, 7*E 6*E
	(Note : $\lambda = 0$, $\omega^- = -AT + ACENT$ and $\theta = 0$ for <u>sharp edge</u>)		

If NFACE = 3	LATERAL FIELD BOUNDARY (See ENTRANCE FIELD BOUNDA Next 3 records only if NEACE = 3	RY)	
$ \begin{array}{l} \lambda,\xi\\ \textit{NC},C_0-C_5,\textit{shift}\\ \omega^-,\theta,R_1,U_1,U_2,R_2,\\ RM3 \end{array} $	Fringe field parameters See above Positioning and shape of the lateral EFB ; RM3 is the radial position on azimuth ACENT	cm, (cm) 0-6, 6*no dim, cm 2*deg, 5*cm	2*E I, 7*E 7*E
NBS	Option index for perturbations to the field map	$-2-0 \text{ or } \geq 1$	Ι
If $NBS = 0$	Normal value. No other record required		
If NBS = -2	The map is modified as follows :		
$R_0, \Delta B/B_0$	B transforms to $B * \left(1 + \frac{\Delta B}{B_0} \frac{R - R_0}{RMAX - RMIN}\right)$	cm, no dim	2*E
If NBS = -1	the map is modified as follows :		
$\theta_0, \Delta B/B_0$	B transforms to $B * \left(1 + \frac{\Delta B}{B_0} \frac{\theta - \theta_0}{AT} \right)$	deg, no dim	2*E
If NBS ≥ 1	Introduction of NBS shims		
For I = 1, NBS	The following 2 records must be repeated NBS times		
$R_1, R_2, heta_1, heta_2, \lambda$	Radial and angular limits of the shim ; λ is unused	2*cm, 2*deg, cm	5*E
$\gamma, \alpha, \mu, \beta$	geometrical parameters of the shim	2*deg, 2*no dim	4*E
IORDRE	Degree of interpolation polynomial : 2 = second degree, 9-point grid 25 = second degree, 25-point grid 4 = fourth degree, 25-point grid	2, 25 or 4	Ι
XPAS	Integration step	cm	Е
KPOS	Positioning of the map, normally 2. Two options :	1-2	Ι
If KPOS = 2 RE, TE, RS, TS	Positioning as follows : Radius and angle of reference, respectively, at entrance and exit of the map.	cm, rad, cm, rad	4*E
If KPOS = 1 <i>DP</i>	Automatic positioning of the map, by means of reference relative momentum	no dim	Е



A : Parameters used to define the field map and geometrical boundaries. B : Parameters used to define the field map and fringe fields.



Second order type fringe field.



Exponential type fringe field.

AUTOREF	Transport beam into a new reference frame		
Ι	1 : Equivalent to CHANGREF($XCE = 0, YCE = Y(1), ALE = T(1)$), <i>i.e.</i> , recentering of the beam on particle #1.	1-4	Ι
	2 : Equivalent to $CHANGREF(XW, YW, T(1))$, with (XW, YW) the location of the intersection (waist) of particles 1, 4 and 5 (useful with <i>MATRIX</i> , for automatic positioning of the first order focus).		
If I = 3 I1, I2, I3	Provide next record if $I = 3$ Three particle numbers Equivalent to <i>CHANGREF</i> (<i>XW</i> , <i>YW</i> , <i>T</i> (<i>I</i> 1)), with (<i>XW</i> , <i>YW</i>) the location of the intersection (waist) of particles <i>I</i> 1, <i>I</i> 2 and <i>I</i> 3 (for instance : <i>I</i> 1 = central trajectory, <i>I</i> 2 and <i>I</i> 3 = paraxial trajectories that intersect at the first order focus).	3*(1– <i>IMAX</i>)	3*I
If $I = 4$ XCE, YCE, ALE	Provide next record if $I = 4$ XCE and beam centroid new coordinates YCE, ALE Equivalent to CHANGREF(XCE, YCE, ALE).	2*cm, mrad	3*E
If $I = 4.1$ XCE, YCE, ALE, DCE, TIME	Provide next record if $I = 4.1$ <i>XCE</i> and beam centroid new coordinates <i>YCE</i> , <i>ALE</i> , <i>DCE</i> , <i>TIME</i> 4Equivalent to <i>CHANGREF</i> (<i>XCE</i> , <i>YCE</i> , <i>ALE</i>) with in addition centering of the beam on a new relative momentum <i>DCE</i> .	2*cm, mrad, -, μs	6*E
If $I = 4.2$ XCE, YCE, ALE, DCE, TIME	Provide next record if $I = 4.2$ XCE and beam centroid new coordinates YCE, ALE, DCE, time setting TIME (same for all particles).	2*cm, mrad, -, μs	6*E
If $I = 5$ ZCE, PLE	Provide next record if $I = 5$ New vertical beam centroid coordinates ZCE, PLE The beam is centered vertically on ZCE, PLE.	cm, mrad	2*E

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BEAMBEAM	Beam-beam lens		
SW, I	0/1 : off/on ; beam intensity. Use <i>SPNTRK</i> to activate spin kicks.	0-2, Amp	I, E
$\alpha_Y, \ \beta_Y, \ \epsilon_{Y,norm}/\pi$	Beam parameters, horizontal.	- , m, m.rad	3*E
$\alpha_Z, \ \beta_Z, \ \epsilon_{Z,norm}/\pi$	Beam parameters, vertical.	- , m, m.rad	3*E
$\sigma_X, \sigma_{dp/p}$	rms bunch length ; rms momentum spread.	m, -	2*E
C, α	Ring circumference ; momentum compaction.	m, -	2*E
Q_Y, Q_Z, Q_s	Tunes, horizontal, vertical, synchrotron.	-, -, -	3*E
A_Y, A_Z, A_X	Amplitudes, horizontal, vertical, longitudinal.	-, -, -	3*E

BEND	Bending magnet, Cartesian frame	(page 76 in PART A	A)
ΠL	$IL = 1, 2[\times 10^n], 7$: print coordinates, fields, etc., step-by-step, in zgoubi.res (1), zgoubi.plt (2), zgoubi.impdev.out (7).	$0-2[\times 10^n], 7$	Ι
XL, Sk, B1	Length ; skew angle ; field (change ALE and wedge signs, if $B{<}0$).	cm, rad, kG	3*E
$X_{\rm E}, \lambda_{\rm E}, W_{\rm E}$	Entrance face : Integration zone extent ; fringe field extent (normally \simeq gap height ; zero for sharp edge) ; wedge angle (>0 for rectangle magnet).	cm, cm, rad	3*E
$N, C_0 - C_5$	Unused ; fringe field coefficients : $B(s) = B1 F(s)$ with $F(s) = 1/(1 + \exp(P(s)))$ and $P(s) = \sum_{i=0}^{5} C_i(s/\lambda)^i$	unused, 6*no dim	I, 6*E
X_S, λ_S, W_S	Exit face : See entrance face	cm, cm, rad	3*E
$N, C_0 - C_5$		unused, 6*no dim	I, 6*E
XPAS	Integration step	cm	Е
KPOS, XCE, YCE, ALE	 <i>KPOS</i>=1 : element aligned, 2 : misaligned ; shifts, Z-tilt. <i>KPOS</i> = 3 : (<i>XCE</i> is unused) entrance and exit frames are shifted by <i>YCE</i> and tilted <i>wrt</i>. the magnet by an angle of either ALE, if ALE is non-zero (normally, ALE>0 in that case) 	1-2, 2*cm, rad	I, 3*E

• or 2 Arcsin($B1 \times XL / 2 \times BORO$) if ALE=0



Geometry and parameters of *BEND* : XL = length, θ = deviation, W_E , W_S are the entrance and exit wedge angles. The motion is computed in the Cartesian frame (O, X, Y, Z).

• Example : Positive or negative field BEND

The data list at left hand, below, simulates a case of positive field, followed by two different ways to simulate the same magnet with negative field. (This can be copy-pasted to zgoubi, as is, for execution.) The right hand column shows the transport matrix in all three cases.

Test signs, with wedges. ! Magnet deviation is ! tta=11.25deg=2asin(L/2rho)=2asin(B.L/2.Brho) with L=247.30039, Brho=1000, B=1.57776 ! 1/ Positive B, regular form of input data 'OBJET' 1000. .01 .1 .01 .1 0. .001 0. 0. 0. 0. 0. 1. Reference particle (# 1), path length : 248.88547 'BEND' TRANSFER MATRIX ORDRE 1 (MKSA units) 247.30039 0. 1.57776 20. 8. 0.04276056667
 0.940559
 2.42528

 -4.768802E-02
 0.940229

 0.00000
 0.00000

 0.00000
 0.00000

 0.00000
 0.00000
 0.00000
 0.0

 0.00000
 0.00000
 0.0
 0.0

 0.985447
 2.48908
 0.0

 -1.163098E-02
 0.985390
 0.0
 0 482374 ! wedge is +2.45deg 0.482374 0.385904 0.00000 0.00000 4 .2401 1.8639 -.5572 .3904 0. 0. 0. 20. 8. 0.04276056667 ! wedge is +2.45deg 20. 0. 0.042/N03666/ 4 .2401 1.8639 -.5572 .3904 0. 0. 0. #30[10]30 3 0. 0. -.1963495408 0.482384 6.370064E-02 0.385970 0.00000 0.00000 1.0 0.00000 0.00000 0.0 0.00000 0.00000 1.00000 'FAISCEAU' 'MATRIX' 1 0 ! 2/ Negative B. Compared to 1/ : Rll-R44 unchaged, R16, R26 change sign. ! 2-a/ By changing sign of B. Note : signs of ALE and wedges have to be reversed. 'OBJET' 1000. .01 .1 .01 .1 0. .001 0. 0. 0. 0. 0. 1. Reference particle (# 1), path length : 248.88547 'BEND' TRANSFER MATRIX ORDRE 1 (MKSA units) 0 247.30039 0. -1.57776 20. 8. -0.04276056667 4 .2401 1.8639 -.5572 s) 0.00000 0.0 -0.482374 0.00000 0.0 -0.385904 2.48908 0.0 0.00000 0.985390 0.0 0.00000 0.00000 1.0 6.3700641 0.00000 0.0 1.00000 0.00000 0.940559 2.42528 0.940559 2.42528 -4.768802E-02 0.940229 0.00000 0.00000 0.00000 0.00000 ! wedge is +2.45deg 1 1.8639 -.5572 .3904 0. 0. 0. -0.04276056667 0.985447 -1.163098E-02 0.00000 0.00000 ! wedge is +2.45deg 20. 8. -4 .2401 1.8639 -.5572 .3904 0. 0. 0. -0.482384 6.370064E-02 -0.385970 #30|10|30 3 0. 0. .1963495408 0.00000 0.00000 'FAISCEAU' 'MATRIX' 1 0 ! 2-a/ Using YMY instead. All data in BEND remain unchanged. 'OBJET' 1000. .01 .1 .01 .1 0. .001 0. 0. 0. 0. 0. 1. 'YMY' Reference particle (# 1), path length : 248.88547 'BEND' TRANSFER MATRIX ORDRE 1 (MKSA units) U 247.30039 0. 1.57776 20. 8. 0.04276056667 4 .2401 1.8639 -.5572 .3904 0. 0. 0. 20. 8. 0.04276056667
 RE
 1
 (MKSA Units)
 0.00000
 0.0
 -0.482374

 0.00000
 0.00000
 0.0
 -0.385904

 0.985447
 2.48908
 0.0
 0.00000

 -1.163098E-02
 0.985390
 0.0
 0.00000

 0.00000
 0.00000
 1.0
 6.370064E-02

 0.00000
 0.00000
 0.0
 1.00000
 0.940559 2.42528 ! wedge is +2.45deg -4.768802E-02 0.940229 -4.768802E-02 0.00000 -0.385970 0.00000 0.00000 ! wedge is +2.45deg -0.482384 0.00000 'FAISCEAU 'MATRIX' 1 0

'END'

BETATRON Betatron core (momentum kick) dp-kick Momentum kick, relative to particle momentum. E

BINARY BINARY ↔ FORMATTED data converter

NF[.J], NCol, NHDR	Number of files to convert [READ format type, see below], of data columns, of header lines.	$\leq 20, \leq 7$, $0-9$	3*I1
The next <i>NF</i> lines : <i>FNAME</i>	Name of the file to be converted. File content is assumed binary <i>iff</i> name begins with "B" or "b", assumed formatted otherwise.		A80

READ format, case of formatted input file :

If FRM not given	Format is '*'
If FRM=1	Format is '1X, 7E11.*'

READ format, case of binary input file :

Expected format is 7 column rows.

BREVOL	1-D uniform mesh magnetic field map <i>X</i> -axis cylindrical symmetry is assumed		
IC, IL	IC = 1, 2: print the map $IL = 1, 2[\times 10^n], 7$: print coordinates, fields, etc., step-by-step, in zgoubi.res (1), zgoubi.plt (2), zgoubi.impdev.out (7).	$0-2; 0-2[\times 10^n], 7$	2*I
BNORM, XN	Field and X-coordinate unit conversion coeff. Convert values as read from map file, to kG and cm units.	2*UnitConv.	2*E
TITL	Title. Start with "FLIP" to get field map X-flipped.		A80
IX	Number of longitudinal nodes of the map	≤ 400	Ι
FNAME [, SUM] ^{1, 2}	File name		A80
ID, A, B, C [, A', B', C', B", etc., if $ID \ge 2$]	Integration boundary. Ineffective when $ID = 0$. $ID = -1$, 1 or ≥ 2 : as for <i>CARTEMES</i>	≥ -1, 2*no dim, cm [,2*no dim, cm, etc.]	I,3*E [,3*E,etc.]
IORDRE	Unused	2, 25 or 4	Ι
XPAS	Integration step	cm	Е
KPOS, XCE, YCE, ALE	KPOS=1 : element aligned, 2 : misaligned ; shifts, tilt.	1-2, 2*cm, rad	I, 3*E

¹ FNAME (e.g., solenoid.map) contains the field data. These must be formatted according to the following FORTRAN sequence :

```
OPEN (UNIT = NL, FILE = FNAME, STATUS = 'OLD' [,FORM='UNFORMATTED'])
DO 1 I = 1, IX
IF (BINARY) THEN
READ(NL) X(I), BX(I)
ELSE
READ(NL,*) X(I), BX(I)
ENDIF
1 CONTINUE
```

where X(I) and BX(I) are the longitudinal coordinate and field component at node (I) of the mesh. Binary file names must begin with FNAME 'B₂' or 'b₂'. 'Binary' will then automatically be set to '.TRUE.'.

² Sumperimposing (summing up) field maps is possible. Up to 4 at most. To do so, pile up file names with 'SUM' following each name but the last one.

In the following example *e.g.*, 3 field maps are read and summed up[~]:

myMapFile1 SUM myMapFile2 SUM myMapFile3

(all maps must all have their mesh defined in identical coordinate frame).

CARTEMES	2-D Cartesian uniform mesh magnetic field map mid-plane symmetry is assumed		
IC, IL	IC = 1, 2: print the map $IL = 1, 2[\times 10^n], 7$: print coordinates, fields, etc., step-by-step, in zgoubi.res (1), zgoubi.plt (2), zgoubi.impdev.out (7).	$0-2; 0-2[imes 10^n], 7$	2*I
BNORM, XN,YN	Field and X-,Y-coordinate unit conversion coeffs. Convert values as read from map file, to kG and cm units.	3*UnitConv.	3*E
TITL	Title. Start with "FLIP" to get field map X-flipped.		A80
IX, JY	Number of longitudinal (IX) and transverse (JY) nodes of the map	$\leq 400, \leq 200$	2*I
FNAME ¹	File name		A80
ID, A, B, C [, A', B', C', A", B",etc., if $ID \ge 2$]	Integration boundary. Normally $ID = 0$. ID = -1: integration in the map begins at entrance boundary defined by $AX + BY + C = 0$. ID = 1: integration in the map is terminated at exit boundary defined by $AX + BY + C = 0$. $ID \ge 2$: entrance (A, B, C) and up to $ID - 1$ exit (A', B', C', A'', B'', etc.) boundaries	≥ -1,2*no dim, cm [,2*no dim, cm, etc.]	I, 3*E [3*E,etc.]
IORDRE	Degree of interpolation polynomial (see DIPOLE-M)	2, 25 or 4	Ι
XPAS	Integration step	cm	E
KPOS, XCE, YCE, ALE	KPOS=1 : element aligned, 2 : misaligned ; shifts, tilt.	1-2, 2*cm, rad	I, 3*E

 2 FNAME (e.g., spes2.map) contains the field data. These must be formatted according to the following FORTRAN sequence :

```
OPEN (UNIT = NL, FILE = FNAME, STATUS = 'OLD' [,FORM='UNFORMATTED'])
IF (BINARY) THEN
READ(NL) (Y(J), J=1, JY)
ELSE
    READ(NL,100) (Y(J), J=1, JY)
   ENDIF
100 FORMAT(10 F8.2)
   DO 1 I=1,IX
 IF (BINARY) THEN
 READ(NL) X(I), (BMES(I,J), J=1, JY)
ELSE
 READ(NL,101) X(I), (BMES(I,J), J=1, JY)
101 FORMAT(10 F8.2)
    ENDIF
1
   CONTINUE
```

where X(I) and Y(J) are the longitudinal and transverse coordinates and *BMES* is the Z field component at a node (I, J) of the mesh. For binary files, *FNAME* must begin with 'B_' or 'b_'. 'Binary' will then automatically be set to '.TRUE.'



OXY is the coordinate system of the mesh. Integration zone limits may be defined, using $ID \neq 0$: particle coordinates are extrapolated linearly from the entrance face of the map, into the plane A'X + B'Y + C' = 0; after ray-tracing inside the map and terminating on the integration boundary AX + BY + C = 0, coordinates are extrapolated linearly to the exit face of the map.

CAVITE ^{1,2}	Accelerating cavity $\Delta W = q\hat{V}\sin(2\pi hf\Delta t + \varphi_s)$ or other voltage and frequency laws.	(page 82 in PAR	TA)
IOPT[.i] [,PRINT] [, Facility] [, SHIFT_PH0] [,CENTROID]	Option, see below ; $i = 1$ (equivalently, presence of 'PRINT') causes info logged to zgoubi.CAVITE.Out ; <i>Facility</i> is accounted for <i>iff IOPT=10</i> , or <i>11</i> (otherwise ignored), it can be : - 'CornellSynch' (hard-coded voltage), or - 'EIC_RCS' (hard-coded synchronous RF phase), or - 'EICRCS_File' (read data from external file zgoubi.RFLaw.In ³), or - CEBAF (overrides <i>SHIFT_PH0</i> : imposes phase origin at $\pi/2$) ; 'SHIFT_PH0' is accounted for <i>iff IOPT=10</i> (otherwise ignored), it shifts the RF phase of any particle by $\pi/2$; 'CENTROID' is accounted for <i>iff IOPT=10</i> (otherwise ignored), it shifts the RF phase of any particle by the bunch centroid phase.	0-11, - , - , -	I[.1] [, A] [, A] [, A] [, A]
If IOPT=0	Element inactive		
X, X X, X	Unused. Unused.		
If IOPT=1 ⁴	f_{BF} follows the timing law given by SCALING		
\mathcal{L}, h \hat{V}, X	Reference closed orbit length ; harmonic number. R.F. peak voltage ; unused.	m, no dim V, unused	2*E 2*E
If IOPT=2[.i]	f_{RF} follows $\Delta W_s = q \hat{V} \sin \phi_s$. Handles SR loss in store mode. Handles double	e RF systems	
- either : \mathcal{L}, h [,POS] \hat{V}, ϕ_s - or :	Reference closed orbit length ; harmonic number ; s location (optional) R.F. peak voltage ; synchronous phase.	m, - [,m] V, rad	2*E [,E] 2*E
$\mathcal{L}, \{h_1, h_2\}$ [,POS] $\{\hat{V}_1, \hat{V}_2\}, \phi_s$ [, dphn]	Reference closed orbit length ; harmonic numbers ; s location (optional) R.F. peak voltages ; synchronous phase ; phase-shift (default is dphn= $\pi/21$).	m, - [,m] 2*V, rad [, rad]	2*E [,E] 3*E [, E]
$If i=2 \\ \gamma_{\rm tr}$	a third input data line is needed (case of acceleration range including transition) Transition gamma value	-	Е
If IOPT=3	No synchrotron motion : $\Delta W = q \hat{V} \sin \phi_s$		
$\begin{array}{c} X, X\\ \hat{V}, \phi_s \end{array}$	Unused ; unused. R.F. peak voltage ; synchronous phase.	2*unused. V, rad	2*E 2*E
If IOPT-6	Read RE frequency and/or phase law from external file "zgoubi freqLaw In"		
$X. E_{kin s}$	Unused : initial synchronous kinenergy: RF harmonic.		2*E
\hat{V}, Φ_s	R.F. peak voltage ; synchronous phase.	v, rad	2*E
If IOPT=7	Quasi- or isochronous acceleration.		
X, f_{RF}	Unused ; RF frequency.	- , Hz	2*E
V, Φ_s	R.F. peak voltage ; synchronous phase.	V, rad	2*E
If IOPT=10	Chambers matrix method (origin of phase determined by 'SHIFT_PH0' option i	n line 1).	
L, f_{RF} \hat{V}, Φ_s [, IOP]	Cavity length ; RF frequency R.F. peak voltage ; synchronous phase ; matrix (damping) options: either <i>IOP</i> =0 : default value, transverse matrix is a drift;	m, Hz V, rad, $[\in [-2, +2]]$	2*E 2*E [, I]
	or $IOP=\pm 1: dE/E \ll 1$ approx. and, resp ^{ly} , $\begin{cases} transverse damping \\ transv. determinant = 1 \end{cases}$;		
	or $IOP=\pm 2$: $\forall dE/E$ and, resp ^{ly} , { transverse damping transv. determinant = 1 ·		

If IOPT=11	Acceleration in presence of SR loss (optionally, line 1: <i>Facility= 'CornellSynch</i> or <i>Facility= 'EIC_RCS'</i> (synchronous phase law is hard-coded).	' (voltage law is h	hard-coded,
\mathcal{L}, E_k	Orbit length and kinetic energy at start of acceleration.	m, MeV [,-]	2*E [,A]
$\hat{V}, \Phi_s, U_{00} [, POS]$	R.F. peak voltage (unused - hardcoded - if Facility= 'CornellSynch');	V, rad, eV [,m]	3*E [,E]
	synchronous phase (will be initial value if Facility= 'EIC_RCS'); energy loss		

to be recovered here (value at initial energy)⁵; optional: cavity distance

from beg. of sequence (not needed if cavity is at an end).

 $^1 For the geek: details in subroutines <code>rcavit.f</code> (read input), <code>cavite.f</code> (cavity models).$

 5 Synchrotron radiation loss at subsequent turns is actualized using $U\propto E^4.$

³ Formatting of zgoubi.RFLaw.In file is 5 columns: turn #, energy/MeV, unused, voltage/V, unused ⁴ For ramping the R.F. frequency following $B\rho(t)$, use *SCALING*, with family *CAVITE*.

² Use *PARTICUL* to declare mass and charge.

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CHAMBR	Long transverse aperture limitation 1		
IA	0 : element inactive1 : (re)definition of the aperture2 : stop testing and reset counters, printinformation on stopped particles.	0-2	Ι
IFORM[.J], C1, C2, C3, C4	<i>IFORM</i> = 1 : rectangular aperture ; <i>IFORM</i> = 2 : elliptical aperture. $J = 0$, default : opening is $^2 \pm YL = \pm C1$, $\pm ZL = \pm C2$, centered at $YC = C3$, $ZC = C4$. $J = 1$: opening is 2 , in Y : [C1, C2], in Z : [C3, C4]	1-2[.0-1]	I[.I], 4*E

¹ Any particle out of limits is stopped. ² When used with an optical element defined in polar coordinates (*e.g.*, *DIPOLE*) YL is the radius and YC stands for the reference radius (normally, $YC \simeq RM$).

CHANGREF	Transformation to a new reference frame
	SCALING can be used to scale positionning parameters in CHANGREF.

"Old Style" (Figure below) :

XCE, YCE, ALE	Longitudinal and transverse shifts,	2*cm, deg	3*E
	followed by Z-axis rotation		

"New Style" (see example below). In an arbitrary order, up to 9 occurrences of :

XS 'val', YS 'val', ZS 'val',	cm or deg	up to 9*(A2,E)
XR 'val', YR 'val', ZR 'val'		



Parameters in the CHANGREF procedure.

• Example : CHANGREF

```
Using CHANGREF "New Style
'OBJET'
51.71103865921708
                                                                          Electron, Ekin=15MeV.
2
1 1
                                                                                One particle, with
2. 0. 0.0 0.0 0.0 1. 'R'
1 1 1 1 1 1 1
'MARKER' BEG .plt
                                                    Y_0=2 cm, other coordinates zero.
                                 .plt
                                                                   -> list into zgoubi.plt.
'DRIFT'
                                                                                          10 cm drift.
10.
'CHANGREF'
ZR -6.34165 YS 1.
'MULTIPOL' Co
                                                    First half Z-rotate, Next Y-shift.

      ZA - 6.34165 15 1.
      First hall 2-rotate, Next F-Shilt.

      'MULTIPOL'
      Combined function multipole, dipole + quadrupole.

      2
      -> list into zgoubi.plt.

      5
      10. 2.064995867082342 2. 0. 0. 0. 0. 0. 0. 0. 0. 0.

      0
      5. 1.1 1.00 1.00 1.00 1.00 1.00 1. 1. 1. 1.

      4
      .1455 2.2670 - .6395 1.1558 0. 0. 0.

5
4
.1 step size
1 0.0.0.
'CHANGREF'
YS -1. ZR -6.341
'DRIFT'
                                        First Y-shift back, next half Z-rotate.
                                                                                         10 cm drift.
10.
'FAISCEAU'
'END'
```

CIBLE, TARGET	Generate a secondary beam following target interaction		
M_1, M_2, M_3, Q T_2, θ, β	Target, incident and scattered particle masses ; Q of the reaction ; incident particle kinetic energy ; scattering angle ; angle of the target	$5*\frac{MeV}{c^2}$, 2*deg	7*E
NT, NP	Number of samples in T and P coordinates after <i>CIBLE</i>		2*I
TS, PS, DT	Sampling size ; tilt angle	3*mrad	3*E
BORO	New reference rigidity after CIBLE	kG.cm	Е



Scheme of the principles of CIBLE (TARGET)

A, T = position, angle of incoming particle 2 in the entrance reference frame P = position of the interaction

B, T = position, angle of the secondary particle in the exit reference frame

 θ = angle between entrance and exit frames

 β = tilt angle of the target

COLLIMA	Collimator ¹		
IA	0 : element inactive1 : element active2 : element active and print information on stopped particles	0-2	Ι
Physical-space collimatio IFORM[.J], C1, C2, C3, C4	n <i>IFORM</i> = 1 or 2 : rectangular or elliptical aperture ; $J = 0$, default : opening is $\pm YL = \pm C1$, $\pm ZL = \pm C2$, centered at $YC = C3$, $ZC = C4$. J = 1 : opening is, in $Y : [C1, C2]$, in $Z : [C3, C4]$	1-2[.0-1], 4*cm	I[.I], 4*E
Longitudinal collimation IFORM.J, H_{min} , H_{max} , V_{min} , V_{max}	<i>IFORM</i> = 6 or 7 for horizontal variable resp ^{ly} S or Time, J=1 or 2 for vertical variable resp ^{ly} 1+dp/p, kinetic-E (MeV) ; horizontal and vertical limits	2*cm or 2*μs, 2*no.dim or 2*MeV	I, 4*E
Phase-space elliptical coll IFORM, α , β , ϵ/π , N_{σ} , XM, XPM	imation <i>IFORM</i> = 11, 14 : horizontal collimation ; horizontal ellipse parameters (unused if 14) ² , emittance, cut-off, ellipse centering (unused if 14) ² ; <i>IFORM</i> = 12, 15 : vertical collimation ; vertical ellipse parameters (unused if 15) ² , emittance, cut-off, ellipse centering (unused if 15) ² ; <i>IFORM</i> = 13, 16 : longitudinal collimation ; to be implemented.	11-16, no.dim, 2*m, no.dim	I, 4*E

¹ Any particle out of limits is stopped. ² If IFORM = 14, 15 or 16, the *rms* ellipse matched to the particle distribution is fist computed (namely, ellipse parameters α , β and centering XM, XPM). It is then considered to be the phase-space collimation aperture.

CYCLOTRON	Spiral setor cyclotron	(page 93 in PART A)	
	$B_Z = \sum_{i=1}^{N \text{ dipoles}} BN_i \mathcal{F}_i(R,\theta) \mathcal{R}_i(R) \text{ with } \mathcal{R}_i(R) = B_0 + \sum_{j=1}^{j \le 20} B_{j,i} \times R_j$	ġ	
IL	$IL = 1, 2[\times 10^n], 7$: print coordinates along trajectories, fields, etc., into zgoubi.res (1) or zgoubi.plt (2[×10 ⁿ]) or zgoubi.impdev.out (7).	$0-2[\times 10^n], 7$	Ι
N, AT, RM, ITYP	Number of dipoles within AT ; total angular extent of the dipole ; reference radius; sector type: spiral (0), radial (1), both (2)	-, deg, cm, 0-2	I, 2*E, I
Repeat N times the follow	ving sequence		
ACN, δRM , BN , B_0 , K , R_{ref} , $[H_i, i = 1, n]$	Dipole positionning (ACN, $RM + \delta RM$); field normalization; dipole field; unused; unused; optional: up to 20 field indices	deg, cm, -, kG, -, - [, cm ^{-j}]	
	ENTRANCE FIELD BOUNDARY		
g_0, κ, g_1, g_2 $NC, C_0 - C_7$, shift $\omega^+, \xi_0, \xi_1, \xi_2, \xi_3$, a, b, c	Fringe field extent : $g = g_0$ if $\kappa = 0$, otherwise $g = g_1 + g_2 R/100$. Unused ; C_0 to C_7 : fringe field coefficients ; unused. Azimuth of entrance EFB with respect to ACN ; ξ_{0-3} : definition of spiral EFB ; a-c: definition of radial EFB (unused)	cm, 0-1, cm, - 0-6, 9*- 2*deg,deg/m,deg/m ² , deg/m ³ , 3*-	E,I,2*E I, 9*E 8*E
	EXIT FIELD BOUNDARY (See ENTRANCE FIELD BOUNDARY)		
$g_0, \kappa, g1, g2$ $NC, C_0 - C_7$, shift $\omega^-, \xi_0, \xi_1, \xi_2, \xi_3$, a, b, c	Fringe field parameters, EFB definition and positioning, see above.	cm, 0-1, cm, - 0-6, 9*- 2*deg,deg/m,deg/m ² , deg/m ³ , 3*-	E,I,2*E I, 9*E 8*E

LATERAL FIELD BOUNDARY to be implemented - following data not used

g_0,κ	2*-	E, I
$NC, C_0 - C_5$, shift	8*-	1, 7*E
$\omega^{-}, \xi, R_1, U_1, U_2, R_2$	6*-	6*E

End of	of re	peat
--------	-------	------

Integration boundaries - next line is optional, starting with string IntLim :

IntLim, <i>ID</i> , <i>A</i> , <i>B</i> , <i>C</i> [, <i>A</i> ', <i>B</i> ', <i>C</i> ']	Integration boundary. Line has to start with 'IntLim'. ID = -1: integration in the magnet begins at entrance boundary defined by A, B, C. ID = 1: integration is terminated at exit boundary defined by A', B', C'. ID = 2: both entrance and exit boundaries.	-1, 1, 2; deg; cm; deg [; <i>id</i> .]	I, 3*E [,3*E]
KIRD, Resol	 KIRD = 2, 4 or 25 : numerical interpolation of field derivatives ; size of flying interpolation mesh is <i>XPAS/Resol</i>. KIRD=2 or 25 : second degree, 9- or 25-point grid KIRD=4 : fourth degree, 25-point grid 	0, 2, 25 or 4; -	I, E
XPAS	Integration step	cm	Е
KPOS, RE, TE, RS, TS	Positioning of the magnet, has to be 2. As follows : radius and angle of reference, respectively, at entrance and exit of the magnet.	2, 2*(cm, rad)	I, 4*E

• Example : CYCLOTRON

A model of a 6-sector cyclotron where one varied the spiral angle is illustrated in Fig 54-left :

-in red, the spiral angle is fixed, $\xi = 30$ deg, while, in blue, the spiral angle increases with the radius, $\xi = 30 + 0.02 \times R$ deg. - the tune calculation is shown in Fig 54-right, were one can see that a proper radial increase of the spiral angle allows stabilizing the vertical wave number.



Figure 54: Comparison of cyclotron spiral sector designs: with fixed spiral angle and with varying spiral angle. Left: orbits around the ring; EFB footprints are superimposed, with constant spiral angle (red) or increasing spiral angle with radius (blue). Right: radial and axial wave numbers over the radial span of the orbits, with and without increasing spiral angle (note that Q_Z is close to 1, this requires some more work...)

The input data file below tracks closed orbits for a few different momenta:

PSI-style CYCLOTRON	spiral sector					
'OBJET'						
1249.382414						! Reference rigidity.
2						
6 1						
268.20121069999999	-15.580272709999999	Ο.	Ο.	Ο.	1.4	′ °′
282.46123799999998	-26.403956470000001	Ο.	Ο.	0.	1.5	'o'
296.05739569999997	-38.103638570000001	Ο.	Ο.	Ο.	1.6	′ °′
309.00757420000002	-50.260491320000000	Ο.	0.	Ο.	1.7	′ ₀ ′
321.32946040000002	-62.556048799999999	Ο.	Ο.	Ο.	1.8	′ °′
333.05392440000003	-74.952056110000001	Ο.	Ο.	0.	1.9	'o'
1 1 1 1 1 1 1 1 1 1	1 1 1 1 1 1 1 1					
'PARTICUL'						
PROTON						
'CYCLOTRON'						
2			!	IL=2	to lo	og stepwise integration data in zgoubi.plt.
1 45.0 2.760000E-	⊧02 1.0					5
0. 0. 0.99212277 51	4590015 .5 8000.47	6376	328	2.2760	02517e	-03 -4.81955890e-06 3.94715806e-09
18.3000E+00 1. 28	32.0					! g0, k, g1, g2 Entrance face.
8 1.10243581. 3.129	9150713.14287154.	3.08	5805	9	1.4354	14992. 0.24047436 0. 0. 0.
11 0 3 5 35 E-3 0	E-4 3 E-8 0 0 0			· / ·	Entra	ance EFB: OMEGA XIO XII XI2 XI3 a b c
18.3000E+00 1. 28	-2.0			•	21102.0	lambda=gap, gap's k gl0 gll.
8 0 70490173 4 1601	305 -4 3309575 3 54041	6 -1	347	2703 0	1 1826	S1076 0 0 0 NBCOEF COEFS CO-5 SHIFT
-8 5 2 12 E-3 75	E-6.0 0 0 0	-		2,05	1 E	wit EFB: OMEGA XIO XII XI2 XI3 a b c
0 -1						Lateral face ignored
0 0 0 0 0	0 0 0					. Dateral late, ignored.
0 0 0 0						
2 10	. U. Internelation or	don	+ 0 0	omput	dori	watiwaa, fluing mach sign is stop sign/10
2 10.	: incerporación or	uer	10 0	ompuce	e derr	Ivacives, ilying mesh size is step-sise/io.
1.0						: INtegration step size.
2 0 0 0						
U. U. U. U.						
· FAISCEAU.						
'END'						

From zgoubi.res file, final FAISCEAU :

***	4 Keyword, label(s) : FAISCEAU																
	TRACE DU FAISCEAU																
	6 TRAJECTOIRES																
					OBJET							FAI	SCEAU				
		D	Y(CM)	T(MR)	Z(CM)	P(MR)	S (0	CM)		D	Y(CM)	T(MR)	Z(CM)		P(MR)	S(CM)	
0	1	1.4000	268.201	-15.580	0.000	0.000		0.0000	1	.4000	268.26	8 -15.80	0.00	0	0.000	2.166099E+02	1
0	1	1.5000	282.461	-26.404	0.000	0.000	maee	(MeV/c2)	. 1	.5000	282.43	4 -29.93	0.00	0	0.000	2.281330E+02	2
0	1	1.6000	296.057	-38.104	0.000	0.000	maee	0.0000 (MeV/c2)	. 1	.6000	295.92	9 -43.48	9 0.00	0	0.000	2.390438E+02	3
0	1	1.7000	309.008 Time of f	-50.260	0.000	0.000 133252E-02	mass	0.0000 (MeV/c2)	. 1	.7000	308.83	0 -56.19	0.00	0	0.000	2.493744E+02	4
0	1	1.8000	321.329 Time of f	-62.556	0.000	0.000 134077E-02	mass	0.0000 (MeV/c2)	1	.8000	321.16	9 -67.99	0.00	0	0.000	2.591432E+02	5
0	1	1.9000	333.054 Time of f	-74.952 Elight (mus)	0.000	0.000 128373E-02	mass	0.0000 (MeV/c2)	: 1	.9000 938.2	332.93 272	9 -79.02	4 0.00	0	0.000	2.683616E+02	6
В	eam	charac	teristics	(EMIT, ALP	,BET,XM,	XPM,NLIV,N	INL,R	ATIN) :									
	7.9	637E-04	75.42	770.0		3.016	-4.87	/39E-02		6	6	1.000	B-Dim	1	1		
	Ο.	000	75.42	770.0		0.000	0.0	000		6	6	1.000	B-Dim	2	1		
	3.2	319E-04	-0.9964	4.1519	E-08 1	.4813E-02	186	5.5		6	6	1.000	B-Dim	3	1		
В	eam	charac	teristics	SIGMA(4,4) :												
		Ex,	Ez = 6.3	337310E-05	0.00000	E+00											
		Alp	X, BetX =	-7.542375E+	01 7.70	0024E+02											
		Alp	Z, BetZ =	N	aN 0.00	0000E+00											
***	***	******	********	********	******	*******	*****	*******	***	*****	******	*******	*******	****	******	******	***

DECAPOLE	Decapole magnet	(page 95 in PART A)		
IL	$IL = 1, 2[\times 10^n], 7$: print coordinates, fields, etc., step-by-step, in zgoubi.res (1), zgoubi.plt (2), zgoubi.impdev.out (7).	$0-2[imes 10^n], 7$	Ι	
XL, R_0, B_0	Length ; radius and field at pole tip	2*cm, kG	3*E	
X_E, λ_E	Entrance face : Integration zone extent ; fringe field extent ($\leq 2R_0, \lambda_E = 0$ for sharp edge)	2*cm	2*E	
<i>NCE</i> , $C_0 - C_5$	<i>NCE</i> = unused $C_0 - C_5$ = Fringe field coefficients such that $G(s) = G_0/(1 + \exp P(s))$, with $G_0 = B_0/R_0^4$ and $P(s) = \sum_{i=0}^5 C_i(s/\lambda)^i$	unused, 6*no dim	I, 6*E	
X_S, λ_S NCS, $C_0 - C_5$	Exit face : see entrance face	2*cm 0-6, 6*no dim	2*E I, 6*E	
XPAS	Integration step	cm	Е	
KPOS, XCE, YCE, ALE	KPOS=1 : element aligned, 2 : misaligned ; shifts, tilt.	1-2, 2*cm, rad	I, 3*E	



DIPOLE	Dipole magnet, polar frame	(page 96 in PART A)									
	$B_Z = \mathcal{F}B_0 \left(1 + N\frac{R - RM}{RM} + B\left(\frac{R - RM}{RM}\right)^2 + G\left(\frac{R - R}{RM}\right)^2 + G\left($	$\left(\frac{M}{2}\right)^3$									
		dim.	data type	FIT num.							
IL	$IL = 1, 2[\times 10^n], 7$: print coordinates, fields, etc., step-by-step, in zgoubi.res (1), zgoubi.plt (2), zgoubi.impdev.out (7).	$0-2[\times 10^n], 7$	Ι								
AT, RM	Total angular extent of the dipole ; reference radius	deg, cm	2*E	2, 3							
ACENT, B_0 , N , B , G	Azimuth for positioning of EFBs ; field and field indices at $R \equiv RM$. $(N = \frac{RM}{B_0} \frac{dB}{dR}; B = \frac{RM}{2B_0} \frac{d^2B}{dR^2}; G = \frac{RM}{6B_0} \frac{d^3B}{dR^3}).$	deg., kG, 3*no dim	5*E	4-8							
	ENTRANCE FIELD BOUNDARY										
λ, ξ	Fringe field extent (normally \simeq gap size) ; unused. Exponential type fringe field $F = 1 / (1 + \exp(P(s)))$ with $P(s) = C_0 + C_1(\frac{s}{\lambda}) + C_2(\frac{s}{\lambda})^2 + + C_5(\frac{s}{\lambda})^5$	cm, unused	2*E	9, 10							
NC , $C_0 - C_5$, shift	Unused ; C_0 to C_5 : see above ; EFB shift	0-6, 6*no dim, cm	I, 7*E	11-18							
$\omega^+, \theta, R_1, U_1, U_2, R_2$	Azimuth of entrance EFB with respect to ACENT ; wedge angle of EFB ; radii and linear extents of EFB (use $U_{\frac{1}{2}} = \mp \infty$ when $R_{1,2} = \infty$)	2*deg, 4*cm	6*E	19-24							
	(Note : $\lambda = 0$, $\omega^+ = ACENT$ and $\theta = 0$ for <u>sharp edge</u>)										
	EXIT FIELD BOUNDARY (See ENTRANCE FIELD BOUNDA	RY)									
λ, ξ $NC, C_0 - C_5$, shift	Fringe field parameters	cm, unused 0-6, 6*no dim, cm	2*E 1, 7*E	25, 26 27-34							
$\omega^-, \theta, R_1, U_1, U_2, R_2$	Positioning and shape of the exit EFB 2*deg, 4*cm 6*E 35-										
	(Note : $\lambda = 0, \omega = -AT + ACENT$ and $\theta = 0$ for <u>sharp edge</u>)										
	LATERAL FIELD BOUNDARY (See ENTRANCE FIELD BOU	NDARY)									
λ, ξ NC, $C_0 - C_5$, shift	Lateral EFB is inhibited if $\xi = 0$	cm, unused 0-6, 6*no dim, cm	2*E 1, 7*E	41-42 43-50							
$\omega^{-}, \theta, R_1, U_1, U_2, R_2, RM3$	Positioning and shape of the EFB	2*deg, 5*cm	7*E	51-57							
IORDRE, Resol	Degree of interpolation polynomial : 2 = second degree, 9-point grid 25 = second degree, 25-point grid 4 = fourth degree, 25-point grid ; size of flying mesh is <i>XPAS/Resol</i>	2, 25 or 4 ; no dim	I, E	58, 59							
XPAS	Integration step	cm	E	60							
KPOS	Positioning of the magnet, normally 2. Two options :	1-2	Ι								
If KPOS = 2 RE, TE, RS, TS	Positioning as follows : Radius and angle of reference, respectively, at entrance and exit of the magnet.	cm, rad, cm, rad	4*E	64-67							
If KPOS = 1 <i>DP</i>	Automatic positioning of the magnet, by means of reference relative momentum	no dim	E								


Parameters used to define the geometry of a dipole magnet with index, using DIPOLE[S]

DIPOLE-M	Generation of dipole mid-plane 2-D map, polar frame	(page 99 in PART A)	
	$B_Z = \mathcal{F}B_0 \left(1 + N \frac{R - RM}{RM} + B \left(\frac{R - RM}{RM} \right)^2 + G \left(\frac{R - RM}{RM} \right)^3 \right)$		
NFACE, IC, IL	Number of field boundaries IC = 1, 2: print field map $IL = 1, 2[\times 10^n], 7$: print coordinates, fields, etc., step-by-step, in zgoubi.res (1), zgoubi.plt (2), zgoubi.impdev.out (7).	2-3; 0-2; 0-2[$\times 10^n$], 7	7 3*I
IAMAX, IRMAX	Azimuthal and radial number of nodes of the mesh	$\leq 400, \leq 200$	2*I
B_0, N, B, G	Field and field indices	kG, 3*no dim	4*E
AT, ACENT, RM, RMIN, RMAX	Mesh parameters : total angle of the map ; azimuth for positioning of EFBs ; reference radius ; minimum and maximum radii	2*deg, 3*cm	5*E
	ENTRANCE FIELD BOUNDARY		
λ, ξ	Fringe field extent (normally \simeq gap size) ; unused. Exponential type fringe field $F = 1 / (1 + \exp(P(s)))$ with $P(s) = C_0 + C_1(\frac{s}{\lambda}) + C_2(\frac{s}{\lambda})^2 + + C_5(\frac{s}{\lambda})^5$	cm, unused	2*E
NC , $C_0 - C_5$, shift	Unused ; C_0 to C_5 : see above ; EFB shift	0-6, 6*no dim, cm	I, 7*E
$\omega^+, \theta, R_1, U_1, U_2, R_2$	Azimuth of entrance EFB with respect to ACENT; wedge angle of EFB; radii and linear extents of EFB (use $U_{\frac{1}{2}} = \mp \infty$ when $R_{1,2} = \infty$)	2*deg, 4*cm	6*E
	(Note : $\lambda = 0$, $\omega^+ = ACENT$ and $\theta = 0$ for <u>sharp edge</u>)		
	EXIT FIELD BOUNDARY (See ENTRANCE FIELD BOUNDARY)		
λ,ξ $NC,C_0-C_5,$ shift	Fringe field parameters	cm, unused 0-6, 6*nodim., cm	2*E 1, 7*E
$\omega^-, \theta, R_1, U_1, U_2, R_2$	Positioning and shape of the exit EFB	2*deg, 4*cm	6*E
	(Note : $\lambda = 0$, $\omega^{-} = -AT + ACENT$ and $\theta = 0$ for <u>sharp edge</u>)		
If NFACE = 3 λ, ξ	LATERAL FIELD BOUNDARY (See ENTRANCE FIELD BOUNDAR Next 3 records <i>only</i> if <i>NFACE</i> = 3 Fringe field parameters	YY) cm. (cm)	2*E
NC, $C_0 - C_5$, shift ω^- , θ , R_1 , U_1 , U_2 , R_2 , RM3	Positioning and shape of the lateral EFB ; RM3 is the radial position on azimuth <i>ACENT</i>	0-6, 6*no dim, cm 2*deg, 5*cm	I, 7*E 7*E
NBS	Option index for perturbations to the field map	normally 0	Ι
If $NBS = 0$	Normal value. No other record required		
If NBS = -2	The map is modified as follows :		
$R_0, \Delta B/B_0$	B transforms to $B * \left(1 + \frac{\Delta B}{B_0} \frac{R - R_0}{RMAX - RMIN} \right)$	cm, no dim	2*E
If NBS = -1	the map is modified as follows :		
$\theta_0, \Delta B/B_0$	B transforms to $B * \left(1 + \frac{\Delta B}{B_0} \frac{\theta - \theta_0}{AT} \right)$	deg, no dim	2*E

If NBS ≥ 1	Introduction of NBS shims		
For I = 1, NBS	The following 2 records must be repeated NBS times		
$R_1, R_2, heta_1, heta_2, \lambda$	Radial and angular limits of the shim ; λ is unused	2*cm, 2*deg, cm	5*E
$\gamma, \alpha, \mu, \beta$	geometrical parameters of the shim	2*deg, 2*no dim	4*E
IORDRE	Degree of interpolation polynomial : 2 = second degree, 9-point grid 25 = second degree, 25-point grid 4 = fourth degree, 25-point grid	2, 25 or 4	Ι
XPAS	Integration step	cm	Е
KPOS	Positioning of the map, normally 2. Two options :	1-2	Ι
If KPOS = 2 RE, TE, RS, TS	Positioning as follows : Radius and angle of reference, respectively, at entrance and exit of the map.	cm, rad, cm, rad	4*E
If KPOS = 1 <i>DP</i>	Automatic positioning of the map, by means of reference relative momentum	no dim	E

DIPOLES	Dipole magnet <i>N</i> -tuple, polar frame Depending on <i>KIRD[.i]</i> below:	(page 101 in PART A)	
	(i) $B_Z = \sum_{i=1}^{N} B_{Z0,i} \mathcal{F}_i(R,\theta) \left(1 + b_{1_i}(R - RM_i)/RM_i + b_{2_i}(R,\theta)\right)$ (ii) $B_Z = B_{Z0,i} + \sum_{i=1}^{N} \mathcal{F}_i(R,\theta) \left(b_{1_i}(R - RM_i) + b_{2_i}(R - RM_i)\right)$	$((R - RM_i)^2 / RM_i^2 +)$)	
		dim.	data type	FIT num.
IL	$IL = 1, 2[\times 10^n], 7$: print coordinates, fields, etc., step-by-step, in zgoubi.res (1), zgoubi.plt (2), zgoubi.impdev.out (7).	$0-2[\times 10^n], 7$	Ι	
N, AT, RM	Number of magnets in the N -tuple ; total angular extent of the dipole ; reference radius	no dim, deg, cm	I, 2*E	2-4
Repeat N times the fo	llowing sequence			
ACN, δRM^{1} , B_{0} , ind, b_{i} , $(i = 1, ind)$	Positioning of EFBs : azimuth, $RM_i = RM + \delta RM$; field ; number of, and field indices at $R \equiv RM$ ($b_1 = \frac{RM}{B_0} \frac{dB}{dR}$; $b_2 = \frac{RM}{2B_0} \frac{d^2B}{dR^2}$; etc.).	deg., cm, kG, $(ind + 1)$ *no dim	3*E, I, ind*E	5-7, 8-(8+ind)
g_0,κ	ENTRANCE FIELD BOUNDARY Fringe field extent $(g = g_0 (RM/R)^{\kappa})$ Exponential type fringe field $F = 1 / (1 + \exp(P(s)))$ with $P(s) = C_0 + C_1(\frac{s}{q}) + C_2(\frac{s}{q})^2 + + C_5(\frac{s}{q})^5$	cm, no dim	2*E	(9+ind) to (10+ind)
$NC, C_0 - C_5$, shift	Unused ; C_0 to C_5 : see above ; EFB shift	0-6, 6*no dim, cm	I, 7*E	etc.
$\omega^+, \theta, R_1, U_1, U_2, R_2$	Azimuth of entrance EFB with respect to ACN ; wedge angle of EFB; radii and linear extents of EFB (use $U_{\frac{1}{2}} = \mp \infty$ when $R_{1,2} = \infty$)	2*deg, 4*cm	6*E	
	(Note : $\lambda = 0$, $\omega^+ = ACN$ and $\theta = 0$ for sharp edge)			
	EXIT FIELD BOUNDARY (See ENTRANCE FIELD BOUNDA	RY)		
$\begin{array}{l} g_0,\kappa\\ NC,C_0-C_5,\text{shift}\\ \omega^-,\theta,R_1,U_1,U_2,R_2 \end{array}$		cm, no dim 0 – 6, 6*no dim, cm 2*deg, 4*cm	2*E 1, 7*E 6*E	
	(Note : $\lambda = 0$, $\omega^{-} = -AT + ACN$ and $\theta = 0$ for <u>sharp edge</u>)			
	LATERAL FIELD BOUNDARY to be implemented - following	data not used		
g_0,κ		cm, no dim	2*E	
$NC, C_0 - C_5$, shift $\omega^-, \theta, R_1, U_1, U_2, R_2,$ End of repeat	RM3	0-6, 6*no dim, cm 2*deg, 5*cm	1, 7*E 7*E	
KIRD[.i], Resol	If KIRD=0 : analytical computation of field derivatives, and . i=0 or absent : default, B_Z formula (i) above, i=1 : B_Z formula . i=7-9 : S. Ruggiero's FFAG (see dipsi.f routine), . Resol = 2/4 for 2nd/4th order field derivatives computation. If KIRD=2, 25 or 4 : numerical interpolation of field derivatives, a . size of flying interpolation mesh is <i>XPAS/Resol</i> . KIRD=2 or 25 : second degree, 9- or 25-point grid . KIRD=4 : fourth degree, 25-point grid	0, 2, 25 or 4 ; no dim (ii),	I, E	
XPAS	Integration step	cm	Е	
KPOS	Positioning of the magnet, normally 2. Two options :	1-2	Ι	
If KPOS = 2 <i>RE</i> , <i>TE</i> , <i>RS</i> , <i>TS</i>	Positioning as follows : Radius and angle of reference, respectively, at entrance and exit of the magnet	cm, rad, cm, rad	4*E	
If KPOS = 1 <i>DP</i>	Automatic positioning of the magnet, by means of reference relative momentum	no dim	E	

DODECAPO	Dodecapole magnet		
IL	$IL = 1, 2[\times 10^n], 7$: print coordinates, fields, etc., step-by-step, in zgoubi.res (1), zgoubi.plt (2), zgoubi.impdev.out (7).	$0-2[\times 10^n], 7$	Ι
XL, R_0, B_0	Length ; radius and field at pole tip	2*cm, kG	3*E
X_E, λ_E	Entrance face : Integration zone extent ; fringe field extent ($\leq 2R_0, \lambda_E = 0$ for sharp edge)	2*cm	2*E
<i>NCE</i> , $C_0 - C_5$	NCE = unused $C_0 - C_5$ = Fringe field coefficients such that $G(s) = G_0/(1 + \exp P(s))$, with $G_0 = B_0/R_0^5$ and $P(s) = \sum_{i=0}^5 C_i(s/\lambda)^i$	unused, 6*no dim	I, 6*E
X_S, λ_S NCS, $C_0 - C_5$	Exit face : see entrance face	2*cm 0-6, 6*no dim	2*E I, 6*E
XPAS	Integration step	cm	Е
KPOS, XCE, YCE, ALE	KPOS=1 : element aligned, 2 : misaligned ; shifts, tilt.	1-2, 2*cm, rad	I, 3*E



DRIFT, ESL Field free drift space

XL [, 'split', N [, IL]]length; 'split', optional, will split into N segments ;cmIL=0, 1 or 2 (0 is default, no logging), optional, causes particle data to be
logged in zgoubi.res (IL=1) or zgoubi.plt (IL=2); IL=0 inhibits logging.

Е



• Example : DRIFT

 \diamond Default format of *DRIFT*, to push particles 30 cm ahead :

'DRIFT' 30.3 \diamond It can be split into 10, 3 cm long pieces. Optionally, using *IL*=2 will cause particle data print out to zgoubi.plt, at the downstream end of each piece.

```
'DRIFT'
30.3 split 10 2
```

◊ Two equivalent methods to cause particle data logging in zgoubi.plt at the downstream end of a drift. 'DRIFT_0' is LABEL1 here, '.plt' is LABEL2.

'DRIFT'	DRIFT_	_0	'DRIFT'	DRIFT_0	.plt
30.3	split 1	2	30.3		

EBMULT ¹	Electro-magnetic multipole	(page 107 in PART A)		
		dim.	data type	FIT num.
IL	$IL = 1, 2[\times 10^n], 7$: print coordinates, fields, etc., step-by-step, in zgoubi.res (1), zgoubi.plt (2), zgoubi.impdev.out (7).	$0-2[\times 10^n], 7$	Ι	1
XL, R_0 , $\phi 1$, $\phi 2$,, $\phi 10$	Electric poles Length of element ; radius at pole tip ; potential at pole tip for dipole, quadrupole, , 20-pole electric components	2*cm, 10*V	12*E	2-13
$X_E, \lambda_E, E_2,, E_{10}$	Entrance face Integration zone ; fringe field extent : dipole fringe field extent = λ_E ; quadrupole fringe field extent = $\lambda_E * E_2$; etc. ; 20-pole fringe field extent = $\lambda_E * E_{10}$ (for any component : sharp edge if field extent is zero)	2*cm, 9*no dim	11*E	14-24
<i>NCE</i> , $C_0 - C_5$	same as QUADRUPO	0-6, 6*no dim	I,6*E	25-31
$X_S, \lambda_S, S_2, \dots, S_{10}$	Exit face Integration zone ; as for entrance	2*cm, 9*no dim	11*E	32-42
<i>NCS</i> , $C_0 - C_5$		0-6, 6*no dim	I, 6*E	43-49
<i>R</i> 1, <i>R</i> 2, <i>R</i> 3,, <i>R</i> 10	Skew angles of electric field components	10*rad	10*E	50-59
XL, R ₀ , B1, B2,, B10	Magnetic poles Length of element ; radius at pole tip ; field at pole tip for dipole, quadrupole, , 20-pole magnetic components	2*cm, 10*kG	12*E	60-71
$X_E, \lambda_E, E_2,, E_{10}$	Entrance face Integration zone ; fringe field extent : dipole fringe field extent = λ_E ; quadrupole fringe field extent = $\lambda_E * E_2$; etc. ; 20-pole fringe field extent = $\lambda_E * E_{10}$ (for any component : sharp edge if field extent is zero)	2*cm, 9*no dim	11*E	72-82
<i>NCE</i> , $C_0 - C_5$	same as QUADRUPO	0-6, 6*no dim	I,6*E	83-89

		dim.	data type	FIT num.
$X_S, \lambda_S, S_2,, S_{10}$	Exit face Integration zone ; as for entrance	2*cm, 9*no dim	11*E	90-100
<i>NCS</i> , $C_0 - C_5$		0-6, 6*no dim	I, 6*E	101-107
<i>R</i> 1, <i>R</i> 2, <i>R</i> 3,, <i>R</i> 10	Skew angles of magnetic field components	10*rad	10*E	108-117
XPAS	Integration step	cm	Е	118-120
KPOS, XCE, YCE, ALE	KPOS=1 : element aligned, 2 : misaligned ; shifts, tilt.	1-2, 2*cm, rad	I, 3*E	121-125



EL2TUB ¹	Two-tube electrostatic lens		
IL	$IL = 1, 2[\times 10^n], 7$: print coordinates, fields, etc., step-by-step, in zgoubi.res (1), zgoubi.plt (2), zgoubi.impdev.out (7).	$0-2[\times 10^n]$, 7	Ι
X_1, D, X_2, R_0	Length of first tube ; distance between tubes ; length of second tube ; inner radius	3*m	4*E
V_1, V_2	Potentials	2*V	2*E
XPAS	Integration step	cm	Е
KPOS, XCE, YCE, ALE	KPOS=1 : element aligned, 2 : misaligned ; shifts, tilt.	1-2, 2*cm,	I, 3*E



Two-electrode cylindrical electric lens.

ELMIR	Electrostatic N-electrode mirror/lens, straight slits		
IL	$IL = 1, 2[\times 10^n], 7$: print coordinates, fields, etc., step-by-step, in zgoubi.res (1), zgoubi.plt (2), zgoubi.impdev.out (7).	$0-2[\times 10^n], 7$	Ι
N, <i>L</i> 1,, <i>LN</i> , <i>D</i> , <i>MT</i>	Number of electrodes ; electrode lengths ; gap ; mode (11/H-mir, 12/V-mir, 21/V-lens, 22/H-lens)	2-7, N*m, m	I, N*E, E, I
V1,, VN	Electrode potentials (normally $V1 = 0$)	N*V	N*E
XPAS	Integration step	cm	Е
KPOS, XCE, YCE, ALE	KPOS=1: element aligned; 2: misaligned; shifts, tilt; 3: automatic positioning, $YCE =$ pitch, $ALE =$ half-deviation	1-2, 2*cm, rad	I, 3*E



Electrostatic N-electrode mirror/lens, straight slits, in the case N = 3, in horizontal mirror mode (MT = 11). Possible non-zero entrance quantities YCE, ALE should be specified using CHANGREF, or using KPOS=3 with YCE and ALE=half-deviation matched to the reference trajectory.

ELCYLDEF	Electrostatic cylindrical deflector	(page 109 in PART A)					
UN	UNDER DEVELOPMENT. To be documented.						
IL	$IL = 1, 2[\times 10^n], 7$: print coordinates, fields, etc., step-by-step, in zgoubi.res (1), zgoubi.plt (2), zgoubi.impdev.out (7).	$0-2[\times 10^n], 7$	Ι				
Dev, RM, E, Ind [, MOD [, K2, K3]]	Deviation; reference radius, E-field at RM; index; potential model (1-3: default, Wollnik, Ikegami); 2nd and 3rd order field index (only used if MOD=3).	rad, m, V/m, - [, 1-3 [, -, -]]	4*E [, I [, 2*E]]				
X_E, λ_E	Entrance face : Integration zone extent ; fringe field extent ($\simeq 2R_0, \lambda_E = 0$ for sharp edge)	2*cm	2*E				
<i>NCE</i> , $C_0 - C_5$	<i>NCE</i> = unused $C_0 - C_5$ = Fringe field coefficients such that $G(s) = G_0/(1 + \exp P(s))$, with $G_0 = B_0/R_0$ and $P(s) = \sum_{i=0}^5 C_i(s/\lambda)^i$	0-6, 6*no dim	I, 6*E				
X_S, λ_S NCS, $C_0 - C_5$	Exit face See entrance face	2*cm 0-6, 6*no dim	2*E I, 6*E				
XPAS	Integration step	cm	E				
KPOS	Positioning of the map, normally 2. Two options :	1-2	Ι				
KPOS RE, TE, RS, TS	KPOS=2, positioning as follows : Radius and angle of reference, respectively, at entrance and exit of the defelctor (as in DIPOLE, see Fig. B, p. 253).	2 cm, rad, cm, rad	I 4*E				

ELMIRC	Electrostatic N-electrode mirror/lens, circular slits		
IL	$IL = 1, 2[\times 10^n], 7$: print coordinates, fields, etc., step-by-step, in zgoubi.res (1), zgoubi.plt (2), zgoubi.impdev.out (7).	$0-2[\times 10^n], 7$	Ι
R1, R2, AT, D	Radius of first and second slits ; total deviation angle ; gap	4*m 2*m, rad, m	4*E 4*E
V - VA, VB - V	Potential difference	2*V	2*E
XPAS	Integration step	cm	Е
<i>KPOS</i> RE, TE, RS, TS	Normally $KPOS = 2$ for positioning ; Radius and angle at respectively entrance and exit.	1-2 cm, rad, cm, rad	I 4*E



Electrostatic N-electrode mirror/lens, circular slits, in the case N = 3, in horizontal mirror mode.

ELMULT ¹	Electric multipole		
IL	$IL = 1, 2[\times 10^n], 7$: print coordinates, fields, etc., step-by-step, in zgoubi.res (1), zgoubi.plt (2), zgoubi.impdev.out (7).	$0-2[imes 10^n]$, 7	Ι
XL, R ₀ , E1, E2,, E10	Length of element ; radius at pole tip ; field at pole tip for dipole, quadrupole, , dodecapole components	2*cm, 10*V/m	12*E
$X_E, \lambda_E, E_2,, E_{10}$	Entrance face Integration zone ; fringe field extent : dipole fringe field extent = λ_E ; quadrupole fringe field extent = $\lambda_E * E_2$; 20-pole fringe field extent = $\lambda_E * E_{10}$ (sharp edge if field extent is zero)	2*cm, 9*no dim	11*E
$NCE, C_0 - C_5$	same as QUADRUPO	0-6, 6*no dim	I, 6*E
$X_S, \lambda_S, S_2,, S_{10}$ NCS, $C_0 - C_5$	Exit face Integration zone ; as for entrance	2*cm, 9*no dim 0-6, 6*no dim	11*E I, 6*E
<i>R</i> 1, <i>R</i> 2, <i>R</i> 3,, <i>R</i> 10	Skew angles of field components	10*rad	10*E
XPAS	Integration step	cm	E
KPOS, XCE, YCE, ALE	<i>KPOS</i> =1 : element aligned, 2 : misaligned ; shifts, tilt.	1-2, 2*cm, rad	I, 3*E



¹ Use *PARTICUL* to declare mass and charge.

ELREVOL ¹	1-D uniform mesh electric field map X-axis cylindrical symmetry is assumed		
IC, IL	IC = 1, 2: print the map $IL = 1, 2[\times 10^n], 7$: print coordinates, fields, etc., step-by-step, in zgoubi.res (1), zgoubi.plt (2), zgoubi.impdev.out (7).	$0-2; 0-2[\times 10^n], 7$	2*I
ENORM, X-NORM	Field and X-coordinate unit conversion coeff. Convert values as read from map file, to MV/cm and cm units.	2*UnitConv.	2*E
TITL	Title. Start with "FLIP" to get field map X-flipped.		A80
IX	Number of longitudinal nodes of the map	≤ 400	Ι
FNAME ²	File name		A80
ID, A, B, C [, A', B', C', B", etc., if $ID \ge 2$]	Integration boundary. Ineffective when $ID = 0$. $ID = -1$, 1 or ≥ 2 : as for <i>CARTEMES</i>	≥ -1, 2*no dim, cm [,2*no dim, cm, etc.]	I,3*E [,3*E,etc.]
IORDRE	Unused	2, 25 or 4	Ι
XPAS	Integration step	cm	Е
KPOS, XCE, YCE, ALE	KPOS=1 : element aligned, 2 : misaligned ; shifts, tilt.	1-2, 2*cm, rad	I, 3*E

¹ Use *PARTICUL* to declare mass and charge.

 2 FNAME (e.g., e-lens.map) contains the field data. These must be formatted according to the following FORTRAN sequence :

OPEN (UNIT = NL, FILE = FNAME, STATUS = 'OLD' [,FORM='UNFORMATTED']) DO 1 I = 1, IX IF (BINARY) THEN READ(NL) X(I), EX(I) ELSE READ(NL,*) X(I), EX(I) ENDIF 1 CONTINUE

where X(I) and EX(I) are the longitudinal coordinate and field component at node (I) of the mesh. Binary file names *FNAME* must begin with 'B_' or 'b_'. 'Binary' will then automatically be set to '.TRUE.'

ЕММА	2-D Cartesian or cylindrical mesh field map for EMMA FFAG	(page 115 in PART	ГА)
IL	$IL = 1, 2[\times 10^n], 7$: print coordinates, fields, etc., step-by-step, in zgoubi.res (1), zgoubi.plt (2), zgoubi.impdev.out (7).	$0-2[imes 10^n], 7$	Ι
BNORM, XN, YN, ZN	Field and X-,Y-,Z-coordinate unit conversion coefficients. Convert values as read from map file, to kG and cm or rad.	4*UnitConv.	4*E
TITL	Title. Start with "FLIP" to get field map X-flipped		A80
IX, IY, IZ, MOD[.i]	Number of nodes of the mesh in the X, Y and Z directions, $IZ = 1$ for single 2-D map; MOD: operational and map FORMAT reading mode ¹ $MOD \le 19$: Cartesian mesh; $MOD \ge 20$: cylindrical mesh; . <i>i</i> , optional, tells the reading FORMAT, default is '*'.	$\leq 400, \leq 200,$ 1, $\geq 0[.1-9]$	3*I
FNAME ¹ (K = 1, NF)	Names of the NF files that contain the 2-D maps, ordered from $Z(1)$ to $Z(NF)$. If $MOD=0$: a single map, superimposition of QF and QD ones, is but If $MOD=1$: a single map, interpolated from QF[x_F] and QD[x_D] o If $MOD=22$: a single map, superimposition of QF and QD ones, is but If $MOD=24$: field at particle is interpolated from a (QF,QD) pair of current (x_F, x_D) value, taken from of set of (QF,QD) pairs registered	uilt for tracking. nes, is built for tracki puilt for tracking. maps, closest to 1 in FNAME	A80 ing.
ID, A, B, C [, A', B', C', B", etc., if $ID \ge 2$]	Integration boundary. Ineffective when $ID = 0$. $ID = -1$, 1 or ≥ 2 : as for CARTEMES	≥ -1, 2*no dim, cm [,2*no dim, cm, etc.]	I,3*E [,3*E,etc.]
IORDRE	If $IZ = 1$: as in CARTEMES If $IZ \neq 1$: unused	2, 25 or 4	Ι
XPAS	Integration step	cm	Е
KPOS, XCE, YCE, ALE	KPOS=1 : element aligned, 2 : misaligned ; shifts, tilt.	1-2, 2*cm, rad	I, 3*E

ERRORS	Injecting errors in optical elements (UNDER DEVELOPMENT)	(page 155 in PA	ART A)
ONF, NBR, SEED [, PRINT]	On/off switch (1/0) ; number of error sets to be injected (<i>i.e.</i> , as well, number of lines following this one) ; random seed. Occurence of <i>PRINT</i> will save error series in zgoubi.ERRORS.	,,,[,] out.	I1, I, I [,A5]
The next line depends on the op (only limited possibilities at the	ptical element of concern, and is to be one of the following : moment, under development)		
MULTIPOL[{LBL1 [,LBL2]}], N, TYP, AR, UG, VC, HW, CUTOFF	Keyword concerned [optionally, first and/or second label ; wilds cards accepted: *LBL1-2, LBL1-2*] ; N=1-10 : pole concerned if TYP=BP or =XR, otherwise ignored TYP= BP : field at pole/kG (dipole to 20-pole), or XR : pole rol (dipole to 20-pole), or ZS : vertical shift of MULTIPOL/cm; AR=A or R : error value is absolute or relative (to current one) ; UG=U or G : uniform or Gaussian random law ; VC= central value ; HW= half-width (case UG=U) or sigma (ca cut-off value in units of sigma (unused if UG=U).	e ,[,],,,,2*kG, d ; l-angle/rad ; use UG=G) ;	A8 [,A20[,A20]], I, A2, A1, A1, 3*E
TOSCA[{LBL1 [,LBL2]}], N, TYP, AR, UG, VC, HW, CUTOFF	Keyword concerned [optionally, first and/or second label] ; N is unused ; TYP= BP : field coefficient <i>BNORM</i> ; AR, UG, etc. : see above.	,[,],,,,2*kG,	A8 [,A20[,A20]], I, A2, A1, A1, 3*E

• Example : ERRORS

'ERRORS'											
1 5 123466				!		cut-	-01	ff			
MULTIPOL{KCV}	1	BP R	U	0.d0	1e-3	0	!	cutoff	unu	ised	(U)
MULTIPOL{B}	2	XR A	U	0.d0	0.349e-3	0					
<pre>MULTIPOL{*_QF}</pre>	1	XR A	U	1.57079632679	0.	0					
<pre>MULTIPOL{*_QF}</pre>	1	BP A	U	0.	0.004	0					
TOSCA	1	BP A	G -	-1.d-3	1.e-5	3	!	cutoff	at	3-si	gma

In this example the various attributes of the error keyword take the following values and meanings : \diamond 1st line :

- ONF = 1 : error setting is on ; NBR=3 : three error setting lines follow ; seed = 123456 \diamond 2nd line :

- all *MULTIPOL* keywords with first label "*KCV*" in the optical sequence are concerned; multipole component ip=1 is affected, *i.e.*, dipole component; "*BP*, *R*, *U*, *0.d0*, *1e-3*, *0*": a random relative defect dB/B (AR=R) concerning the field $B_{\rm ip}$ (TYP=BP) for that component, will be sorted in a uniform (UG=U) distribution centered on $V_{\rm ip} = 0$ (VC=0.d0) with half-width $HW = 10^{-3}$, CUTOFF at n-sigma (n=0 here) is unused (only used for Gaussian distributions, case UG=G) - $B_{\rm ip}$ is changed to $B_{\rm ip} + V_{\rm ip} + dB/B \times B_{\rm ip}$.

◇ 3rd line :
- all MULTIPOL keywords with first label "B" in the optical sequence are concerned ; multipole component ip=2 is affected, *i.e.*, quadrupole component ; "XR, A, U, 0.d0, 0.349e-3, 0 : a random absolute defect dR_{ip} (AR=A) of the roll-angle R_{ip} (TYP=XR) for that component, will be sorted in a uniform (UG=U) distribution centered on V_{ip} = 0 (VC=0.d0) with half-width HW = 0.349 × 10⁻³ rad, CUTOFF at n-sigma (n=0 here) is unused (only used for Gaussian distributions, case UG=G)
- R_{ip} is changed to R_{ip} + V_{ip} + dR_{ip}.

◊ 4th and 6th lines :

- all *MULTIPOL* keywords in the optical sequence with first label of the form "*_*QF*" are concerned ('*' is a wilde card). Their dipole component is applied a $\pi/2$ skewing 4th line), and that skewed dipole field is given a value at random, unform, within [-0.004,0.004] kG (5th line).

♦ 6th line :

- all *TOSCA* keywords in the optical sequence are concerned; field map field coefficient *BNORM* (see TOSCA keyword) is affected; *BP*, *A*, *G*, -1.*d*-3, 1.*e*-5, 3 : a random absolute defect *dBN* (AR=A) concerning *BNORM* (TYP=BP) will be sorted in a Gaussian (UG=G) distribution centered on $BNC = -10^{-3}$ (VC=-1.d-3) with *rms* value $HW = 10^{-5}$, CUTOFF 3-sigma - *BNORM* is changed to BNC + dBN (not to BNORM + BNC + dBN !). (If AR=R instead : random relative defect dBN/BN generated, and BNORM changed to VC + dBN/BN).

FAISCEAU [, FORCE] Print particle coordinates

Printout (in zgoubi.res) particle coordinates at the location where the keyword is introduced in the structure. If first label is 'FORCE', will force printout when normally inhibited (*e.g.*, by *OPTIONS[WRITE]* or *REBELOTE[KWRIT]*)

FAISCNL	Store particle coordinates in file FNAME	
$FNAME^1$	Name of storage file (<i>e.g.</i> , zgoubi.fai, or b_zgoubi.fai for binary storage).	A80
FAISTORE	Store coordinates every <i>IP</i> other pass [, at elements with appropriate label]	
FNAME ¹ [,LABEL(s)]	Name of storage file (<i>e.g.</i> zgoubi.fai). Optional : a list of up to 10 labels, (the first label of element(s) at the exit of which the store should occur) ; wild card accepted, in the form ' <i>*LABEL</i> ' or ' <i>LABEL*</i> ' or ' <i>*LABEL*</i> '. If either <i>FNAME</i> or first <i>LABEL</i> in the list is 'none' then <i>FAISTORE</i> is inhibited. Store occurs at all elements if the list begins with <i>LABEL</i> =all or ALL.	A80, [, 0-10*A20]
IP	Store every <i>IP</i> other pass (when using <i>REBELOTE</i> with <i>NPASS</i> $\geq IP - 1$).	Ι

FFAG	FFAG magnet, N-tuple	(page 116 in PART A	A)
	UNDER DEVELOPMENT $D = \sum_{i=1}^{N} D = T(D, 0) (D/D) ^{K_i}$		
	$B_Z = \sum_{i=1} B_{Z0,i} \mathcal{F}_i(R,\theta) (R/R_{M,i})$		
IL	$IL = 1, 2[\times 10^n], 7$: print coordinates, fields, etc., step-by-step,	$0-2[\times 10^n], 7$	Ι
	in zgoubi.res (1), zgoubi.plt (2), zgoubi.impdev.out (7).		
N, AT, RM	Number of dipoles in the FFAG N-tuple ;	no dim,	I, 2*E
	total angular extent of the dipole ; reference radius	deg, cm	
Repeat N times the follow	ving sequence		
ACN δBM	Azimuth for dipole positioning : $B_{M,i} = BM + \delta BM$:	deg cm kG	4*E
B_{Z0}, K	field at $R_{M,i}$; index	no dim	1 2
	ENTRANCE FIELD BOUNDARY		
00 K	Fringe field extent $(a = a_0 (BM/B)^{\kappa})$	cm_no dim	2*E
$NC, C_0 - C_5$, shift	Unused ; C_0 to C_5 : fringe field coefficients ; EFB shift	0-6, 6*no dim, cm	I, 7*E
$\omega^+, \theta, R_1, U_1, U_2, R_2$	Azimuth of entrance EFB with respect to ACN;	2*deg, 4*cm	6*E
, , 1, 1, 2, 2	wedge angle of EFB ; radii and linear	0,	
	extents of EFB (use $U_{\frac{1}{2}} = \mp \infty$ when $R_{1,2} = \infty$)		
	(Note : $g_0 = 0$, $\omega^+ = ACN$, $\theta = 0$ and KIRD=0 for sharp edge)		
	EXIT FIELD BOUNDARY (See ENTRANCE FIELD BOUNDARY)		
q_0, κ	Fringe field parameters, see above	cm, no dim	2*E
$NC, C_0 - C_5$, shift		0-6, 6*no dim, cm	1,7*E
$\omega^-, \theta, R_1, U_1, U_2, R_2$		2*deg, 4*cm	6*E
	(Note : $g_0 = 0, \omega^- = -AT + ACN, \theta = 0$ and KIRD=0 for sharp edge	<u>ge</u>)	
	LATERAL FIELD BOUNDARY to be implemented - following data	a not used	
g_0, κ		cm, no dim	2*E
$NC, C_0 - C_5$, shift		0-6, 6*no dim, cm	1,7*E
$\omega^-, \theta, R_1, U_1, U_2, R_2$		2*deg, 4*cm	6*E
End of repeat			
KIRD Resol	If KIRD=0 : analytical computation of field derivatives :	0.2.25 or 4.	ΙE
Rinde, Resol	Resol = 2/4 for 2nd/4th order field derivatives computation	no dim	г, ш
	If KIRD -2 4 or 25 : numerical interpolation of field derivatives :	no uni	
	size of flying interpolation mesh is $XPAS/Resol$		
	KIRD-2 or 25 · second degree 9- or 25-point grid		
	KIRD=4 · fourth degree 25-noint grid		
	Mind - 1. Iourui degree, 25 point gild		
XPAS	Integration step	cm	E
KPOS	Positioning of the magnet, normally 2. Two options :	1-2	Ι
If KPOS = 2	Positioning as follows :		
RE, TE, RS, TS	Radius and angle of reference, respectively,	cm, rad, cm, rad	4*E
	at entrance and exit of the magnet		
If KPOS = 1	Automatic positioning of the magnet, by means of		
DP	reference relative momentum	no dim	Е

FFAG-SPI	Spiral FFAG magnet, N-tuple UNDER DEVELOPMENT $B_Z = \sum_{i=1}^N B_{Z0,i} \mathcal{F}_i(R,\theta) (R/R_{M,i})^{K_i}$		
IL	$IL = 1, 2[\times 10^n], 7$: print coordinates along trajectories, fields, etc., into zgoubi.res (1) or zgoubi.plt ($2[\times 10^n]$) or zgoubi.impdev.out (7).	$0-2[\times 10^n], 7$	Ι
N, AT, RM	Number of dipoles in the FFAG <i>N</i> -tuple ; total angular extent of the dipole ; reference radius.	no dim, deg, cm	I, 2*E
Repeat N times the follow	ving sequence		
ACN, δRM , B_{Z0}, K	Azimuth for dipole positioning ; $R_{M,i} = RM + \delta RM$; field at $R_{M,i}$; index.	deg, cm, kG, no dim	4*E
	ENTRANCE FIELD BOUNDARY		
g_0, κ NC, $C_0 - C_5$, shift $\omega^+, \xi, 4$ dummies	Fringe field extent $(g = g_0 (RM/R)^{\kappa})$ Unused; C_0 to C_5 : fringe field coefficients; EFB shift Azimuth of entrance EFB with respect to ACN; spiral angle; $4 \times$ unused.	cm, no dim 0-6, 6*no dim, cm 2*deg, 4*unused	2*E I, 7*E 6*E
	EXIT FIELD BOUNDARY (See ENTRANCE FIELD BOUNDARY))	
g_0, κ $NC, C_0 - C_5$, shift $\omega^-, \xi, 4$ dummies	Fringe field parameters, see above	cm, no dim 0-6, 6*no dim, cm 2*deg, 4*unused	2*E 1, 7*E 6*E
	LATERAL FIELD BOUNDARY to be implemented - following dat	a not used	
g_0, κ $NC, C_0 - C_5$, shift $\omega^-, \theta, R_1, U_1, U_2, R_2$		cm, no dim 0-6, 6*no dim, cm 2*deg, 4*cm	2*E 1, 7*E 6*E
End of repeat			
Integration boundaries -	next line is optional starting with string Int Lim.		
IntLim, <i>ID</i> , <i>A</i> , <i>B</i> , <i>C</i> [, <i>A</i> ', <i>B</i> ', <i>C</i> ']	Integration boundary. Line has to start with 'IntLim'. ID = -1: integration in the magnet begins at entrance boundary defined by A, B, C. ID = 1: integration is terminated at exit boundary defined by A', B', C'. ID = 2: both entrance and exit boundaries.	-1, 1, 2; deg; cm; deg [; <i>id</i> .]	I, 3*E [,3*E]
KIRD, Resol [, DNEWT]	If KIRD=0 : analytical computation of field derivatives ; Resol = $2/4$ for $2nd/4$ th order field derivatives computation	0, 2, 25 or 4 ;	I, E

	If DNEWT is added, the distance to the magnet edge is calculated numerically (in the case KIRD \neq 0). In its absence, and if $\kappa = -1$, then the distance in terms of generalised azimuthal angle is used instead.					
XPAS	Integration step	cm	Е			
KPOS , RE, TE, RS, TS	Positioning of the magnet, has to be 2. As follows : radius and angle of reference, respectively, at entrance and exit of the magnet.	2, 2*(cm, rad)	I, 4*E			

If KIRD = 2, 4 or 25: numerical interpolation of field derivatives;

KIRD=2 or 25 : second degree, 9- or 25-point grid

size of flying interpolation mesh is XPAS/Resol.

KIRD=4 : fourth degree, 25-point grid

FIN, END End of input data list

Any information in zgoubi.dat following these keywords will be ignored

FIT, FIT2	Fitting procedure	(page 156 in PART A))
NV [, nofinal] [, noSYSout] [, save [, FileName]]	NV : Number of physical parameters to be varied ; 'nofinal' avoids final run (default is : final run performed using fitted values, once fit is done) ; 'noSYSout' inhibits system output of variable and constraint status, except for start and end, and update of penalty value in between ; 'save' saves fit variables when fit is completed, either in 'FileName' if specified, or by default in zgoubi.FITVALS.out.	≤ 20 [, nofinal] save [string]	I [, A7] [, A4 [, A80]]
For I = 1, NV	repeat NV times the following sequence		
indifferently, either : IR, IP, XC, DV	Number of the element in the structure (see p. 157); number of the physical parameter in the element; coupling switch of the form int1.int2, with int1.int2< 0 if coupled variation is to be with opposite signs, or int1.int2> 0 for same sign variation; relative variation range (\pm).	\leq MXL ¹ , \leq MXD ¹ , \pm MXL.MXD ² , relative or [v1,v2]	2*I, 2*E
or : IR, IP, XC, $[V_{min}, V_{max}]$	<i>IR</i> , <i>IP</i> , <i>XC</i> as above; V_{min} , V_{max} : lower and upper limits of the variable, absolute ³ .		2*I, 3*E
NC [, Penalty [,ITER]] ⁴	Number of constraints [, penalty [, max. numb. of iterations]].	$\leq 20 [, 10^{-n} [, > 0]]$	I [, E [, I]]
For I = 1, NC	repeat NC times the following sequence :		
$IC[.JC], I, J, IR, V^3,$ WV, NP $[, p_i(i = 1, NP)]$	IC, I and J define the type of constraint (see table below); IR : number of the element after which the constraint applies, or IR = #End to apply at end of the sequence (<i>i.e.</i> , just bfore <i>FIT</i> [2]; V : value; W : weight (the stronger the lower WV); NP : number of parameters, and, <i>iff</i> NP \geq 1 then provide N parameter values $p_i(i = 1, NP)$.	0-5, 3*(>0), current unit, 2*no dim., curr. units	I[.I1], 3*I, 2*E, I, <i>NP</i> *E

¹ The values for the maximum number of elements (*i.e.*, keywords in zgoubi.dat) that a sequence in zgoubi can contain, MXL, and for the maximum number of parameters under a keyword, MXD, are set in the include file MXLD. H. 2 The coupling input data VC is a fit of the file MXLD.

The coupling input data XC is of the form "integer1 integer2" with integer1 \leq MXL and integer2 \leq MXD. MXL and MXD are the maximum number of elements, and data in an optical element, defined in MXLD.H include file: can be increased there, if necessary, then requires re-compiling.

 $^{^{3}}$ V is in current **zgoubi** units in the case of particle coordinates (*i.e.*, cm, mrad, μ s, momentum relative to BORO) and B field (kG). It is in MKSA units (m, rad) in the case of matrix coefficients. ⁴ FIT[2] will stop when the sum of the squared residuals gets < penalty, or when the maximum allowed number of iterations is reached.

• Examples : Combining FIT and REBELOTE

Combining FIT and REBELOTE, Example 1:

In the example below, *FIT* requests that (i) the particle trajectory with initial coordinates defined by *OBJET* have identical horizontal coordinates at both ends of the snake (this is achieved by varying Y_0 , T_0 in *OBJET*), and that (ii) the trajectory across the snake - an helix - be *Y*-centered along the snake axis.

The way this works :

FIT is executed a first time for $B\rho_{ref} = BORO = 7205.1782956$ kG.cm, namely the execution loops between *OBJET* and *FIT* until the constraints are best fulfilled. Once this is completed, the execution pointer then goes to the next instruction in the data list, namely '*SPNPRT*', this is discussed below, and then points to *REBELOTE*, which will have the effect of sending it back to the begining of zgoubi.dat data list. However, prior to that, the "*IOPT=1*" flag, fourth data in first row in *REBELOTE*, requests a change of, next line, parameter number 35 in element "*OBJET*" (that is, the relative regidity of the particle, *D*). The list of values follows, namely, {1.3872739973 2.1368296674 4.8261190694 11.015241321}. The change occurs **4** times, according to *NRBLT=4*, the first data in *REBELOTE* data list.

Note that, (i) spin data so computed (spin vector components, precession, etc) are stored/stacked in zgoubi.SPNPRT.Out by placing the keyword 'SPNPRT' with label "PRINT", between FIT and REBELOTE; (ii) current updated FIT variables are saved in zgoubi.FITVALS.out using the 'save' command in FIT, and further stacked in zgoubi.FITVALS.out_cat for each REBELOTE case, using SYSTEM.

The AGS warm snake 3-D OPERA field map used here, table55.map, can be found here: https://sourceforge.net/p/zgoubi/code/HEAD/tree/trunk/exemples/AGS/snakeFieldMaps/Wsnk3D/.

```
Centering 5 helical orbits in the AGS warm helical snake 3-D OPERA map.
                      This data list may be copy-pasted and run, as is.
 'OBJET'
7.2051782956D3
                    ! Reference rigidity of the problem
2
1 1
                    ! A single particle. Initial coordinates :
-2.2 0. 0. 0. 0. 1. 'o'
                                     ! Yo, To, Zo, Po, So, p/po
1
 'PARTICUL'
                    ! proton data are necessary for spin tracking
                                                                                Zgoubi Zpo
29/08/**
938.27203 1.602176487E-19 1.7928474 0 0
                                             ! M, Q, G factor
'SPNTRK'
                                                                             0.01
4.1
                    ! Initial spin is positionned vertical
                                                                             0.01
0. 0. 1.
                                                                             0.00
 'FAISCEAU'
 'SPNPRT'
                                                                              0.0
 ' TOSCA
0 20
                                                                             -.01
1.e1
      100. 100. 100.
HEADER_0 wsnake
801 29 29 12.1
                     ! The map is a 801x29x29 node 3-D mesh.
                                                                                           .01
                                                                                                            0.01
table55.tab
                       ! AGS warm snake 3-D OPERA field map.
                                                                          This figure shows how, using REBELOTE, the
0 0 0 0
2
                                                                           helical trajectories at five different momenta
.1
                                                                          are moved by the FIT procedure, one after the
2 0. .0 0. 0.
                                                                          other, from initial off-centered position to final
 'FAISCEAU'
                                                                              centering on the snake axis (at Y=Z=0).
 'FIT'
                    ! Two variables. Save FIT variables (in zgoubi.FITVALS.out).
2
   save
  30 0 [-3,3]
1
                           Vary initial coordinate Y_0 (horiz. position)
 31 0 [-3,3]
                         ! Vary initial coordinate T_0 (horiz. angle)
1
     1E-2
                     ! Three constraints (penalty 2E-3 requested)
3
3.1 1 2 6 0. 1. 0
                        ! Y_0=Y after at exit of the magnet
3.1 1 3 6 0. 1. 0
                         ! T 0=T after at exit of the magnet
7.3 1 2 6 0. 1. 0
                         ! Y min+Y max=0 inside the OPERA field map
 'SPNPRT' PRINT
                     ! Stack spin data (in zgoubi.SPNPRT.Out).
'SYSTEM'
                    ! Save zgoubi.FITVALS.out data following from successive REBELOTE.
1
cat zgoubi.FITVALS.out >> zgoubi.FITVALS.out_cat
 'REBELOTE'
                    ! Will loop on re-doing the FIT for 4 additional particle rigidities
4 0.1 0 1
                    ! List of 4 successive values of D in OBJET follows
1
OBJET 35 1.3872739973 2.1368296674 4.8261190694 11.015241321
 'SYSTEM'
                    ! Save a copy of zgoubi.FITVALS.out_cat and of zgoubi.SPNPRT.Out_cat
2
\cp zgoubi.FITVALS.out_cat zgoubi.FITVALS.out_cat_copy
\cp zgoubi.SPNPRT.Out
                           zgoubi.SPNPRT.Out_copy
 'END'
```

Type of		Parame	ters definiı	ng the constraints (see also footnotes)			Recommended [MC]OBJET
constraint	IC	I	J	Constraint (all are defined and managed in ff.f)	Addition NP	nal parameter(s) Param. values, $pr_1 - pr_{NP}$	(not an exclusive list) ; comments
Transported σ -matrix $(\sigma(s) = T\sigma(0)\tilde{T})$	0	1-6	1-6	σ_{IJ} ($\sigma_{11} = \beta_Y, \sigma_{21, 12} = \alpha_Y$, etc.)			OBJET[KOBJ=5.1]
Periodic σ -matrix ($\sigma = I \cos \mu + J \sin \mu$), tunes ($N = 1 - 9$ for MATRIX block 1-9)	$\begin{array}{c} 0.\mathrm{N} \\ (N \leq 9) \end{array}$	1-6 7 8 9 10	$1-6 \ [0,1] \ [0,1] \ [-1,1] \ [-1,1]$	$\sigma_{IJ} (\sigma_{11} = \cos \mu_Y + \alpha_Y \sin \mu_Y, \text{etc.}) \\ \begin{array}{c} \mu_Y / 2\pi \\ \mu_Z / 2\pi \\ \cos(\mu_Y) \\ \cos(\mu_Z) \end{array}$			OBJET[KOBJ=5] if N = 1, OBJET[KOBJ=5.N] if $N \ge 2$.
First order transport coeffs. & determinants.	1	$ \begin{array}{r} 1-6 \\ 7 \\ 8 \end{array} $	1-6 j j	Transport coeff. R_{IJ} $j \neq 8$: YY-determinant ; j=8: YZ-det. $j \neq 7$: ZZ-determinant ; j=7: ZY-det.			OBJET[KOBJ=5]
Chromas.	1.1	7 8	7 8	$dQ_Y / dp/p \ dQ_Z / dp/p$			OBJET[KOBJ=5.2] or KOBJ=5.3
Second order transport coeffs.	2	1 - 6	11-66	Transport coeff. $T_{I,j,k}$ (j = [J/10], k = J - 10[J/10])			OBJET[KOBJ=6]
Trajectory coordinates	3	1 - IMAX - 1	$1 - 7 \\ 1 - 7$	$F(J,I) \\ < F(J,i) >_{i=I1,I2}$	[2]	$[I_1, I_2]$	$[MC]OBJET$ none $[1 \le I_1 \le I_2 \le IMAX]$
(I = particle number; J=1-7 for D,Y,T,Z,P,S,time)	3.1	-2 -3 -4 1-IMAX	$egin{array}{c} 1-7 \ 1-7 \ 1-7 \ 1-7 \ 1-7 \ 1-7 \end{array}$	$Sup(F(J, i))_{i=1,IMAX} \\ Dist [F(J, I)_{i=I1,I2}] \\ Dist [PU_i, i = 1, N] \\ F(J, I) - FO(J, I) $	3 2	$I_1, I_2, \Delta I$ NOEL _A , NOEL _B	$1 \le I_1 \le I_2 \le IMAX$ PU range
	3.2 3.4 3.5	1-IMAX 1-IMAX 1-IMAX	$1 - 7 \\ 1 - 7 \\ 1 - 7$	$egin{array}{c} F(J,I)+FO(J,I) \ F(J,I)-F(J,K) \ (F(J,I)-F(J,K))/F(J,K) \end{array}$	1 1	K K	$K \le IMAX$ $K \le IMAX$
Ellipse parameters	4	1 - 6	1-6	$\sigma_{IJ} (\sigma_{11} = \beta_Y, \\ \sigma_{12} = \sigma_{21} = \alpha_Y, \text{ etc.})$			OBJET[KOBJ=8] ; MCOBJET[KOBJ=3]
Number of particles	5	-1 1 - 3 4 - 6	$ \leq 1 \\ \leq 1 \\ \leq 1 $	$N_{survived} / IMAX$ $N_{in \ \epsilon_{Y,Z,X}} / N_{survived}$ $N_{in \ best \ \epsilon_{Y,Z,X,rms}} / N_{survived}$	1	$\epsilon_{Y,Z,X}/\pi$	OBJET MCOBJET MCOBJET
Coordinates & fields, across optical elements $(J=1, 2, 3 \text{ for} B_{X, Y, Z})$	7.1 7.2 7.3 7.6 7.7 7.8 7.9 7.10	1 – IMAX 1 – IMAX	$ \begin{array}{r} 1-7\\1-7\\1-7\\1-3\\1-3\\1-3\\1-3\\1-7\end{array} $	min. (param.=1) or max. (2) of $F(J, I)$ max $(F(J, I))$ - min $F(J, I)$) min $F(J, I)$) + max $(F(J, I))$ min. or max. value of B_J max (B_J) - min (B_J) min (B_J) + max (B_J) $\int B_J ds$ to be documented	1 [or 3] 0 [or 2] id. 1 [or 3] 0 [or 2] id. id. id. id.	1 or 2 [, X1, X2] [X1, X2] id. 1 or 2 [, X1, X2] [X1, X2] id. id. id.	[MC]OBJET
Spin	10 10.1 10.2 10.3 10.4 10.5	1–IMAX 1–IMAX 1–IDMAX 1–IDMAX 1–IDMAX 1–IMAX	1 - 4 1 - 3 any 1 - 3 [0, 1] 1 - 3	$S_{X,Y,Z}(I), \vec{S}(I) $ $ S_{X,Y,Z}(I) - SO_{X,Y,Z}(I) $ spin precession angle $([-\pi,\pi])$ X, Y or Z component of precession axis spin tune $\langle S_{X,Y,Z} \rangle_{N=1,I \text{ particles}}$	0 [or 1]	[1]	SPNTRK+ [MC]OBJET OBJET[KOBJ=2] OBJET[KOBJ=1,2] OBJET[KOBJ=2] OBJET[KOBJ=2]

 \diamond IMAX: total number of particles tracked.

 \diamond *F*(*J*,*I*) : particle coordinate array ; J: coordinate (1-7 for respectively D, Y, T, Z, P, S, time, resp. units: none, cm, mrad, cm, mrad, cm, μ s) ; I: particle number.

 \diamond FO(J,I) : initial particle coordinates.

 $\diamond S(J,I)$: spin coordinate array ; J: coordinate (1, 2, 3 for respectively X, Y, Z) ; I: particle number.

 \diamond SO(J,I) : initial spin coordinates.

♦ Constraints 7.1 - 7.9: X1 and X2, optional, define the longitudinal coordinate interval inside the optical element, over which it applies.

 \diamond Constraint 10.3: If NP=1 and pr_{NP} =1, then the absolute value of the X, Y or Z component is accounted for.

Combining FIT and REBELOTE, Example 2:

The goal in this problem is to produce the outer and inner coil current values of RHIC 9 o'clock snake, for a series of values of the snake axis orientation and spin rotation by the snake.

Down the optical sequence, the execution pointer meets *FIT2*; when the latter is completed, the execution pointer continues to *REBELOTE*. The latter will re-launch the problem NRBLT=5 times, but prior to re-launching, it will change the values of 3 of the constraints in *FIT*.

This results in the graph displayed on the right.

The files and scripts in this example, incluing the two snake OPERA field maps, can be found in Zgoubi repository:

https://sourceforge.net/p/zgoubi/code/HEAD/tree/trunk/exemples/RHIC/spinTransparency/spinTransparencyExperiment/scanSnake_MuPhi/

```
Snake 1. 9 o'clock snake, in Yellow going clockwise.
 79.366778931425273 * 1d3
     1 1 1 1 1
                                                                                       ! 3 times the same particle, to compute a spin matrix.
                                   0.0 0.00 0.000000E+00
0. 0. 1.
 0.0 0.0 0.0
0. 0. -1.3206397 0.
'PARTICUL'
                        0.0
PROTON
'SPNTRK'
1.000 0.000 0.0000000E+00
                                                                                 ! Respective spins of the 3 particles, in that order, for
! spin matrix computaion by SPNPRT[MATRIX].
0.000
             1.000
                          0.0000000E+00
0.000
              0.000
                          1.00000000E+00
 'SCALING'
TOSCA
              snklLowB
184.47838 ! low-field coils current (A)
                                                                                                                                                                                    250
TOSCA snklHighB
                                                                                                                                                                                                                                                                    ų,
                                                                                                                                                                                                                                                                         •
                                                                                                                                                                                                                                                                                  0.9
198.70954 ! high-field coils current (A)
                                                                                                                                                                                                                                                                   alty
                                                                                                                                                                                                                                                                                  0.8
                                                                                                                                                                               lout, I<sub>h</sub> [A]
'TOSCA'
                            snklLowB
                                                                                                                                                                                                                                                                                  0.7
150
                                                                                                                                                                                                                                                                                  0.6
                                                                                                                                                                               Z<sub>co</sub> [10<sup>-4</sup>m],
                                                                                                                                                                                                                                                                                  0.5
                                                                    ! = 1/1.3360e4
       del3a2a-x-4_4_y-4_4_z-180_180-integral.table
                                                                                                                                                                                    100
                                                                                                                                                                                                                                                                                  0.4
    0 0 0
                                                                                                                                                                                ¢ [deg],
                                                                                                                                                                                                                                                                                  0.3
 .3
                                                                                                                                                                                      50
 .3
2 0.000 0.000 0.00000000E+00
'DRIFT' 2.162m_CltoC2
-98.800000
                                                                                                                                                                                                                                                                                  0.2
 'DRIFT'
                                                                                                                                                                                                                                                                                  0.1
'TOSCA'
                           snklHighB
'TOSCA' snklHighB

0 0 !.plt

+1. 1.000 1.000 1.0000000000000

HEADER_8 RHIC_helix

361 81 81 15.1 0.246305418719e-4 != 1/4.060e4

b_model3a2a322a-x-4_4_y-4_4_z-180_180-integral.table
                                                                                                                                                                                                                                                                                  0
                                                                                                                                                                                                     This figure is obtained from
0 0 0 0
                                                                                                                                                                                zgoubi.FITVALS.out, using the gnuplot script
  . 3
                                                                                                                                                                                                                             below:
-37.6
'DRIFT'
                 2.162m_C2toC3
-37.6
                                                                                                                                                                              set title "I {out} and I {in} current in 9 o'clock snake"
'TOSCA'
                           snklHighB
set xtics; set ytics nomirror; set y2tics
                                                                                                                                                                              set key maxrow 1; set grid

        system "grep '4
        2
        4 ' zgoubi.FITVALS.out | cat > temp1"

        system "grep '4
        3
        8 ' zgoubi.FITVALS.out | cat > temp2"

        system "grep '1t reached penalty value' zgoubi.FITVALS.out | cat > temp3"
        system "grep '10
        0
        19 ' zgoubi.FITVALS.out | cat > temp4"

        system "grep '10
        1
        2
        19 ' zgoubi.FITVALS.out | cat > temp5"

0 0 0 0
 .3
 2 0.000 0.000 0.00
'DRIFT' 2.162m_C3toC4
-98.800000
                                  r2d = 180. / (4.*atan(1.))
-98.800000

'TOSCA' snklLowB

0 0 !.plt

+1. 1.000 1.000 1.00000000E+00

HEADER_8 RHIC_helix

361 81 15.1 0.748502994012e-4 != 1/1.3

b_model3a2a-x-4_4y-4_4_z-180_180-integral.table
                                                                                                                                                                              plot '
                                                                                                                                                                                plot \
"temp1" u 0:($6) w lp pt 4 tit "I_{out}",\
"temp2" u 0:($6) w lp pt 5 tit "I_{in}", \
"temp3" u 0:($5) axes xly2 w lp pt 6 tit "penalty",\
"temp3" u 0:($7 *r20 w lp pt 7 tit "phi",\
"temp5" u 0:(-asin($7) *r20 * 10.) w lp pt 8 tit "-10* mu"
                                                                    ! = 1/1.3360e4
.3
       0.000 0.000 0.0000000E+00
 DRIFT'
16.4
'FIT2'
                           ! Save FIT outcomes (variable values, penalty, ...) to zgoubi.FITVALS.out, for plotting.
! Z_0, vertical position of reference orbit at OBJET.
! Low B coil current.
! High B coil current.
   save
42 0 1.5
4 0 1.5
    8 0 1.5
     1e-8
! Vertically center traj #1 in 3rd helix;
    ! D-group 1. Spin rotation angle = 180;
    ! X component of rotation axis = cos(-lodeg);
    ! Y component of rotation axis = sin(-lodeg);
'FAISCEAU
'SPNPRT' MATRIX PRINT
                                                               ! Cumulate spin matrix and data in zgoubi.SPNPRT.Out, at each pass.
'REBELOTE

        J
        J

        FIT2
        64
        3.0368728
        2.9845130
        2.9321531
        2.8797932
        2.8797932

        FIT2
        74
        0.9945218
        0.9975640
        0.9993908
        1.
        1.

        FIT2
        84
        -0.1045284
        -0.0697564
        -0.0348994
        0.
        0.

                                                                                                                                                                  ! mu (deg),
                                                                                                                                                                  ! cos(phi),
! sin(phi).
'END'
```

• Example : FIT[2] options

In this example, *FIT*[2] options, "nofinal", "save FileName", "penalty" and "ITER", are all specified explicitely. *FIT*[2] finds the reference closed orbit; the outcomes of that FIT are saved in zgoubiFIT.result; the final run normally following FIT (with variables updated to their matched values) is skipped; penalty and maximum number of calls to the function are explicit (default values would be, respectively, 1e-10 and 999). When FIT is done, the execution pointer moves on to *FAISCEAU*, etc.

```
An example with some explicit FIT options 'GETFITVAL'
zgoubi.FITVALS.In
 'MCOBJET'
79.e3
                                                                                          ! reference rigidity.
3.1
2 2 2 2 1 1
0. 0. 0. 0. 0.
                 4.61943880E-01
2.703371 1.859656 1.48563786487e-9
-2.592712 2.421706 1.48563786487e-9
                                            a
                                            9
0.1.0.9
12345 23456 34567
'SPNTRK'
                                                                          ! It seems spins are being tracked!
4.1
0. 0. 1.
'PICKUPS'
2
'INCLUDE'
                                                                ! Include some periodic structure concerned.
AGS_Booster.inc[ring_S:ring_E]
                                                  ! AGS_Booster.inc file includes the optical sequence, it
                                                              ! can be a standalone zgoubi input data file.
'FTT2'
4 save zgoubiFIT.result nofinal     ! Save variables in zgoubiFIT.result when FIT done. No final run.
2 40 0 [-1.e-2,1.e-2]
                                                        ! The four variables are Yo, To, Zo, Po in MCOBJET.
2 41 0 [-1.e-2,1.e-2]
2 42 0 [-1.e-2,1.e-2]
2 43 0 [-1.e-2,1.e-2]
4 1e-15 90 ! Pena
3.1 1 2 7500 0. 1. 0
                ! Penalty=1e-15 (default would be 1e-10). Maximum allowed calls to the function is 90.
                                                         ! The four constraints are : initial Y, T, Z, P of
! particle #1 equal to its final Y, T, Z, P.
3.1 1 3 7500 0. 1. 0
3.1 1 4 7500 0. 1. 0
3.1 1 5 7500 0. 1. 0
'FAISCEAU'
                                                        ! This will log particle coordinates in zgoubi.res.
'SPNPRT'
                            ! This will log spin vector data - thus on the closed orbit - in zgoubi.res.
'END'
```

FOCALE	Particle coordinates and horizontal beam size at distance XL		
XL	Distance from the location of the keyword	cm	E
FOCALEZ	Particle coordinates and vertical beam size at distance XL		
XL	Distance from the location of the keyword	cm	Е

GASCAT	Gas scattering		
KGA	Off/On switch	0, 1	I
AI, DEN	Atomic number ; density		2*E

GETFITVAL Get values of *variables* as saved from former FIT[2] run

FNAMEName of storage file. Zgoubi will proceed silently if
FNAME='none' or FNAME='NONE', or if the file is not found.

А

• Example : GETFITVAL

Expected content of file FNAME is the result of a prior FIT[2], of the form:

SI	ATUS	OF V	ARI	ABLES	(Iterati	ion #	95)						
I	MNT	VAR	PAR	AM MI	NIMUM	INITIAL	FINAL	MAXIMUM	STEP	NAME		LBL1	LBL2
	145	1	4	-3	.000E+03	762.	761.9484791	3.000E+03	1.254E	-05 MULT	IPOL	HKIC	DHCB02
	182	2	4	-1	.000E+03	-231.	-230.9846875	1.000E+03	4.182E	-06 MULT	IPOL	HKIC	DHCB08
	146	3	4	-1	.000E+03	-320.	-319.8554171	1.000E+03	4.182E	-06 MULT	IPOL	VKIC	DVCB02
	183	4	4	-1	.000E+03	528.	527.7249064	1.000E+03	4.182E	-06 MULT	IPOL	VKIC	DVCB08
	615	5	4	-3	.000E+03	308.	307.6860565	3.000E+03	1.254E	-05 MULT	IPOL	HKIC	DHCF02
	651	6	4	-1	.000E+03	-114.	-113.8490362	1.000E+03	4.182E	-06 MULT	IPOL	HKIC	DHCF08
	616	7	4	-1	.000E+03	-78.9	-78.88730937	1.000E+03	4.182E	-06 MULT	IPOL	VKIC	DVCF02
	652	8	4	-1	.000E+03	212.	211.8789183	1.000E+03	4.182E	-06 MULT	IPOL	VKIC	DVCF08
#	STATU	JS OF	CO	NSTRAI	NTS								
#	TYPE	I	J	LMNT#	DESI	IRED	WEIGHT	REACHED		KI2	*	Parame	ter(s)
#	3	1	2	127	0.00000	000E+00	1.0000E+00	1.0068088E	-08 6	.0335E-0	1 *	0:	
#	3	1	3	127	0.0000	000E+00	1.0000E+00	7.0101405E	-09 2	.9250E-0	1 *	0:	
#	3	1	4	127	0.00000	000E+00	1.0000E+00	2.9184383E	-10 5	.0696E-04	4 *	0:	
#	3	1	5	127	0.00000	000E+00	1.0000E+00	3.1142381E	-10 5	.7727E-0	4 *	0:	
#	3	1	2	436	0.00000	000E+00	1.0000E+00	3.8438378E	-09 8	.7944E-02	2 *	0:	
#	3	1	3	436	0.0000	000E+00	1.0000E+00	1.5773011E	-09 1	.4808E-02	2 *	0:	
#	3	1	4	436	0.00000	000E+00	1.0000E+00	2.2081272E	-10 2	.9022E-0	4 *	0:	
#	3	1	5	436	0.0000	000E+00	1.0000E+00	5.7930552E	-11 1	.9975E-0	5 *	0:	
#	Fur	nctio	n (called	1859 t	imes							
#	Xi2 =	=	1.6	8006E-	16 Busy	/···							

HALBACH

Halbach style permanent magnet

UNDER DEVELOPMENT

А

HELIX	Helical dipole	(page 123 in PART A)		
IL	$IL = 1, 2[\times 10^n], 7$: print coordinates, fields, etc., step-by-step,			
VI DIT B. d	in zgoubi.res (1), zgoubi.plt (2), zgoubi.impdev.out (7).	cm cm kG rad	/*F	
KIRD, resol	Field and derivatives analytical: KIRD=0, resol =2 (default);	-, -	2*I	
XPAS	Field derivatives from mesh: KIRD=3, mesh size is XPAS/Resol Integration step	cm	E	
KPOS, XCE, YCE, ALE	<i>KPOS</i> =1 : element aligned, 2 : misaligned ; shifts, tilt.	1-2, 2*cm, rad	I, 3*E	

GOTO	Branching statement				
	Under development				
OPTION	Can be 'PASS#', 'GOBACK', 'NEXT' (skips the next element), it can also be an existing <i>LABEL1</i> (will send execution pointer to closest following occurence of <i>LABEL1</i>).	String	А		
If OPTION = PASS#	One additional line needed :				
LABEL1,, LABELN	List of labels (expected is label #1 that follows a keyword) to go to, pass after pass (passes are incremented, from 1 to N, by <i>REBELOTE</i>	N strings for instance).	N*A20		

HISTO	1-D histogram	(195 in Part A)	
J, X _{min} , X _{max} , NBK, NH [,PRINT]	J = coordinate to be histogrammed, as follows: • current coordinates : 1(D), 2(Y), 3(T), 4(Z), 5(P), 6(S), • initial coordinates : $11(D_0), 12(Y_0), 13(T_0), 14(Z_0), 15(P_0), 16(S_0),$ • spin : $21(S_X), 22(S_Y), 23(S_Z), 24(S);$ $X_{\min}, X_{\max} = \text{limits of the histogram, in units}$ of the coordinate of concern ; <i>NBK</i> = number of bins ; <i>NH</i> = number of the histogram (for independence of histograms of the same coordinate); <i>PRINT</i> , optional, will cause output to zgoubi.HISTO.out.	1-24, 2* current units, ≤ 120, 1-5 [,A]	I, 2*E, 2*I
NBL, KAR, NORM, TYP	Number of lines (= vertical amplitude); alphanumeric character; normalization if <i>NORM</i> = 1, otherwise <i>NORM</i> = 0; <i>TYP</i> = 'P': primary particles are histogrammed, or 'S': secondary, or Q: all particles - for use with <i>MCDESINT</i>	normally 10-40, char., 1-2, P-S-Q	I, A1, I, A1

• Example : HISTO

The following will cause an histogram of the relative rigidity (D), case of the sole P-rimary particles (case of in-flight decay). 'PRINT' causes output to zgoubi.HISTO.out (can be used for gnuplot-ing, for instance).

Keywords and input data formatting

IMAGE Localization and size of horizontal waist

IMAGES	Localization and size of horizontal waists

For each momentum group, as classified by means of *OBJET*, *KOBJ* = 1, 2 or 4

IMAGESZ Localization and size of vertical waists

For each momentum group, as classified by means of *OBJET*, *KOBJ* = 1, 2 or 4

IMAGEZ	Localization and	l size of	vertical	waist

(page 168 in PART A)

NBF	Number of files to be included	1	Ι	
	(1 at the moment - under development).			

NBF following lines (one file name per line) :

FNAME[Name of input zgoubi.dat-style file to be included. LBL_1A, _2A :	A80 [,[A20], [A20]]
[LBL_1A] [, [LBL_2A]]:	entrance branching tags, LBL_1B , $_2B$: exit branching tags.	
[LBL_1B] [, [LBL_2B]]]		
	(An INCLUDEd file must terminate with "'END' ".)	

• Example : INCLUDE

In this example of an energy-recovery electron recirculator [83], the linac, spreader and combiner data lists are given in separate files, declared as *INCLUDEs*. Using *INCLUDE* has a series of merits :

- it shortens the parent input data file, so making the optical structure more apparent,

- it allows picking optical spreader, combiner and ring sequences from files that may actually be set to - for instance - compute optical parameters; in that case, LBL_A and LBL_B are used for this targetted picking: they define the ends of the sequence to be *INCLUDE*'d, ignoring the upper and lower parts in the *INCLUDE*'d file (which may be specific, for instance, to MATRIX computations).

Note the following : (i) juggling between linac, spreaders, combiners and recirculating ring, is handled using *GOTO* statement, (ii) the use of *REBELOTE* in this ERL context is discussed in an example page 315.

Cornell CBETA prototype (of an eRHIC) FFAG arc ERL 19.9411300960454126 ! T.m E tot=6MeV 5.01 .01 .01 .01 .01 .01 0. 0. 0. 0. 0. 1. -0.8475 1.5739 -0.8481 1.59 0. 1. 7.49E-03 4.12E-03 0. 0. 0.51099892 1.60217653e-19 1.15965218076e-3 0.0 0.0 'ERRORS' 0 1 123466 dB(kG) MULTIPOL{} 1 BP A U 0.d0 0.0 9999 'SCALING' MULTIPOL 1. 1. 1 9999 MULTIPOL SA1.1 SB1.1 1. 1. 1 9999 'OPTIONS' WRITE ON !///// Racetrack sequence starts here, at linac entrance Linac ! Linac 'INCLUDE' ./LA/LA_obj5.inc[LA.MAR.BEG\1:LA.MAR.END\1] ! Goto splitter line 'GOTO' PASS# SA1 SA2 SA3 SA4 SA3 SA2 SA1 'MARKER' RT_SA ! Goto FFAG return loop : arc+(DS+straight+DS)+arc GOTO 'GOIO' PASS# FA FA FA FA FA FA FA FA FA 'MARKER' RT_FA 'GOTO' PASS# * * * * * * * * * 'MARKER' RT_ 'GOTO' 'GOIO' PASS# FB FB FB FB FB FB FB FB FB 'MARKER' RT_FB ! Goto combiner line 'GOTO' 'GOIO' PASS# SB1 SB2 SB3 SB4 SB3 SB2 SB1 'MARKER' RT_SB 'MATRIX' 1 0 MARKER' rebelote REBELOTE' ! send zgoubi execution pointer back to 0.1 99 ! the top (and linac entrance), 7 times 'MARKER' 7 'MARKER' stop

! Splitter lines 'MARKER' SAl 'INCLUDE' 1 ./SA/SA1.inc[LA.MATCH1:S1.MERGE.MAR.END\1] 'GOTO GOBACK 'MARKER' SA2 'INCLUDE' ./SA/SA2.inc[LA.DEMER.MAR.BEG\2:S1.MERGE.MAR.END\2] ' GOTO' GOBACK 'MARKER' SA3 'INCLUDE' ./SA/SA3.inc[SA3#S:SA3#E] 'GOTO' GOBACK 'MARKER' SA4 ./SA/SA4.inc[SA4#S:SA4#E] ' GOTO' GOBACK 'MARKER' FA 'INCLUDE' ./FA/FA.inc[FA#S:FA#E] ' GOTO' GOBACK 'MARKER' X 'INCLUDE' ./X./X.inc[X#S:X#E] ' GOTO' GOBACK 'MARKER' FB 'INCLUDE' ./FB/FB.inc[FB#S:FB#E] GOBACK ! Combiner lines 'MARKER' SB1 'INCLUDE' 1 1 /SB/SB1.inc[SB1#S:SB1#E] 'GOTO' GOBACK 'MARKER' SB2 'INCLUDE' ./SB/SB2.inc[SB2#S:SB2#E] ' GOTO GOBACK 'MARKER' SB3 'INCLUDE' ./SB/SB3.inc[SB3#S:SB3#E] 'GOTO' GOBACK 'MARKER' SB4 'INCLUDE' ./SB/SB4.inc[SB4#S:SB4#E] GOTO GOBACK 'MATRIX' 1 0 'END'

MAP2D	2-D Cartesian uniform mesh field map - arbitrary magnetic field		
IC, IL	IC = 1, 2: print the field map $IL = 1, 2[\times 10^n], 7$: print coordinates, fields, etc., step-by-step, in zgoubi.res (1), zgoubi.plt (2), zgoubi.impdev.out (7).	0-2; 0-2[×10 ⁿ], 7	2*I
BNORM, XN, YN	Field and X-,Y-coordinate unit conversion coeffs. Convert values as read from map file, to kG and cm units.	3*UnitConv.	3*E
TITL	Title. Start with "FLIP" to get field map X-flipped.		A80
IX, JY	Number of longitudinal and horizontal-transverse nodes of the mesh (the Z elevation is arbitrary)	$\leq 400, \leq 200$	2*I
FNAME ¹	File name		A80
ID, A, B, C [, A', B', C', B'', etc., if $ID \ge 2$]	Integration boundary. Ineffective when $ID = 0$. $ID = -1$, 1 or ≥ 2 : as for <i>CARTEMES</i>	≥ -1, 2*no dim, cm [,2*no dim, cm, etc.]	I,3*E [,3*E,etc.]
IORDRE	Degree of polynomial interpolation, 2nd or 4th order.	2, 4	Ι
XPAS	Integration step	cm	Е
KPOS, XCE, YCE, ALE	KPOS=1 : element aligned, 2 : misaligned ; shifts, tilt.	1-2, 2*cm, rad	I, 3*E

¹ *FNAME* (*e.g.*, magnet.map) contains the field map data.

These must be formatted according to the following FORTRAN read sequence (normally compatible with TOSCA code OUTPUTS - details and possible updates are to be found in the source file ' fmapw.f'):

 $\begin{array}{l} \text{OPEN} \text{ (UNIT = NL, FILE = FNAME, STATUS = 'OLD')} \\ \text{DO 1 J = 1, JY} \\ \text{DO 1 I = 1, IX} \\ \text{IF} (BINARY) \text{ THEN} \\ \text{READ(NL) Y(J), Z(1), X(I), BY(I,J), BZ(I,J), BX(I,J)} \\ \text{ELSE} \\ \text{READ(NL,100) Y(J), Z(1), X(I), BY(I,J), BZ(I,J), BX(I,J)} \\ 100 \\ \text{FORMAT} (1X, 6E11.4) \\ \text{ENDIF} \\ 1 \\ \text{CONTINUE} \end{array}$

where X(I), Y(J) are the longitudinal, horizontal coordinates in the at nodes (I, J) of the mesh, Z(1) is the vertical elevation of the map, and BX, BY, BZ are the components of the field.

For binary files, FNAME must begin with 'B_' or 'b_'; a logical flag 'Binary' will then automatically be set to '.TRUE.'
МАР2Д-Е	2-D Cartesian uniform mesh field map - arbitrary electric field		
IC, IL	IC = 1, 2: print the field map $IL = 1, 2[\times 10^n], 7$: print coordinates, fields, etc., step-by-step, in zgoubi.res (1), zgoubi.plt (2), zgoubi.impdev.out (7).	$0-2; 0-2[\times 10^n], 7$	2*I
ENORM, X-, Y-NORM	Field and X-,Y-coordinate unit conversion coeffs. Convert values as read from map file, to MV/cm and cm units.	3*UnitConv.	3*E
TITL	Title. Start with "FLIP" to get field map X-flipped.		A80
IX, JY	Number of longitudinal and horizontal-transverse nodes of the mesh (the Z elevation is arbitrary)	$\leq 400, \leq 200$	2*I
FNAME ¹	File name		A80
ID, A, B, C [, A', B', C', B", etc., if $ID \ge 2$]	Integration boundary. Ineffective when $ID = 0$. $ID = -1$, 1 or ≥ 2 : as for <i>CARTEMES</i>	≥ -1, 2*no dim, cm [,2*no dim, cm, etc.]	I,3*E [,3*E,etc.]
IORDRE	Degree of polynomial interpolation, 2nd or 4th order.	2,4	Ι
XPAS	Integration step	cm	Е
KPOS, XCE, YCE, ALE	KPOS=1 : element aligned, 2 : misaligned ; shifts, tilt.	1-2, 2*cm, rad	I, 3*E

¹ *FNAME* (*e.g.*, "mirror.map") contains the field map data. These must be formatted according to the following *FORTRAN* read sequence - details and possible updates are to be found in the source file ' fmapw.f':

where X(I), Y(J) are the longitudinal, horizontal coordinates in the at nodes (I, J) of the mesh, Z(1) is the vertical elevation of the map, and EX, EY, EZ are the components of the field.

For binary files, FNAME must begin with 'B_' or 'b_'; a logical flag 'Binary' will then automatically be set to '.TRUE.'

MARKER

Marker

Just a marker. No data '.plt' as a second *LABEL* will cause storage of current coordinates into zgoubi.plt

MATRIX

Calculation of transfer coefficients, periodic parameters

(page 197 in PART A)

IORD, IFOC	Options :	0-2, 0-1 or > 10	2*I [.A]				
[, PRINT] [, coupled]	IORD = 0: Same effect as FAISCEAU	,	L/]				
	<i>IORD</i> = 1, using <i>OBJET</i> , <i>KOBJ</i> = 5[.N] : 1st order transport param	eters,					
	- if $KOBJ = 5.1$: beam matrix, phase advance, otherwise						
	- 1st order data (cf. IFOC value) for N different cases of optical reference.						
	IORD = 2, using OBJET, KOBJ = 6 : 1st order transport matrix $[R_{ij}]$,						
	2nd order array $[T_{ijk}]$ and a few higher order transport coefficients;						
	some periodic parameters in addition if $IFOC > 10$;						
	IORD = 3, using OBJET, KOBJ = 6.1 : 1st order transport matrix $[R_{ij}]$,						
	2nd and 3rd order arrays $[T_{ijk}], [T_{ijkl}].$						
	IFOC = 0: matrix at actual location ¹ ;						
	IFOC = 1: matrix at the closest first order horizontal focus ¹ ;						
	IFOC = 10 + NPER: same as $IFOC = 0$, and also calculates 1 or N sets						
	(case respectively of KOBJ = 5 or KOBJ = 5.N, $2 \le N \le 99$) of Twiss						
	parameters, tune numbers, etc., assuming zgoubi.dat file describes						
	one period of a NPER-period structure ¹ .						
	Occurence of "PRINT" will cause printout to zgoubi.MATRIX.out	file.					

Occurence of "coupled", in the periodic case (IFOC = 10 + NPER, above), will cause use of coupled formalism.

¹ The reference in computing transport coefficients and other periodic parameters is particle # 1 of the ray-traced set. If N 13-particle sets are ray-traced in order to get (in a single zgoubi run) transport coefficients for N different cases of reference orbit (using *OBJET*, *KOBJ* = 5.N, $2 \le N \le 99$), the reference particle for each 13-particle set is respectively particle #1, 12, 23, ... 1+(N-1)×11.

MCDESINT ¹	Monte-Carlo simulation of in-flight decay $M1 \rightarrow M2$ + $M3$	(page 169 in PART)	(page 169 in PART A)		
M2, M3, τ2 ² [, back] [, INFO] ³	Mass of the two decay products (M1 is defined using <i>PARTICUL</i>); COM lifetime of M2 [; allow backward: 1/0 default is 0] [; Print out info]	2*MeV/c ² , s [,0-1] [, INFO]	3*E [, E] [, A4]		
<i>I</i> 1, <i>I</i> 2, <i>I</i> 3	Seeds for random number generators	$3^* \simeq 10^6$	3*I		



Particle 1 decays into 2 and 3 ; **zgoubi** then calculates trajectory of 2, while 3 is discarded. θ and ϕ are the scattering angles of particle 2 relative to the direction of the incoming particle 1. They transform to T_2 and P_2 in Zgoubi frame.

¹ *MCDESINT* must be preceded by *PARTICUL*, for the definition of the mass and lifetime of the incoming particle M1. ² τ^2 can be left blank, in which case the lifetime of particle 2 is set to zero (it decays immediately, which from a practical point of view means that it is not tracked).

³ Presence of 'INFO' will cause more info on decay kinematics parameters to be printed zgoubi.res at each decay.

MCOBJET	Monte-Carlo generation of a 6-D object		
BORO [* fac]	Reference rigidity = <i>BORO</i> [* <i>fac</i>], with <i>fac</i> an arbitrary numerical value.	kG.cm [,-]	E [,E]
КОВЈ	Type of support of the random distribution <i>KOBJ</i> = 1 : window <i>KOBJ</i> = 2 : grid <i>KOBJ</i> = 3 : phase-space ellipses	1-3	Ι
IMAX	Number of particles to be generated	$\leq 10^4$	
$KY, KT, KZ, KP, KX, KD^{1}$	Type of probability density	6*(1-3)	6*I
$Y_0, T_0, Z_0, P_0, X_0, D_0$	Mean value of coordinates ($D_0 = B\rho/BORO$)	m, rad, m, rad, m, no dim	6*E
If KOBJ = 1	In a window		
$ \begin{aligned} \delta Y, \delta T, \delta Z, \delta P, \\ \delta X, \delta D \end{aligned} $	Distribution widths, depending on KY , KT etc. ¹	m, rad, m, rad, m, no dim	6*E
$N_{\delta Y}, N_{\delta T}, N_{\delta Z}, N_{\delta P}, N_{\delta X}, N_{\delta D}$	Sorting cut-offs (used only for Gaussian density)	units of σ_Y , σ_T , etc.	6*E
N_0, C_0, C_1, C_2, C_3	Parameters involved in calculation of P(D)	no dim.	5*E
<i>IR</i> 1, <i>IR</i> 2, <i>IR</i> 3	Random sequence seeds	$3^* \simeq 10^6$	3*I
If KOBJ = 2	On a grid		
IY, IT, IZ, IP, IX, ID	Number of bars of the grid		6*I
PY, PT, PZ, PP, PX, PD	Distances between bars	m, rad, m rad, m, no dim	6*E
$ \begin{aligned} \delta Y, \delta T, \delta Z, \delta P, \\ \delta X, \delta D \end{aligned} $	Width of the bars (\pm) if uniform, Sigma value if Gaussian distribution	ibidem	6*E
$N_{\delta Y}, N_{\delta T}, N_{\delta Z}, N_{\delta P}, N_{\delta X}, N_{\delta D}$	Sorting cut-offs (used only for Gaussian density)	units of σ_Y , σ_T , etc.	6*E
N_0, C_0, C_1, C_2, C_3	Parameters involved in calculation of $P(D)$	no dim.	5*E
IR1, IR2, IR3	Random sequence seeds	$3^* \simeq 10^6$	3*I

¹ Let x = Y, T, Z, P or X. KY, KT, KZ, KP and KX can take the values

1 : uniform, $p(x) = 1/2\delta x$ if $-\delta x \leq x \leq \delta x$

2: Gaussian,
$$p(x) = \exp(-x^2/2\delta x^2)/\delta x \sqrt{2\pi}$$

3 : parabolic,
$$p(x) = 3(1 - x^2/\delta x^2)/4\delta x$$
 if $-\delta x \le x \le \delta x$

 $KD\xspace$ can take the values

1 : uniform, $p(D) = 1/2\delta\!D$ if $-\delta\!D \leq x \leq \delta\!D$

2: exponential, $p(D)=\operatorname{No}\,\exp(C_0+C_1l+C_2l^2+C_3l^3)$ if $-\delta D\leq x\leq \delta D$

3: kinematic, $D = \delta D * T$

If KOBJ = 3**Over 2-D** phase-space ellipses ¹. Four lines follow :

$ \begin{aligned} &\alpha_Y, \beta_Y, \varepsilon_Y/\pi, N_{\sigma_{\epsilon_Y}} \\ &[, N'_{\sigma_{\epsilon_Y}} \text{ if } N_{\sigma_{\epsilon_Y}} < 0]^2 \\ &[, D_Y, D_T] \end{aligned} $	Ellipse parameters and emittance, Y-T phase-space ; cut-off ; dispersion and derivative	no dim, m/rad, m, units of $\sigma(\varepsilon_Y)$; [, m, rad]	4*E [,E] [,2*E]
$ \begin{aligned} &\alpha_Z, \beta_Z, \varepsilon_Z/\pi, N_{\sigma_{\epsilon_Z}} \\ &[, N'_{\sigma_{\epsilon_Z}} \text{ if } N_{\sigma_{\epsilon_Z}} < 0]^2 \\ &[, D_Z, D_P] \end{aligned} $	Ellipse parameters and emittance, Z-P phase-space ; cut-off ; dispersion and derivative	no dim, m/rad, m, units of $\sigma(\varepsilon_Z)$ [, m, rad]	4*E [,E] [,2*E]
$ \begin{aligned} &\alpha_X, \beta_X, \varepsilon_X/\pi, N_{\sigma_{\epsilon_X}} \\ &[, N'_{\sigma_{\epsilon_X}} \text{ if } N_{\sigma_{\epsilon_X}} < 0]^2 \end{aligned} $	Ellipse parameters and emittance, X-D phase-space ; cut-off	no dim, m/rad, m, units of $\sigma(\varepsilon_X)$	4*E [,E]
IR1, IR2, IR3	Random sequence seeds. In order for different runs to produce different series (meaning, over seeds) launch zgoubi using 'irank' argument: [pathTo]/zgoubi -iranl	$3^* \simeq 10^6$ riding these c 'someNonZeroIintege	3*I er'.

¹ Similar possibilities, non-random, are offered with *OBJET*, KOBJ=8 (p. 298) ² Works with Gaussian density type only : sorting is within the ellipse frontier $\left(\frac{1+\sigma_Y^2}{\beta_Y^2}Y^2 + 2\alpha_YYT + \beta_YT^2 = \frac{\varepsilon_Y}{\pi}\right)$ if $N_{\sigma_{\epsilon_Y}} > 0$, or, if $N_{\sigma_{\epsilon_Y}} < 0$ sorting is within the annular region $\left[|N_{\sigma_{\epsilon_Y}}|, N'_{\sigma_{\epsilon_Y}}\right]$ of that ellipse.



A scheme of input parameters to *MCOBJET* when *KOBJ*= 2. Top : Possible distributions of the Y coordinate Bottom : A 2-D grid in (Y, Z) space.

MULTIPOL Magnetic Multipole

		dim.	data type	FIT num.
IL	$IL = 1, 2[\times 10^n], 7$: print coordinates, fields, etc., step-by-step,	$0-2[\times 10^n], 7$	Ι	1
$KL, R_0, B1, B2,, B10,$ Length of element ; radius at pole tip ; field at pole tip for dipole, quadrupole, , dodecapole components		2*cm,10*kG	12*E	2-13
$X_E, \lambda_E, E_2,, E_{10}$	Entrance face Integration zone ; fringe field extent : dipole fringe field extent = λ_E ; quadrupole fringe field extent = $\lambda_E * E_2$; 20-pole fringe field extent = $\lambda_E * E_{10}$ (sharp edge if field extent is zero)	2*cm,9*no dim	11*E	14-24
<i>NCE</i> , $C_0 - C_5$	same as QUADRUPO	0-6, 6*no dim	I, 6*E	25-31
$X_S, \lambda_S, S_2,, S_{10}$	Exit face Integration zone ; as for entrance	2*cm, 9*no dim	11*E	32-42
$NCS, C_0 - C_5$		0-6, 6*no dim	I, 6*E	43-49
<i>R</i> 1, <i>R</i> 2, <i>R</i> 3,, <i>R</i> 10	Skew angles of field components	10*rad	10*E	50-59
XPAS	Integration step	cm	Е	60-62
If KPOS = 1-3 <i>KPOS, XCE, YCE, ALE</i>	Positioning as follows : KPOS=1 : element aligned ; $KPOS=2$: misaligned ; shifts, tilt ; $KPOS=3$: effective only if $B1 \neq 0$: entrance and exit frames are tilted <i>wrt</i> . the magnet by an angle of • either ALE if ALE $\neq 0$ • or 2 Arcsin($B1 XL / 2BORO$) if ALE=0	1-3, 2*cm, rad	I, 3*E	63-66
If KPOS = 4 KPOS, XS, YS, ZR, ZS, YR	UNDER DEVELOPMENT X-, Y-shift, Z-rotation, Z-shift, Y-rotation Automatic ZR-positioning (as with ALE in case <i>KPOS</i> = 3).	4, cm, 2*(cm, rad) I, 5*E	63-68
If KPOS = 5 <i>KPOS</i> , XS, YS, ZS, XR, YR, ZR	UNDER DEVELOPMENT X-, Y-, Z-shift, X-, Y-, Z-rotation: Automatic ZR-positioning (as with ALE in case <i>KPOS</i> = 3).	5, 3*cm, 3*rad	I, 5*E	

OBJET	Generation of an object	(page 61 in PART A)		
BORO [* fac]	Reference rigidity = <i>BORO</i> [* <i>fac</i>], with <i>fac</i> an arbitrary numerical value.	kG.cm [,-]	E [,E]	
KOBJ[.K2]	Option index [.More options]	1-6	Ι	
If KOBJ = 1[.N]	By default, tracking assumes mid-plane symmetry; N=1: generate particles with $Z_0 > 0$ only; N=2: same as default, but all particles tracked, no mid-plane symmetry	netry assumed.		
IY, IT, IZ, IP, IS, ID	Ray-Tracing assumes mid-plane symmetry. Generated points : $YR \pm IY * dY$, $TR \pm IT * dT$, $ZR \pm IZ * dZ$, $PR \pm IP * dP$ $[ZR + IZ * dZ$, $PR + IP * dP$ if KOBJ = 1.1], $SR \pm IS * dS$ and $DR \pm ID * dD$ coordinates ($IY \le 20$,, $ID \le 20$)	$\mathrm{IY}*\mathrm{IT}*\mathrm{IZ}*\mathrm{IP}*\mathrm{IS}*\mathrm{ID} \leq 10^4$	6*1	
dY, dT, dZ, dP, dS, dD	Sampling size in Y, T, Z, P, S and in relative momentum $(dD = \delta B \rho / BORO)$	2(cm,mrad), cm, no dim	6*E	
YR, TR, ZR, PR, SR, DR	Reference trajectory ($DR = B\rho/BORO$)	2(cm,mrad), cm, no dim	6*E	
If KOBJ = 2[.1]	All the initial coordinates must be entered explicitly [2.1: units are	e different, see below]		
IMAX, IDMAX	total number of particles ; number of distinct momenta (if $IDMAX > 1$, group particles of same momentum)	$IMAX \le 10^4$	2*I	
For I = 1, IMAX	Repeat IMAX times the following line			
Y, T, Z, P, S, D, LET	Coordinates and tagging of the <i>IMAX</i> particles ; 2(cm,mrad), cm, no dim <i>If KOBJ</i> = 2.1 input units are different : 2(m,rad), m, no dim			
IEX(I = 1, IMAX)	X(I = 1, IMAX) IMAX times 1 or -9. If $IEX(I) = 1$ trajectory I is ray-traced, it is not if $IEX(I) = -9$.			
If KOBJ=3[.N, N=0 - 3] [, 'HEADER_NH']	Read coordinates from storage file. Optional 'HEADER_NH' tells lines NH (case $N \neq 0$: default NH=0; case N=0: NH=NHDFL N=0 (default): [b_]zgoubi.fai style data file FORMAT N=1: read FORMAT is ``READ (NL, *) Y, T, Z, P, S, DP'' N=2: read FORMAT is ``READ (NL, *) X, Y, Z, PX, PY, PZ'' N=3: read FORMAT is ``READ (NL, *) DP, Y, T, Z, P, S, TIME, N=4: read FORMAT is ``READ (NL, *) Y, T, Z, P, S, DP, LET N=5: read FORMAT is ``READ (NL, *) Y, T, Z, P, S, DP, LET N=6: read FORMAT is ``READ (NL, *) Y, Z, X, PY, PZ, PX''	s the number of header hardcoded in robjet.f). MASS,CHARGE'' C, IEN, IT'' Z,P,TIME, GAMMA''		
IT1, IT2, ITStep	Read particles numbered IT1 to IT2, step ITStep (For more than 10^4 particles stored in <i>FNAME</i> , use ' <i>REBELOTE</i> ')	$\geq 1, \geq IT1, \geq 1$	3*I	
IP1, IP2, IPStep	Read particles that belong in pass numbered IP1 to IP2, step IPStep	$\geq 1, \geq IP1, \geq 1$	3*I	
YF, TF, ZF, PF, SF, DF, TF, TAG	Scaling factor. TAG-ing letter : no effect if $TAG='*'$, otherwise only particles with TAG=LET are retained.	7*no.dim, char.	7*E, A1	
YR, TR, ZR, PR, SR, DR, TR	Reference. Given the previous line of data, all coordinate C (=Y, T) is transformed to C*CF+CR	2(cm, mrad), cm, no dim,µs	7*E	
InitC	0 : set new $\vec{R}_0 = \vec{R}_0$ as read, new $\vec{R} = \vec{R}$ as read ; 1 : set new $\vec{R}_0 = \vec{R}$ as read, new $\vec{R} = \vec{R}$ as read ; 2 : save \vec{R} as read in new \vec{R}_0 , set new $\vec{R} = \vec{R}_0$ as read.	0-1	Ι	
FNAME	File name (e.g., [b_]zgoubi.fai) (N in KOBJ=3.N determines formation of the second sec	atting)		

If KOBJ = 5[.N, $N \ge 1$]	Generation of 13 particles, or 13*N if $N \ge 2$ (for use with MAX)	TRIX[IORD=1], TWISS)	
dY, dT, dZ, dP, dS, dD	Sampling size in Y, T, Z, P, S (unused) and D	2(cm,mrad), cm, no dim	6*E
YR, TR, ZR, PR, SR, DR	Reference trajectory ($DR = B\rho/BORO$; SR is not sused)	2(cm,mrad), cm, no dim	6*E
$ \diamond \text{ If } N=1 (KOBJ = 5.1) \\ \alpha_Y, \beta_Y, \alpha_Z, \beta_Z, \alpha_S, \beta_S, \\ D_Y, D'_Y, D_Z, D'_Z $	One additional data line : Initial beam ellipse parameters ¹	2(no dim,m), ?, ?, 2(m,rad)	6*E 4*E
◊ If $N ≥ 2$ (KOBJ = 5.N) YR, TR, ZR, PR, SR, DR	An additional N-1 data lines ² Reference trajectory for each of the N-1 additional 13-particle sets # i=2,N; ($DR = B\rho/BORO$; SR is not sused).	2(cm,mrad), cm, no dim	6*E
If KOBJ = $\begin{bmatrix} 6 \\ 6.1 \end{bmatrix}$	Generation of $\begin{bmatrix} 61\\ 102 \end{bmatrix}$ particles (for use with <i>MATRIX</i> , <i>IORD</i>	$=\left[egin{array}{c}2\\3\end{array} ight)$	
dY, dT , dZ , dP , dS , dD	Sampling size in Y, T, Z, P, S (unused) and D	2(cm,mrad), cm, no dim	6*E
YR, TR, ZR, PR, SR, DR	Reference trajectory ; $DR = B\rho/BORO$	2(cm,mrad), cm, no dim	6*E
If KOBJ = 7	Object with kinematics		
IY, IT, IZ, IP, IS, ID	Number of points in $\pm Y$, $\pm T$, $\pm Z$, $\pm P$, $\pm S$; <i>ID</i> is not used	$IY*IT*IZ*IP*IS \le 10^4$	6*I
dY, dT , dZ , dP , dS , dD	Sampling size in Y, T, Z, P and S; dD = kinematic coefficient, such that $D(T) = DR + dD * T$	$2(\text{cm,mrad}), \text{cm, mrad}^{-1}$	6*E
YR, TR, ZR, PR, SR, DR	Reference ($DR = B\rho/BORO$)	2(cm,mrad), cm, no dim	6*E
If KOBJ = 8	Generation of phase-space coordinates on ellipses ³		
IY, IZ, IS	Number of samples in each 2-D phase-space ; if zero the central value (below) is assigned	$\begin{split} 0 &\leq IY, IZ, IS \leq IMAX, \\ 1 &\leq IY * IZ * IS \leq IMAX \end{split}$	3*I
$Y_0, T_0, Z_0, P_0, S_0, D_0$	Central values ($D_0 = B\rho/BORO$)	2(m, rad), m, no dim	6*E

¹ They can be transported by using MATRIX.
 ² The maximum value for N, normally MXREF=999, is hard-coded in obj5.f.
 ³ Similar possibilities, random, are offered with MCOBJET, KOBJ=3 (p. 294).

• Example : OBJET, KOBJ=3, recovering from a crash

The job below simulates spin tracking in SATURNE 3 GeV proton synchrotron. Turn-by-turn coordinates at the beginning of the ring sequence are stored in zgoubi.fai during the tracking. *CAVITE/Option=2* is used.

The left column shows the input data file for initial job, turn3000.dat. Note: the 'INCLUDE' command uploads SATURNE.ring sequence, from the very file used in the example in Sec. 5 (page 362, PART B of the guide) - it only loads that part of the file which is comprised between the markers labelled "#StartRing" and "#EndRing").

The right column, job resume.dat, shows how *OBJET*, *KOBJ=3* is used to allow resuming tracking at start of turn #1000, possibly following a crash during that turn. *OBJET*, *KOBJ=3* requests reading initial coordinates from turn3000.fai, at turn 1000.

A possible check: the 2,000 tracking by resume.dat (right column below) should yield all three phase spaces, namely, (Y, T), (Z, P), (D, time) superimposing with turns 1,000-3,000 of the original turn3000.dat job (left column). If this does not happen: a quick check is by comparison of turn 1000 in turn3000.fai and the initial value of the coordinates in resume.fai, they should be *identical*.

This 3,000-turn job crashed at turn number 1,000.	coordinates as read at turn 1,000 in turn3000.fai.
the optical sequence, in turn3000.fai.	SATURNE. CROSSING GammaG=7-NUz, NUz=3.60877(perturbed) 'OBJET'
SATURNE. CROSSING GammaG=7-NUz, NUz=3.60877(perturbed) 'OBJET'	3 1 1 1
5018.67	1000 1000 1
2	1. 1. 1. 1. 1. 1. *
1 1	0. 0. 0. 0. 0. 0. 0.
0. 0458 0. 0. 1.00 'o' 1	0 turn3000.fai
'PARTICUL'	'PARTICUL'
PROTON	PROTON
'SPNTRK'	'SPNTRK'
3	3
'FAISCNL'	'FAISTORE'
turn3000.fai	resume.fai
'SCALING'	1
1 3 PRINT	'SCALING'
QUADRUPO	1 3 PRINT
-1	QUADRUPO
5018.67E-3	-1
1	5018.67E-3
MULTIPOL	1
-1	MULTIPOL
5018.67E-3	-1
1	5018.67E-3
BEND	1
-1	BEND
5018.67E-3	-1
1	5018.67E-3
	1
'INCLUDE'	
1	'INCLUDE'
SATURNE.ring[#StartRing:#EndRing]	1
	SATURNE.ring[#StartRing:#EndRing]
'CAVITE'	
2 PRINT	'CAVITE'
105.5556848673 3.	2 PRINT
6000. 0.205303158892	105.5556848673 3.
	6000. 0.205303158892
'REBELOTE'	
2999 0.2 99	'REBELOTE'
'FAISCEAU'	2000 0.2 99
'SPNPRT'	'FAISCEAU'
'END'	SPNPRT'
	'END'

Particle and spin coordinates at the end of the complete 3,000 turn run and at the end of the 1,000 to 3,000 turn recovery, as from the two files above, are *identical*, they are displayed below.

				(fo	TRACE DU FAIS llows element l TRAJECI	SCEAU : # 90) FOIRES							
			c	BJET					FAISCEAU	J			
	D	Y(cm)	T(mr)	Z(cm)	P(mr)	S(cm)	D-1	Y(cm)	T(mr)	Z(cm)	P(mr)	S(cm)	
o 1	1.0000	0.000 Time of fl:	0.000 ight (mus)	0.458 : 1244.3	0.000 530 mass	0.0000 (MeV/c2) :	0.0029 938.272	0.006	0.007	0.498	-1.263	0.00000E+00	1
		Spin comp	ponents of	each of	the 1	particles	s, and ro	otation a	ingle :				
		INITIA	Ĺ				FINAL						
	SX	SY	SZ	S	SX	SY	SZ	S	GAMMA (Sf_X :	A (Si (de proje	,Sf) (Z eg.) (ction of	,Sf_X) (Z,Sf) deg.) (deg.) Sf on YZ plane)	
o 1	0.000000	0.000000	1.000000	1.000000	-0.926463	0.185319	0.327602	1.000000	1.89	937 7	0.877 2	9.496 70.877	1

The input data below recover from the crash, starting with

OBJETA	Object from Monte-Carlo simulation of decay reaction						
	$M1 + M2 \longrightarrow M3 + M4$ and $M4 \longrightarrow M5 + M6$						
BORO	Reference rigidity	kG.cm	Е				
IBODY, KOBJ	Body to be tracked : $M3$ (<i>IBODY</i> =1), $M5$ (<i>IBODY</i> =2) $M6$ (<i>IBODY</i> =3) ; type of distribution for Y_0 and Z_0 : uniform (<i>KOBJ</i> =1) or Gaussian (<i>KOBJ</i> =2)	1-3,1-2	2*I				
IMAX	Number of particles to be generated (use ' <i>REBELOTE</i> ' for more)	$\leq 10^4$	Ι				
$M_{1} - M_{6}$	Rest masses of the bodies	6*GeV/c ²	6*E				
T_1	Kinetic energy of incident body	GeV	Е				
Y_0, T_0, Z_0, P_0, D_0	Only those particles in the range $Y_0 - \delta Y \le Y \le Y_0 + \delta Y$	2(cm,mrad), no dim	5*E				
	$D_0 - \delta D \le D \le D_0 + \delta D$ will be retained						
$\delta Y, \delta T, \delta Z, \delta P, \delta D$		2(cm,mrad), no dim	5*E				
XL	Half length of object : $-XL \le X_0 \le XL$ (uniform random distribution)	cm	E				
IR1, IR2	Random sequence seeds	$2^* \simeq 0^6$	2*I				

OCTUPOLE	Octupole magnet	(page 128 in PART	A)
IL	$IL = 1, 2[\times 10^n], 7$: print coordinates, fields, etc., step-by-step, in zgoubi.res (1), zgoubi.plt (2), zgoubi.impdev.out (7).	$0-2[\times 10^n], 7$	Ι
XL, R_0, B_0	Length ; radius and field at pole tip of the element	2*cm, kG	3*E
X_E, λ_E	Entrance face : Integration zone ; Fringe field extent ($\lambda_E = 0$ for sharp edge)	2*cm	2*E
<i>NCE</i> , $C_0 - C_5$	<i>NCE</i> = unused $C_0 - C_5$ = fringe field coefficients such that : $G(s) = G_0/(1 + \exp P(s))$, with $G_0 = B_0/R_0^3$ and $P(s) = \sum_{i=0}^5 C_i(s/\lambda)^i$	0-6, 6*no dim	I, 6*E
X_S, λ_S	Exit face : Parameters for the exit fringe field ; see entrance	2*cm	2*E
<i>NCS</i> , $C_0 - C_5$		0-6, 6*no dim	I, 6*E
XPAS	Integration step	cm	Е
KPOS, XCE, YCE, ALE	KPOS=1 : element aligned, 2 : misaligned ; shifts, tilt.	1-2, 2*cm, rad	I, 3*E



Octupole magnet

OPTICS

Write out optical functions. Log to zgoubi.OPTICS.out

IOPT[.NLBL], label(s)	IOPT = 0/1: Off/On; NLBL = number of labels (default is 1);	0-1[.1-10], - ,	I[.I],
[,PRINT]	'label' : can be 'all', 'ALL', or a list of NLBL first label(s) as	-,-	1-10*A20,
[, coupled]	appearing at one or more elements in zgoubi.dat sequence ;		I1 or A5, A7
	wild card accepted, in the form '*label' or 'label*' or '*label*'.		
	Presence of 'PRINT' will cause print out of optical		
	functions in zgoubi.OPTICS.out ; optical function computation is		
	in coupled hypothesis if specified, uncoupled otherwise.		

• Example : OPTICS

The following will cause a print of transported optical functions in zgoubi.res, at all optical elements of the zgoubi.dat sequence, as well as their print out in zgoubi.OPTICS.out :

'OPTICS' 1 all PRINT

OPTIONS	Global or special options	(page 172 in PART A)	
IOPT, NBOP	IOPT = 0/1: Off/On ; 0 (off) will inhibit all <i>NBOP</i> subsequent requests. <i>NBOP</i> : total number of options.	0-1 , ≥ 0	2*I
NBOP lines follow. Po	ossible choices :		
'WRITE', OPT	OPT = ON/OFF : allows/inhibites (most) write statements to zgoubi.res.	'WRITE', 'ON' or 'OFF'	2*A
'.plt', IL	IL=-1, 0-2, 7: option inactive (IL=-1); all .plt inhibited (IL=0); log stepwise particle data to zgoubi.res (IL=1), or to zgoubi.plt (IL=2), or to zgoubi.impdev.out (IL=7).	'.plt', -1,0-2,7	A, I
'CONSTY', OPT	OPT = ON : forces constant Y and Z across optical elements.	'CONSTY', 'ON' or 'OFF'	2*A
'AGSQUADS', OPT	OPT = ON : modify winding currents (agsquf.f does that).	'AGSQUADS', 'ON'	2*A
'MONITOR', OPT	OPT = IDLUNI : monitor IDLUNI counter.	'AGSQUADS', 'IDLUNI'	2*A

• Example : OPTIONS, CONSTY

The example below yields (data saved to zgoubi.plt due to IL = 2) 3-D field components (trivially uniform in that particular case, $B_R = B_\theta = 0$, $B_Z = B_0$ at all (R, θ, Z)) on a $n_R \times n_\theta \times n_Z = (41-1)/2 \times (R*AT/XPAS) \times (11-1)/2$ node, uniform 3-D mesh, with $\Delta R = \delta Y$ in *OBJET* = 1 cm, $\Delta \theta \equiv XPAS/RM = 10.471975512$ mrd, $\Delta Z = \delta Z$ in *OBJET* = 0.2 cm, across a 60 degree hard-edged sector dipole (6 of these make up a uniform field cyclotron).

```
Cyclotron, classical.
'OBJET'
1000.e0
 41 1 11 1 1 1
 1. 0. 0.2 0. 0. 1.
0. 0. 0. 0. 0. 1.
  'OPTIONS'
1 1
CONSTY ON
 'DIPOLES'
2
1 60.50.
30.0.5.10.
30. 0. 5. 1 0.

0. 0.

4 .1455 2.2670 -.6395 1.1558 0. 0. 0.

30. 0. 1.E6 -1.E6 1.E6 1.E6

0. 0.

4 .1455 2.2670 -.6395 1.1558 0. 0. 0.

-30. 0. 1.E6 -1.E6 1.E6 1.E6

0 0
                                                                         ! EFB 1 hard-edge
                                                                         ! EFB 2
                                                                        ! EFB 3
                                                       0.0.0.
0 0. 0. 0. 0. 0. 0.
0. 0. 0. 0. 0. 0. 0. 0.
0 2 KIRD, Resol=IDB
0.523598775598
 2 00. 0. 00. 0.
  'FAISCEAU'
  'END'
```

ORDRE Taylor expansions order

IO	Taylor expansions of \vec{R} and \vec{u} (Eq. 1.2.4) up to $\vec{u}^{(IO)}$	2-5	Ι
	(default is $IO = 4$)		

PARTICUL Particle characteristics

Either :

M, Q, G, τ, X	Mass (or coded, see Note below) ; charge ; gyromagnetic factor ; COM life-time ; unused	MeV/c ² , C, no dim, s, NA	5*E
or :			
Name	ELECTRON, POSITRON, MUON+, MUON-, PION+, PION-, PROTON, DEUTERON, HELION		А

Note : If M is of the form {M1 M2}, then when masses are assigned to particles from a previously defined object (by [MC]OBJET), then the first half of the particles are given the mass M1, and the second half are given the mass M2.

If Q is zero, the reference charge is left unchanged.

Only the parameters to be used need their value be specified (for instance M, Q only when electric lenses are used, M, Q, G only when tracking spin, etc.); unused parameters can be set to zero.

PICKUPS	Bunch centroid path; orbit Particle coordinates at pickups may be printed out in zgoubi.PICKUP.out; they are anyway listed next to the sequence ' <i>END</i> ' keyword down zgoubi.res. In multi-turn mode, pickup contents are zeroed at start of each pass.		
N [, PRINT]	0 : inactive ≥ 1 : number of <i>LABELs</i> at which beam centroid is computed <i>[,PRINT]</i> is optional: will cause print of pickup contents to zgoubi.	≥ 0 [, string] PICKUP.out.	I [,A]
A list of N keywords' label	s follows		
LABEL1 [,LABEL2, []]	The N label(s) at which beam data are to be computed/recorded.	N string(s)	N*A20

wild card accepted, in the form '*LABEL' or 'LABEL*' or '*LABEL*'.

If some "*LABELi*" in this list actually does not appear in zgoubi.dat optical sequence, then it is peacefully ignored ;

• Example : PICKUPS

A trick :

```
'PICKUPS'
1
none labelA labelB ...
```

This is a possible way to inhibit an earlier use of *PICKUPS* with "labelA, labelB, ..." keyword list. It is sufficient (and necessary) for that, that no keyword in zgoubi.dat data list have "none" as its first *LABEL*.

PLOTDATA Intermediate output for the PLOTDATA graphic software

To be documented.

POISSON	Read magnetic field data from POISSON output		
IC, IL	IC = 1, 2: print the field map $IL = 1, 2[\times 10^n], 7$: print coordinates, fields, etc., step-by-step, in zgoubi.res (1), zgoubi.plt (2), zgoubi.impdev.out (7).	$0-2; 0-2[\times 10^n], 7$	2*I
BNORM, XN, YN	Field and X-, Y-coordinate unit conversion coeffs.	3*no dim	3*E
TITL	Title. Start with "FLIP" to get field map X-flipped		A80
IX, IY	Number of longitudinal and transverse nodes of the uniform mesh	$\leq 400, \leq 200$	2*I
FNAME ¹	File name		A80
ID, A, B, C [, A', B', C', B", etc., if $ID \ge 2$]	Integration boundary. Ineffective when $ID = 0$. $ID = -1$, 1 or ≥ 2 : as for <i>CARTEMES</i>	≥ -1, 2*no dim, cm [,2*no dim, cm, etc.]	I,3*E [,3*E,etc.]
IORDRE	Degree of interpolation polynomial as for <i>DIPOLE-M</i>	2, 25 or 4	Ι
XPAS	Integration step	cm	Е
KPOS, XCE, YCE, ALI	E KPOS=1 : element aligned, 2 : misaligned ; shifts, tilt.	1-2, 2*cm, rad	I, 3*E

¹ *FNAME* (*e.g.*, ''outpoi.lis'') contains the field map data. These must be formatted according to the following *FORTRAN* read sequence - details and possible updates are to be found in the source file ' fmapw.f':

I = 011 CONTINUE I = I+1READ(LUN,101,ERR=99,END=10) K, K, K, R, X(I), R, R, B(I) 101 FORMAT(I1, I3, I4, E15.6, 2F11.5, 2F12.3) GOTO II 10 CONTINUE

where X(I) is the longitudinal coordinate, and B(I) is the Z component of the field at a node (I) of the mesh. K's and R's are variables appearing in the POISSON output file outpoi.lis, not used here.

POLARMES	2-D polar mesh magnetic field map mid-plane symmetry is assumed		
IC, IL	IC = 1, 2: print the map $IL = 1, 2[\times 10^n], 7$: print coordinates, fields, etc., step-by-step, in zgoubi.res (1), zgoubi.plt (2), zgoubi.impdev.out (7).	$0-2; 0-2[\times 10^n], 7$	2*I
BNORM, AN,RN	Field and A-,R-coordinate unit conversion coeffs.	3*no dim	3*E
TITL	Title. Start with "FLIP" to get field map X-flipped		A80
IA, JR	Number of angular and radial nodes of the mesh	$\leq 400, \leq 200$	2*I
FNAME ¹	File name		A80
ID, A, B, C [, A', B', C', B", etc., if $ID \ge 2$]	Integration boundary. Ineffective when $ID = 0$. $ID = -1$, 1 or ≥ 2 : as for <i>CARTEMES</i>	≥ -1 , 2*no dim, cm [,2*no dim, cm, etc.]	I,3*E [,3*E,etc.]
IORDRE	Degree of interpolation polynomial (see <i>DIPOLE-M</i>)	2, 25 or 4	Ι
XPAS	Integration step	cm	E
KPOS	as for DIPOLE-M. Normally 2.	1-2	Ι
$\begin{array}{l} \mathbf{I} \ \mathbf{KPOS} = 2 \\ RE, TE, RS, TS \\ \mathbf{KKPOS} = 1 \end{array}$		cm, rad, cm, rad	4*E
DP		no dim	E

 1 FNAME (e.g., spes2.map) contains the field data. These must be formatted according to the following FORTRAN read sequence - details

and possible updates are to be found in the source file ' fmapw.f' :

```
\begin{array}{l} \text{OPEN} \left(\text{UNIT} = \text{NL}, \text{FILE} = \text{FNAME}, \text{STATUS} = \text{`OLD'} \left[, \text{FORM='UNFORMATTED'} \right] \right) \\ \text{IF} \left(\text{BINARY}\right) \text{THEN} \\ \text{READ}(\text{NL}) \left(\text{Y}(\text{J}), \text{J=1}, \text{JY}\right) \\ \text{ELSE} \\ \text{READ}(\text{NL}, 100) \left(\text{Y}(\text{J}), \text{J=1}, \text{JY}\right) \\ \text{ENDIF} \\ 100 \quad \text{FORMAT}(10 \text{ F8.2}) \\ \text{DO 1 I = 1, IX} \\ \text{IF} \left(\text{BINARY}\right) \text{THEN} \\ \text{READ} \left(\text{NL}\right) X(\text{I}), \left(\text{BMES}(\text{I},\text{J}), \text{J=1}, \text{JY}\right) \\ \text{ELSE} \\ \text{READ}(\text{NL}, 101) X(\text{I}), \left(\text{BMES}(\text{I},\text{J}), \text{J=1}, \text{JY}\right) \\ \text{ELSE} \\ \text{READ}(\text{NL}, 101) X(\text{I}), \left(\text{BMES}(\text{I},\text{J}), \text{J=1}, \text{JY}\right) \\ 101 \quad \text{FORMAT}(10 \text{ F8.1}) \\ \quad \text{ENDIF} \\ 1 \quad \text{CONTINUE} \end{array}
```

where X(I) and Y(J) are the longitudinal and transverse coordinates and *BMES* is the Z field component at a node (I, J) of the mesh. For binary files, *FNAME* must begin with 'B_' or 'b_'. 'Binary' will then automatically be set to '.TRUE.'

PS170	Simulation of a round shape dipole magnet		
IL	$IL = 1, 2[\times 10^n], 7$: print coordinates, fields, etc., step-by-step, in zgoubi.res (1), zgoubi.plt (2), zgoubi.impdev.out (7).	$0-2[\times 10^n], 7$	Ι
XL, R_0, B_0	Length of the element, radius of the circular dipole, field	2*cm, kG	3*E
XPAS	Integration step	cm	Е
KPOS, XCE, YCE, ALE	KPOS=1 : element aligned, 2 : misaligned ; shifts, tilt.	1-2, 2*cm, rad	I, 3*E



Scheme of the PS170 magnet simulation.

QUADISEX	Sharp edge magnetic multipoles $B_Z \mid_{Z=0} = B_0 \left(1 + \frac{N}{R_0}Y + \frac{B}{R_0^2}Y^2 + \frac{G}{R_0^3}Y^3 \right)$		
IL	$IL = 1, 2[\times 10^n], 7$: print coordinates, fields, etc., step-by-step, in zgoubi.res (1), zgoubi.plt (2), zgoubi.impdev.out (7).	$0-2[imes 10^n], 7$	Ι
XL, R_0, B_0	Length of the element ; normalization distance ; field	2*cm, kG	3*E
N, EB1, EB2, EG1, EG2	Coefficients for the calculation of B. if $Y > 0$: $B = EB1$ and $G = EG1$; if $Y < 0$: $B = EB2$ and $G = EG2$.	5*no dim	5*E
XPAS	Integration step	cm	Е
KPOS, XCE, YCE, ALE	<i>KPOS</i> =1 : element aligned, 2 : misaligned ; shifts, tilt.	1-2, 2*cm, rad	I, 3*E

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QUADRUPO	Quadrupole magnet	(page 133 in PART	A)
IL	$IL = 1, 2[\times 10^n], 7$: print coordinates, fields, etc., step-by-step, in zgoubi.res (1), zgoubi.plt (2), zgoubi.impdev.out (7).	$0-2[\times 10^n], 7$	Ι
XL, R_0, B_0	Length ; radius and field at pole tip	2*cm, kG	3*E
X_E, λ_E	Entrance face : Integration zone extent ; fringe field extent ($\simeq 2R_0, \lambda_E = 0$ for sharp edge)	2*cm	2*E
<i>NCE</i> , $C_0 - C_5$	<i>NCE</i> = unused $C_0 - C_5$ = Fringe field coefficients such that $G(s) = G_0/(1 + \exp P(s))$, with $G_0 = B_0/R_0$ and $P(s) = \sum_{i=0}^5 C_i(s/\lambda)^i$	0-6, 6*no dim	I, 6*E
X_S, λ_S NCS, $C_0 - C_5$	Exit face See entrance face	2*cm 0-6, 6*no dim	2*E I, 6*E
XPAS	Integration step	cm	Е
KPOS, XCE, YCE, ALE	KPOS=1 : element aligned, 2 : misaligned ; shifts, tilt.	1-2, 2*cm, rad	I, 3*E







Scheme of the elements QUADRUPO, SEXTUPOL, OCTUPOLE, DECAPOLE, DODECAPO and MULTIPOL

(OX) is the longitudinal axis of the reference frame (0, X, Y, Z) of **zgoubi**.

The length of the element is XL, but trajectories are calculated from $-X_E$ to $XL + X_S$, by means of automatic prior and further X_E and X_S translations.

REBELOTE

'Do it again'

NPASS, KWRIT, K[.n], [IOPT], [, LABEL1 [, LABEL2']]	NPASS : Number of runs ; $KWRIT = i.j$: $i=1/0$ to switch arbi on/off FORTRAN WRITEs to .res, j=integer ≥ 1 for logging 0, 99 turn number to screen every 10^{j-1} turns; 0-1 K option : K = 0: initial conditions (coordinates and spins) are generated following the regular functioning of [MC]OBJET. If random generators are used (e.g. in MCOBJET) their seeds will not be reset. K = 99 or 98 : coordinates at end of previous pass are used as initial coordinates for the next pass ; <i>idem</i> for spin components. K=99 causes a reset of particle path-length in CAVITE ¹ , K=98 does not. K=98 IS UNDER DEVELOPMENT, IN cavite.f, IN THIS VERSION OF THE K = 99.1 : a "LABEL1" is expected in the optical sequence, subsequent passed will start from that element with LABEL1, down to REBELOTE and so forth K = 99.2 : "LABEL1" and "LABEL2" are expected ; the last pass (# NPASS will terminate at element with LABEL1' whereupon zgoubi execution will jurn keyword next to REBELOTE and will be carried out down to 'END'. IOPT is optional : IOPT = 1 : will change the value of NPRM different parameters in one or more of optical elements, using the data list in the next line.	trary ; 0-1 ; 9 ; [1[.any]] ; 0, 22, 99 E CODE. es ; +1) np to the	3*I 2A10 2A10
If IOPT = 1^2			
NPRM	Number of parameters to be changed at each of the NPASS passes.		Ι
NPRM lines with the folle	owing sequence (tells parameters concerned, and for each, its successive value	es) :	
<i>LMNT, KPRM</i> , values	 LMNT : two possible forms : (i) LMNT=element number in zgoubi.dat -, -, sequence ; (ii) LMNT=KEYWORD[{LABEL1 [, LABEL2]}], i.e., NV keyword concerned followed optionnally by LABEL1 (and possibly LABEL2) concerned. KPRM : parameter number under that keyword (similar nomenclature to FIT[2], see page 273) ; 'values' defines the new parameter values. 'values' can take two forms : either an explicit list of NPASS numerical values or, first_value:last_value - the interval between consecutive values will be (last_value - first_value)/(npass-1). 	NV*dim ³ *E	I or A, I

¹ Usefull if the tracking distance is orders of magnitudes greater than particle distances within a bunch: the computation of the synchronous phase of a particle (from its total path length and its distance to the virtual synchronous particle) may be jeopardized if the difference is within computer accuracy. ² *IOPT=1* is compatible with use of the *FIT[2]* procedure : *e.g.*, allows successive *FIT*s in a single **zgoubi** run, with successive sets of optical parameter values.

 $^{^{3}}$ V is in current **zgoubi** units in the case of particle coordinates (cm, mrad). It is in MKSA units (m, rad) in the case of matrix coefficients.

• Example : REBELOTE[IOPT=1]

In this example of an energy-recovery electron recirculator based on FFAG arcs, the arguments in the keyword AUTOREF and CAVITE are changed 20 times by REBELOTE, over the 21-pass recirculation process [84]. The role of AUTOREF is to mimic a spreader-recombiner, i.e., re-centering the beam on the design FFAG orbit at the start of each one of the 11 accelerated and 10 decelerated return loop passes. The RF voltage in CAVITE is set positive (accelerating, from 7.944 GeV to 21.16 GeV) during the first 11 passes through the optical structure, and negative (decerating, from 21.16 to 7.944 GeV) over the remaining 10 passes. The voltage value at each pass is adjusted (for an energy of 1.322 GeV per turn on average) so to compensate the energy lost by synchrotron radiation in the arcs.

eRHIC ENERGY RECOVERY LINAC RECIRCULATOR WITH FFAG ARCS. 'MCOBJET' 57.36635309d3 reference rigidity (kG.cm) 2000 2 2 2 2 1 1 -5.360667E-03 5.059706E-3 0. 0. 0. 4.619439E-01 'o' 0.1 0. 3 0.1 0. 3 123456 234567 345678 2 'PARTICUL 0.51099892 1.60217653e-19 1.15965218076e-3 0.0 0.0 'SPNTRK' 'FAISCEAU' 'FAISCEAU' 'SRLOSS' 1 srLoss MULTIPOL 1 123456 'SCALING' 6 1 MULTIPOL 57.36635309 57.36635309 11 'MARKER' ARC#S_1 'OPTIONS' 7 8 1 1 WRITE OFF 'MARKER' MARK CELL 'DRIFT' DRIF HD 14.547181 'MULTIPOL' RBEN BD2 CELLSTART HD 10 11 'MULTIPOL' REN ED2
O . Dip
90. 10. 0. -0.87159105 0. 0. 0. 0. 0. 0. 0. 0. 0. 0. 0.
0. 4. 1455 2.2670 -.6395 1.1558 0. 0. 0. 0.
0. 0. 10.00 4.0 0.800 0.00 0.00 0.00 0.00 0. 0. 0. 0.
1.455 2.2670 -.6395 1.1558 0. 0. 0.
0. 0. 0. 0. 0. 0. 0. 0. 0. 0. 0.
1.41455 2.2670 -.6395 1.1558 0. 0. 0.
1.41455 2.2670 -.6395 1.1558 0. 0. 0.
1.41455 2.2670 -.6395 1.1558 0. 0. 0.
1.41455 2.2670 -.6395 1.1558 0. 0. 0.
1.41455 2.2670 -.6395 1.1558 0. 0. 0.
1.41455 2.2670 -.6395 1.1558 0. 0. 0.
1.41455 2.2670 -.6395 1.1558 0. 0. 0.
1.41455 2.2670 -.6395 1.1558 0. 0. 0.
1.41455 2.2670 -.6395 1.1558 0. 0. 0.
1.41455 2.2670 -.6395 1.1558 0. 0. 0.
1.41455 2.2670 -.6395 1.1558 0. 0. 0.
1.41455 2.2670 -.15071892929E-03
2.401471 -.1507189
2.401471 -.1507189
2.401471 -.1507189
2.401471 -.1507189
2.401471 -.1507189
2.4 12 29.094362

'MULTIPOL' RBEN QF2	13
0 .Dip	
110. 10. 0. 0.86286642 0. 0.0 0.0 0.0 0.0 0.0 0.0	0.0
0. 0. 10.00 4.0 0.800 0.00 0.00 0.00 0.00 0. 0. 0.	0.
4 .1455 2.26706395 1.1558 0. 0. 0.	
0. 0. 10.00 4.0 0.800 0.00 0.00 0.00 0.00 0. 0. 0.	0.
4 .1455 2.26706395 1.1558 0.0.0.	
0. 0. 0. 0. 0. 0. 0. 0. 0. 0.	
#30 110 30 Dip QF2	
3 03.6008008661E-01 -1.8710983347E-03	
'DRIFT' DRIF HD	14
14.54/181	
'MARKER' MARK CELLEND	15
6-138-1 additional such ED colls simulating a 6 arc	
energy recovery ring 138 cells per arc	
'MARKER' ARC#E 6	5820
'OPTIONS'	5821
1 1	
WRITE ON	
'FAISTORE'	5822
zgoubi.fai	
1	
'FAISCEAU'	5823
'CAVITE'	5824
3	
0 0	
1.322e9 1.57079632679	
'AUTOREF'	5825
4.1	
05.168354E-01 4.169759E+00 5.38813280E-01	
'FAISCEAU'	5826
'REBELOTE'	5827
20 0.1 99 1	
AUTOREF 11 -4.7493E-01 -4.1290E-01 -3.3292E-01 -2.36	34E-01
-1.26268E-01 -2.59/05E-03 (a list of 20 values	00010
AUTOREF 12 3.34619E+UU 2.58215E+UU 1.8/15/E+UU 1	20916
5.9019/E-01 1.0569/E-02 (a list of 20 values	
AUTUREF 15 .015002000 .092552080 .709421480 .84	222000
-323100200 1.00002370 (d 11St OI 20 Values CNVITE 20 1.33730060 1.3303460 1.3401260 1.24	11869
(15 more voltage values)1 30660-0 1 200	57769
<pre>/cpppNT/</pre>	5828
OIN INFI	J020

'END'

• Example : Combining REBELOTE and FIT

See page 274.

5829

RESET

Reset counters and flags

Resets counters involved in CHAMBR, COLLIMA, HISTO and INTEG procedures.

Switches off CHAMBR, MCDESINT, SCALING and SPNTRK options.

SCALING	Power supplies and R.F. function generator	(page 178 in PAR	AT A)
IOPT, NFAM [, PRINT]	IOPT = 0 (inactive) or 1 (active); $NFAM =$ number of families to be scaled. Occurence of <i>PRINT</i> will cause printing of scaling infos in zgoubi.SCALING.out.	0-1, 1-45 [,-]	I1, I2 [,A]
For NF=1, NFAM :	repeat NFAM times the following sequence :		
NAMEF [, Lbl]	Name of family (<i>i.e.</i> , keyword of concern) ; up to 9 labels, wild card accepted, in the form '*myLABEL' or 'myLABEL*'.		A10 [,1-9*A20]
NT [.Int]	$NT \ge 1$: normal usage, number of timings (see $NT = -1$ for a convenient, easy short-cut); 1.Int: Int=1 or 10-13, optional. For special scaling laws and/or reading from external files; $NT = -1$: field scaling is updated to follow $B\rho$ change by <i>CAVITE</i> ; NT = -2: to read RF law for <i>CAVITE</i> from an external data file; $NT = -60$: field scaling follows $B\rho$ change by <i>CAVITE</i> - to be documented NT = -87: AGS tune-jump quadrupoles - to be documented ¹ ; NT = -88: AC dipole function generator ² .	-88[.1, .1013], , 1[.1, .1013] ented ¹ ; d ¹ ;	I[.1]
SCL(I), I = 1, NT	Scaling values. if $NT = 1$: $SCL(I) = SCL(1)$ whatever the pass number. Special cases :	-	NT*E E
	if $NT = -1$: a single value, SCL [* fac] (scaling value is SCL [* fac], with fac an arbitrary numerical value); if $NT = -2$: unused; if $NT = -88$, four vlues expected : phase of the ac dipole; Q1, tune at start of the sweep; Q2, tune at end of the sweep; scale factor.	- [, -] - rad, -, -, -	E [, E] E 4*E
TIM(I), I = 1, NT	Corresponding timings, in units of turns Special cases : if $NT = -1$ · TIM(I=1)=1 ·	NT turn#	NT*I I
	if $NT = -2$: unused; if $NT = -88$, four turn numbers expected : hold duration (at zero); ramp up duration; sweep duration; ramp down duration.	- - 4 turn#	I 4*E

SEPARA¹ Wien Filter - analytical simulation

IA, XL, E, B,	IA = 0: element inactive	0-2, m,	I, 3*E
	IA = 1: horizontal separation	V/m, T	
	IA = 2: vertical separation ;		
	Length of the separator; electric field; magnetic field.		



Horizontal separation between a wanted particle, (W), and an unwanted particle, (U). (W) undergoes a linear motion while (U) undergoes a cycloidal motion.

¹ SEPARA must be preceded by PARTICUL for the definition of mass and charge of the particles.

SEXQUAD	Sharp edge magnetic multipole $B_Z \mid_{Z=0} = B_0 \left(\frac{N}{R_0} Y + \frac{B}{R_0^2} Y^2 + \frac{G}{R_0^3} Y^3 \right)$		
IL	$IL = 1, 2[\times 10^n], 7$: print coordinates, fields, etc., step-by-step, in zgoubi.res (1), zgoubi.plt (2), zgoubi.impdev.out (7).	$0-2[\times 10^n], 7$	Ι
XL, R_0, B_0	Length of the element ; normalization distance ; field	2*cm, kG	3*E
N, EB1, EB2, EG1, EG2	Coefficients for the calculation of B. if $Y > 0$: $B = EB1$ and $G = EG1$; if $Y < 0$: $B = EB2$ and $G = EG2$.	5*no dim	5*E
XPAS	Integration step	cm	Е
KPOS, XCE, YCE, ALE	KPOS=1 : element aligned, 2 : misaligned ; shifts, tilt.	1-2, 2*cm, rad	I, 3*E

SEXTUPOL	Sextupole Magnet		
IL	$IL = 1, 2[\times 10^n], 7$: print coordinates, fields, etc., step-by-step, in zgoubi.res (1), zgoubi.plt (2), zgoubi.impdev.out (7).	$0-2[\times 10^n], 7$	Ι
XL, R_0, B_0	Length ; radius and field at pole tip of the element	2*cm, kG	3*E
X_E, λ_E	Entrance face : Integration zone ; fringe field extent ($\lambda_E = 0$ for sharp edge)	2*cm	2*E
<i>NCE</i> , $C_0 - C_5$	NCE = unused $C_0 - C_5$ = Fringe field coefficients such that $G(s) = G_0/(1 + \exp P(s))$, with $G_0 = B_0/R_0^2$ and $P(s) = \sum_{i=0}^5 C_i(s/\lambda)^i$	0-6, 6* no dim	I, 6*E
	Exit face :		
X_S, λ_S	Parameters for the exit fringe field ; see entrance	2*cm	2*E
<i>NCS</i> , $C_0 - C_5$		0-6, 6*no dim	I, 6*E
XPAS	Integration step	cm	Е
KPOS, XCE, YCE, ALE	KPOS=1 : element aligned, 2 : misaligned ; shifts, tilt.	1-2, 2*cm, rad	I, 3*E



Sextupole magnet

SOLENOID	Solenoid	(page 137 in PART A))
IL	$IL = 1, 2[\times 10^n], 7$: print coordinates, fields, etc., step-by-step, in zgoubi.res (1), zgoubi.plt (2), zgoubi.impdev.out (7).	$0-2[\times 10^n], 7$	Ι
XL, R ₀ , B ₀ [, MODL]	Length ; radius ; asymptotic field (= $\mu_0 NI/XL$) ; $MODL=1$: default, <i>r</i> -extrapolation from on-axis field model, $MODL=2$: elliptic integrals method	2*cm, kG [, no dim]	3*E
X_E, X_S	Entrance and exit integration zones	2*cm	2*E
XPAS	Integration step	cm	Е
KPOS, XCE, YCE, ALE	KPOS=1 : element aligned, 2 : misaligned ; shifts, tilt.	1-2, 2*cm, rad	I, 3*E



SPACECHARG	Space charge		
LMNT, model [, PRINT]	<i>LMNT</i> = 'all', 'none', or keyword ; model : 'KV', 'Gaussian' ; [optional : print out to zgoubi.SPACECHARG.out].	-, - [,-]	2*A [,A]
λ	Linear charge density	C/m	Е

SPINR	Spin rotation SCALING can be used to scale μ .	(page 139 in PART	A)
IOPT	Option	0-2	Ι
If IOPT=0	Element inactive		
Χ, Χ	Unused	2*unused	2*E
If IOPT=1	Axis and spin precession angle values.		
ϕ , μ	Angle (in (X, Y) plane) between X-axis and spin precession axis, $\phi \in [-180, 180]$; spin precession angle, $\mu \in [0, 180]$.	deg, deg	2*E
If IOPT=2	Given the spin precession axis direction, ϕ , in the horizontal plane,	the spin precession	
	angle follows a function of the Lorentz factor : $\mu(\gamma) = \left(\frac{B}{B_0}\right)^2 \times \left(\frac{B}{B_0}\right)^2$	$C_0 + \frac{C_1}{\gamma} + \frac{C_2}{\gamma^2} + \frac{C_2}{\gamma}$	$\left(\frac{\mathcal{I}_3}{\gamma^3}\right)$
$\phi, B, B_0, C_0, C_1, C_2, C_3$	Angle (in (X, Y) plane) between the X-axis and the spin precession axis; six coefficients that define the spin precession around that axis.	deg.; 6*no dim	7*E

SPNPRNL	Store spin coordinates in file FNAME	
FNAME ¹	Name of storage file (<i>e.g.</i> , zgoubi.spn)	A80
SPNSTORE	Store spin coordinates every IP other pass	
FNAME ¹ [,LABEL(s)] ²	Name of storage file (<i>e.g.</i> , zgoubi.spn) [; label(s) of the element(s) at the exit of which the store occurs (10 labels maximum)].	A80 [, 1-10*A20]
IP	Store every IP other pass (when using REBELOTE with NPASS $\geq IP - 1$).	Ι

 $^{^{1}}$ *FNAME* = 'none' will inhibit printing. 2 If first *LABEL* = 'none' then printing will be inhibited.
SPNPRT [,PRINT] [,MATRIX]

Print spin coordinates, compute spin matrix

(page 202 in PART A)

Print spin coordinates in zgoubi.res, at the location where this keyword is introduced in the structure.

A label '*PRINT*' is optional, if it appears, then local data are stored in the file zgoubi.SPNPRT.Out. That file is opened at the first occurence of *SPNPRT* and left open until **zgoubi** execution is completed.

A label '*MATRIX*' is optional, if it appears, then computation of spin rotation matrix is performed. This however assumes appropriate trajectory and spin sampling (see Sec. 6.5, p. 202).

• Example : Spin matrix

In the example below, SPNPRT followed by LABEL=MATRIX is a request for the computation of spin transport matrix of the AGS warm Siberian (an oxymoron?) snake (using its 3D OPERA field map, here). Three matrices will be computed in this example (this number is arbitrary), as OBJET defines 3 successive groups of 3 particles each, with each group its specific relative rigidity $D = \frac{B\rho}{BORO} = 1$, 0.98855, 0.090783 (typically in the AGS: extraction rigidity at $G\gamma = 45.5$, rigidity at the strongest intrinsic resonance $G\gamma = 36 + \nu_y \approx 44.98$, and injection rigidity at $G\gamma = 4.5$).

The AGS warm snake 3-D OPERA field map used here, table55.map, can be found here: https://sourceforge.net/p/zgoubi/code/HEAD/tree/trunk/exemples/AGS/snakeFieldMaps/Wsnk3D/.

```
Spin transport matrices of AGS warm Siberian snake, at 3 different energies.
 'OBJET'
                           ! This data list may be copy-pasted and run, as is.
79.366778931425273 *1D3
                                             ! Reference rigidity of the problem.
2
93
                                              ! 9 particles, 3 different momenta.
0. 0. 0. 0. 0. 1. 'o'
                          ! First 3-partile group; D=1, rigidity is BORO above.
0. 0. 0. 0. 0. 1. 'o'
0. 0. 0. 0. 0. 1. 'o'
0. 0. 0. 0. 0. 0.98855355391551 'o'
                                      ! 2nd 3-particle group, rigidity = D*BORO.
0. 0. 0. 0. 0. 0.98855355391551 'o'
0. 0. 0. 0. 0. 0.98855355391551 'o'
0. 0. 0. 0. 0. 9.078330315E-002 'o'
                                      ! 2nd 3-particle group, rigidity = D*BORO.
0. 0. 0. 0. 0. 9.078330315E-002 'o'
0. 0. 0. 0. 0. 9.078330315E-002 'o'
1 1 1 1 1 1 1 1 1
'PARTICUL'
                                  ! proton data are necessary for spin tracking.
PROTON
'SPNTRK'
4
       ! Initial spins of the 9 particles, in that order for matrix computation.
1. 0. 0.
0. 1. 0.
0. 0. 1.
1. 0. 0.
0. 1. 0.
0. 0. 1.
1. 0. 0.
0. 1. 0.
0. 0. 1.
'TOSCA'
             ! The AGS
0 20
      100. 100. 100.
1.e1
HEADER_0 wsnake
801 29 29 12 1
                                           ! The map is a 801x29x29 node 3D mesh.
                                            ! AGS warm snake 3-D OPERA field map.
table55.tab
       ! Initial spins of the 9 particles, in that order for matrix computation.
4
0 0 0 0
2
.1
2 0. .0 0. 0.
'SPNPRT' MATRIX
'END'
```

SPNTRK ¹	Spin tracking switch, and spin coordinate initialization(page 183 in PART(Spin coordinate initializations are ignored if using OBJET[KOBJ=3])		CTA)	
KSO[.KSO2], [startAt N]	KSO=0: spin tracking [switched] off ² ; $KSO=-1$: spin tracking resumes. Otherwise : as stated below; "startAt N" is a request to only start spin tracking at turn number N	-1 or 0 or 1-3 0r 4[.1] or 5	I[.J] [A I]	
If KSO = 1 – 3	KSO = 1 (respectively 2, 3) : all particles			
	have their spin automatically set to $(1,0,0)$, longitudinal (respectively $(0,1,0)$, horizontal and $(0,0,1)$, vertical)			
If KSO = 4	Repeat IMAX times (for IMAX particles in 'OBJET') the following set	equence :		
S_X, S_Y, S_Z	X, Y and Z initial components of the initial spin.	3*no dim	3*E	
If KSO = 4.1				
S_X, S_Y, S_Z	X, Y and Z components of the initial spins. These will be assigned to all particles.	3*no dim	3*E	
If KSO = 4.2	Read spins from ancillary file - UNDER DEVELOPMENT			
FNAME ³	File name		A80	
If KSO = 5	Random distribution in a cone (see figure). Enter the following two se UNDER DEVELOPMENT - TO BE COMPLETED IN spn.f.	quences :		
TO, PO $A, \delta A$	Angles of average polarization direction. A = angle of the cone around (TO, PO) ; δA = standard deviation of distribution around A	2*rad 2*rad	2*E 2*E	
IR	Random sequence seed	$\lesssim 10^6$	Ι	



Option KSO = 5: spins are distributed at random within an annular strip with standard deviation δA , centered at an angle A with respect to the axis of mean polarization (\vec{S}) defined by T_0 and P_0 .

- ² Spin tracking can be switched off at any location in zgoubi.dat data list using KSO=0, and further away resumed using KSO= -1.
- 3FNAME contains the spin components. Formatting should be has follows :

TXT, SXI, SYI, SZI, SMI,SX, SY, SZ, SM

with TXT a (arbitrary) 3-character string, SXI, SYI, SZI, SMI the initial spin components and their modulus (unused), SX, SY, SZ, SM the current spin components (these will be tracked further) and their modulus(unused).

¹ SPNTRK must be preceded by PARTICUL for the definition of G and mass.

SRLOSS	Synchrotron radiation energy loss	(page 185 in PART	A)
KSR[.i] [,PRINT] [,KSOK]	On/off switch; $i = 1$ for info output into zgoubi.SRLOSS.Out; optional, <i>PRINT</i> , anywhere beyond <i>KSR</i> : has the same effect as $i = 1$; under development: Sokolov-Ternov switch, optional (1/0 for on/off, default is off).	0 or 1[.1], - , 0 or 1	I[.I] [,A] [,I]
Next l	ine, two possibilities :		
either 1 KEYWORI	D[{LABEL1 list}] subject to SR (possibly, all KEYWORDs) :		
KWRD[{lblst}] [, STR [, List]]	Apply SR loss to a particular KEYWORD, or to $KWRD = ALL'$ or 'all', and in the former case: $\{Iblst\}=\{Ibl1, Ibl2,\}$: a list of up to 5 LABEL1s to which this applies; STR, optional: STR = 'scale' will scale fields following energy loss, List: a list of up to 10 keywords to which this scaling applies.		A[1-5A] [,A [,1-10A]]
or, up to 10 keyword	ls (no LABEL1 ist in that case) subject to SR :		
KWRD1 [, KWRD2 [, KWRD3]] [, STR [, List]]	A list of up to 10 KEYWORDs to apply SR loss to ; STR, ptional : STR = 'scale' will scale fields following energy loss, List : a list of up to 10 keywords to which this scaling applies.		1-10A [,A [,1-10A]]
Option, seed	Option = 0 or 1 : SR causes dp only ; Option = 2 : SR causes both dp and angle kick (under development).	$1 - 3, > 10^5$	I1, I6

SRPRNT

SVDOCSVD orbit correctionUNDER DEVELOPEMENT - Feb. 2019

 LABEL1 [,LABEL2, [...]]
 The N label(s) at which beam data are to be computed/recorded.
 N string(s)
 N*A20

 If some "LABELi" in this list actually does not appear
 in zgoubi.dat optical sequence, then it is peacefully ignored ;
 wild card accepted, in the form '*LABEL' or 'LABEL*' or '*LABEL*'.
 N*A20

SYNRAD	Synchrotron radiation spectral-angular densities		
KSR	Switch 0 : inhibit SR calculations 1 : start 2 : stop	0-2	Ι
If KSR = 0			
<i>D</i> 1, <i>D</i> 2, <i>D</i> 3	Dummies		3*E
If KSR = 1			
X0, Y0, Z0	Observer position in frame of magnet next to SYNRAD	3*m	3*E
If KSR = 2			
ν_1, ν_2, N	Frequency range and sampling	2*eV, no dim	2*E, I

Keywords and input data formatting

SYSTEM	System call		
NCMD	The number of calls to follow.	≥ 0	I

NCMD lines follow, one command per line.

• Example : SYSTEM

The first occurence of the command (top region in the data list below) allows establishing links from remote folders to the current one (the one in which **zgoubi** is presently run). These folders happen to contain files appearing in the *SCALING* command, as well as OPERA field maps of the siberian snakes used in subsequent *TOSCA* commands.

The second occurence of the command (bottom region in the data list below) allows saving zgoubi.res output file as resulting from the **zgoubi** run, under a different name.

```
AGS, polarized protons. 2 snakes. t = 145 ms.
'GETFITVAL'
fitVals.data
'OBJET' LBL_OBJFit
7069.3668040036146
5
.01 .01 .01 .01 0. .0001
0. 0. 0. 0. 0. 1.
'FAISCEAU'
                            ' o'
'SYSTEM'
ln -sf /rap/lattice_tools/zgoubi/AgsZgoubiModel/snakeFieldMaps/TOSC3D/Csnk3D .
   -sf /rap/lattice_tools/zgoubi/AgsZgoubiModel/snakeFieldMaps/TOSC3D/Wsnk3D
CALING' LBL_SCLfit
'SCALING'
1 1/
AGSMM *AF *BF *CF !# of params 2Bchanged. dB0 (FIT#3) dB1 (FIT#4) dB2
-1 3 13 3E-20 14 -1.473595E-03 15 8.01942
-1 3
1.00000000 ! (FIT #6)
AGSMM *AD *BD *CD !# of params 2Bchanged. dB0 (FIT#9) dB1 (FIT#10)
                                                                              dB2
                                                          14 -1.011857E-03 15 -1.70597
                                              13 9E-20
-1 3
1.000000 ! (FIT#12)
1
AGSQUAD QH_* !# of params 2Bchanged. (FIT#15)
−1 1 15 0.0
1.000000
AGSQUAD QV_* QP_*
                         !# of params 2Bchanged. (FIT#15)
1 15 0.0
1.000000
MULTIPOL QJUMP_*
7.06936680E+00
MULTIPOL COH1
./Csnk3D/Hlx68.2_Sol42.3/CHREF_+_dipolCORR.scal
MULTIPOL COV1
1.10
./Csnk3D/H1x68.2_So142.3/CHREF_+_dipolCORR.scal
MULTIPOL COH2
1.10
 ./Csnk3D/H1x68.2_So142.3/CHREF_+_dipolCORR.scal
MULTIPOL COV2
1.10
./Csnk3D/H1x68.2 Sol42.3/CHREF + dipolCORR.scal
MULTIPOL WOH1
1.10
./Csnk3D/H1x68.2_Sol42.3/CHREF_+_dipolCORR.scal_51.8_0.0
MULTIPOL WOV1
1.10
./Csnk3D/H1x68.2_So142.3/CHREF_+_dipolCORR.scal_51.8_0.0
MULTIPOL WOH2
1.10
./Csnk3D/H1x68.2_So142.3/CHREF_+_dipolCORR.sca1_51.8_0.0
MULTIPOL WOV2
1.10
./Csnk3D/H1x68.2 Sol42.3/CHREF + dipolCORR.scal 51.8 0.0
CHANGREE WONKE
1.12
//Csnk3D/H1x68.2_Sol42.3/CHREF_+_dipolCORR.scal_51.8_0.0
1 1 1 3
CHANGREF WSNKO
./Csnk3D/H1x68.2_Sol42.3/CHREF_+_dipolCORR.scal_51.8_0.0
CHANGREF CSNKE
 ./Csnk3D/Hlx68.2_Sol42.3/CHREF_+_dipolCORR.scal
1 1 1 3
CHANGREF CSNKO
```

• Example : SYSTEM

An additional example can be found page 274

TOSCA2-D and 3-D Cartesian or cylindrical mesh field map (page 140 in PART A)	
dim. data type	FIT num.
<i>IC</i> , <i>IL</i> IC = 1, 2: print the map $IL = 1, 2[\times 10^n], 7$: print coordinates, fields, etc., step-by-step, in zgoubi.res (1), zgoubi.plt (2), zgoubi.impdev.out (7). 0-2; 0-2[×10^n], 7 2*I	1, 2
BNORM, XN, YN, ZNField and X-,Y-,Z-coordinate unit conversion coefficients.4*UnitConv.4*EConvert values as read from map file, to kG and cm or rad.	10-13
TITLTitle. Include "FLIP" to get field map X-flipped.A80Include "HEADER n" if FNAME starts with $n \ge 1$ header lines.Include "ZroBXY" to force $B_X = B_Y = 0$ at all Z=0 (only applies for MOD=15 and MOD=24).Include "RHIC_helix" to normalize BNORM to measured value ¹ ; in that case, if SCALING[TOSCA] is used, sign(BNORM*SCAL)==sign(BNORM) [field sign is independent of sign(SCAL)].	
$IX, IY, IZ, ^2$ Number of nodes of the mesh in the X, Y and Z directions, $\leq MXX, \leq MXY,$ $3*I, I[.$ $MOD[.MOD2 [, a(i),i=$ $IZ = 1$ for a 2-D map ; MOD and $MOD2$: field map style, see $\leq IZ, [0-22.1-9], -$ [, MOD $1,MOD2]]$ table next page ; $a(i = 1, MOD2)$ are the field normalisation factors. $*E]$	[20-24 2 [, 25-27]
Next NF lines :Map file name(s), one line per name.A80 $FNAME^3$ If $MOD=0$: $NF = 1 + [IZ/2]$, the NF 2-D maps are for $0 \le Z \le Z_{max}$, they are symmetrized with respect to the $Z(1) = 0$ plane.If $MOD=1$: $NF = IZ$, no symmetry assumed ; $Z(1) = Z_{max}$, $Z(1 + [IZ/2]) = 0$ and $Z(NF) = -Z_{max}$. If $MOD=12$: a single FNAME file contains the all 3-D volume. $MOD=15$, 20-22, etc. : see table page 335	
$ID, A, B, C [, A', B', C']$, Integration boundary. Ineffective when $ID = 0$. $\geq -1, \text{ cm}, I,3^*E [$ $A'', \text{ etc., if } ID \geq 2]$ $ID = -1, 1 \text{ or } \geq 2$: as for CARTEMES $2^*\text{no dim } [,idem]$ $3^*E, \text{etc.}$, 30-33 [, c.] 34-36,]
IORDREIf $IZ = 1: 2, 25 \text{ or } 4 \text{ as in CARTEMES}$; unused if $IZ \neq 1.$ 2, 25 or 4I	40
XPAS Integration step cm E	50
If Cartesian mesh (see MOD) : <i>KPOS</i> , <i>XCE</i> , <i>YCE</i> , <i>ALE KPOS</i> =1 : element aligned, 2 : misaligned ; shifts, tilt 1-2, 2*cm, rad I, 3*E If nolar mesh :	60-63
KPOSAs for POLARMES. Normally 2. $1-2$ IIf KPOS = 2 :cm, rad, cm, rad $4*E$	60 70-73

¹B field along RHIC Snake helix versus helix current, normalized to field measurements or not, is managed in program toscac.f.

 ^{1}MXX , MXY, IZ may be changed, they are stated in the include file PARIZ.H.

²Case of 2-D field maps : Each file FNAME(K) contains the field specific to elevation Z(K) and must be formatted according to the following FOR-TRAN read sequence (that usually fits TOSCA code OUTPUTS - details and possible updates are to be found in the source file ' fmapw.f':

```
DO JF = 1, NF
   \label{eq:constraint} \begin{split} D(J) &= 1, NF \\ OPEN (UNT = NL, FILE = FNAME(JF), STATUS = 'OLD' [,FORM='UNFORMATTED']) \\ DO &= 1, JY ; DO &= 1, IX \\ READ(NL,*) Y(J), Z(JF), X(I), BY(J,I), BZ(J,I), BX(J,I) \\ ENDDO ; ENDDO ; NL = NL + 1 \end{split}
                                                                                                                                                                                                                                                     node coordinates, field components at node
  ENDDO
BX and BY are assumed zero at all nodes of the 2-D mesh, regardless of BX(J,1,I), BY(J,1,I) values.
Case of 3-D field maps :
  DO JF = 1, NF
OPEN (UNIT = NL, FILE = FNAME(JF), STATUS = 'OLD' [,FORM='UNFORMATTED'])
DO J = 1, JY; DO K = 1, KX ; DO I = 1, IX
READ(NL*) Y(J), Z(K), X(I), BY(J,K,I), BZ(J,K,I), BX(J,K,I)
ENDDO; ENDDO ; ENDDO
NL = NL + 1
```

ENDDO

node coordinates, field components at node

• Example : RHIC Siberian snake module, using, or not, "RHIC_helix" flag.

The two *TOSCA* input data lists below are equivalent, they provide quasi-identical fields. The left one features "RHIC_helix" as part of the field map "*TITL*" (which normalizes the OPERA field to the input current BNORM (Amps) using measured field versus current data); the right one does not - this is the origin of a very small difference in the field along the helix [70].

Incidentally: these two jobs perfom a centering of the helical motion along the helix (that's the *FIT* constraint), finding the optimal initial vertical trajectory coordinate (*FIT* variable). They end up with a computation of the spin matrix transport along that trajectory. The field map used can be found in zgoubi repository, at

https://sourceforge.net/p/zgoubi/code/HEAD/tree/trunk/exemples/RHIC/3DSnakes/fieldMaps/

RHIC Siberian snake low field module. 'OBJET' \$53.71244451829796e3 ! E=255 GeV.	RHIC Siberian snake low field module. 'OBJET' 853.71244451829796e3 ! E=255 GeV.
1 1	1 3 11111 ! Spin matrix computation requires sets (only 1 here) 0. 0. 0. 0. 0. 0. 0. . 0. 00.21589188 0. 0.00 1.
'PARTICUL' PROTON 'SPNTRK' 4 1. 0. 0. ! Spin vectors for each particle of a 3-set. 0. 1. 0.	'PARTICUL' PROTON 'SPNTRK' 4 1. 0. 0. ! Spin vectors for each particle of a 3-set. 0. 1. 0. 0. 0. 1.
'TOSCA' high_normalized 0 2 -322. 1. 1. 1. 1. ! BNORM is a currnt, is Amps, here. HEADER_6 RHIC_helix 361 81 81 15.1 0.246305418719e-4 ! = 1/4.060e4 b_model3a2a322a-x-4_4_y-4_4_z-180_180-integral.table 0 0 0 0 0 2 .1 2 0.0000000E+00 0.0000000E+00 0.0000000E+00	<pre>'TOSCA' high_B_notNormalized 0 2 -1.E-03 1. 1. 1. ! Normalize data read from map: B to kG, and X, Y, Z to cm. HEADER_8 10 "RHIC_helix" here!! 361 81 81 15.1 1. b_model3a2a322a-x-4_4_y-4_4_z-180_180-integral.table 0 0 0 0 0 2 .1 2 0.00000000E+00 0.0000000E+00 0.0000000E+00</pre>
<pre>'FIT' 1 1 42 0 [-3,3] 1 1D-10 7.3 1 4 4 0.1.0 ! min(Z)+max(Z) =0 in element 4=helix -> vertical centering</pre>	'FIT' 1 nofinal 1 42 0 [-3,3] 1 1D-10 3.2 1 4 #End 0. 1. 0 ! Z_final + Z_0 = 0: this centers the helical trajectory.
'SPNPRT' MATRIX PRINT 'END'	'SPNPRT' MATRIX PRINT 'END'

• The various IZ, MOD and MOD2 possibilities, when using TOSCA.

IZ : number of nodes of the *complete* field map along the Z direction (IZ=1 for 2-D) MOD, MOD2 : determine the coordinate system, symmetries, reading format and column sequence, etc. NF : number of field map input data files to be declared. Always include mid-plane map. Expected columns : formatting of the coordinates and field data columns in the field map data file(s) 'Exemple' example folder : examples of zgoubi runs using field maps can be found in the subfolders of zgoubi-code/exemples/KEYWORDS/TOSCA/cartesian (case MOD≤19) or zgoubi-code/exemples/KEYWORDS/TOSCA/cylindrical (case MOD≥20).

The rightmost column below indicates the subfolder of concern, following (IZ, MOD, MOD2) options of interest.

MOD	< 19 :	Cartesian	mesh
	_		

IZ	MOD	.MOD2		NF	Expected columns	Example folder
1	0, 1	none or .1, .2, .3	2-D map. File contains $B_Z(X, Y) _{Z=0}$, mid-plane antisymmetry assumed. Several different reading formats (see fmapw.f/fmapr3).	1	Y, Z, X, BY, BZ, BX	IZ-MODMOD2_1-0-none/ (GSI KAOS spectrometer)
1	3	none or .1	2-D map. Used for AGS main magnet. If MOD2=1, $B_Z(X, Y, Z = 0)$ field is perturbed by $(1 + n_1 Y + n_2 Y^2 + n_3 Y^3)$ factor.	1	Special - see example	AGS/usingMainMagnetsMaps (AGS with main magnet maps)
1	15	.1 – .4	2-D map. Up to 4 files to be combined linearly into a new map : field at all node of new map is $\vec{B} = \sum_{i=1}^{i=MOD2} a_i \vec{B}_i$. Mid-plane antisymmetry is assumed : each file has to contain $B_Z(X, Y, Z = 0)$.	1 to 4	Y, Z, X, BY, BZ, BX	IZ-MODMOD2_1-1514 (EMMA FFAG cell)
>1	0	none	3-D map. Files span upper half of magnet, one per $(X,Y) _{0 \le Z \le Z_{max}}$ plane including median plane, mid-plane antisymmetry assumed.	1+IZ/2	Y, Z, X, BY, BZ, BX	IZ-MODMOD2_gt1-0-none/ (GSI KAOS spectrometer)
odd, ≥ 3	1	none	3-D map. Files span full magnet volume, one file per (X,Y) plane, no symmetry assumed.	IZ	Y, Z, X, BY, BZ, BX	IZ-MODMOD2_gt1-1-none/ (AGS warm helix snake)
>1	12	none	3-D map. Single file, upper half of magnet, mid-plane antisymmetry assumed.	1		
>1	12	.1	3-D map. Single file, whole magnet volume, no symmetry assumed.	1	Y, Z, X, BY, BZ, BX	IZ-MODMOD2_gt1-121/ (AGS warm helix snake)
>1	12	.2	3-D map. Single file, 1/8th of the magnet, symmetry wrt. $(X, Y)_{Z=0}, (X, Z)_{Y=0}, (Y, Z)_{X=0}$ planes.	1		
odd, ≥ 3	15	.1 – .4	3-D map. Up to 4 files to be combined linearly into a new map, field at all node of new map is $\vec{B} = \sum_{i=1}^{i=MOD^2} a_i \vec{B}_i$. Each file has to contain $B_{X,Y,Z}(X, Y, Z)$ data over <i>IZ</i> equally <i>Z</i> -spaced (<i>X</i> , <i>Y</i>) planes (no symmetry assumed).	1 to 4		
odd, ≥ 3	16	.1 – .4	3-D map. Fields from up to 4 maps to be combined linearly into a new field value at particle location, $\vec{B} = \sum_{i=1}^{i=MOD2} a_i \vec{B}_i$. Each file has to contain $B_{X,Y,Z}(X, Y, Z)$ data over <i>IZ</i> equally <i>Z</i> -spaced (X, Y) planes.	1 to 4	UNDER DEVELOPMENT	
MOD 2	≥ 20 : Cyli	ndrical mesh				
IZ	MOD	.MOD2				
1	25	.1 – .4	2-D map. Up to 4 files to be combined linearly into a new map : at all node of new map $\vec{B} = \sum_{i=1}^{i=MOD2} a_i \vec{B}_i$. Each file contains mid-plane $B_Z(X, Y, Z = 0)$ data, mid-plane antisymmetry is assumed.	1 to 4	Y, Z, X, BY, BZ, BX	IZ-MODMOD2_1-1514 (EMMA FFAG cell)
>1	20, 21		3-D map. Single file. MOD=20 : $1/4$ magnet, cylindrical symmetry with respect to (Y,Z) plane and antisymmetry wrt (X,Y) plane. MOD=21 : another type of symmetry (to be documented - see fmapw.f).	1	$Y(r, \theta), Z, X(r, \theta),$ BY, BZ, BX	IZ-MODMOD2_gt1-20 (KEK 150 MeV FFAG)
odd, ≥ 1	22, 23	.1 – .4	2-D or 3-D map. Mid-plane antisymmetry assumed. Up to 4 files can be combined linearly into a new one; each file is $Z \ge 0$ half-magnet. Field at all node of new map is $\vec{B} = \sum_{i=1}^{i=MOD2} a_i \vec{B}_i$. Each file has to contain $B_{X,Y,Z}(X, Y, Z)$ data over (<i>IZ</i> +1)/2 equally <i>Z</i> -spaced (<i>X</i> , <i>Y</i>) planes. MOD=23 : special, test code (see fmapw.f).	1 to 4	$\begin{split} \mathbf{Y}(r,\theta) &= r\cos\theta, \mathbf{Z}, \\ \mathbf{X}(r,\theta) &= r\sin\theta, \\ \mathbf{BY}, \mathbf{BZ}, \mathbf{BX} \end{split}$	IZ-MODMOD2_gt1-2214 (ERIT FFAG)
odd, ≥ 3	24		3-D map, full volume. No symmetry assumed. The file contains $B_{X,Y,Z}(X, Y, Z)$ data over <i>IZ</i> equally <i>Z</i> -spaced (X, Y) planes.	1	$\theta, R, Z, B_{\theta}, BR, BZ$	

TRANSMAT	Matrix transfer		
IORDRE	Transport matrix order	1-2	Ι
XL	Length (ineffective, for updating)	m	E
For $IA = 1, 6:$			
R(IA, IB), IB = 1, 6	First order matrix	m, rad	6 lines
If IORDRE = 2	Following records <i>only</i> if $IORDRE = 2$		6*E each
T(IA, IB, IC),	Second order matrix, six 6*6 blocks	m, rad	36 lines 6*E each

TRAROTTranslation-RotationTX, TY, TZ,
RX, RY, RZTranslations, rotations3*m, 3*rad6*E

TWISS 1**Compute periodic optical parameters. Log to zgoubi.TWISS.out** (page 204 in PART A)
Hint: use FIT preceding TWISS for closed orbit search in case the latter is not known.KTWKTW = 0/1/2/3 : Off / as MATRIX / add computation of
0-3 2*anyI1 2*E [A]

$\mathbf{K} \mathbf{I} \mathbf{W},$	K I W = 0/1/2/3: OII / as MATRIX / and computation of	0-5, 2 ⁺ any	$\Pi, Z^{*}E[,A]$
FacD, FacA	chromaticities / add computation of anharmonicities. Chromatic	[,coupled]	[,A] [,A]
[, SRINT] [, DKINT]	orbits are at FacD \times D = B ρ /BORO, with D the momentum	[, SRINT]	
	sampling in OBJET; FacA: unused;	[, DKINT]	
	presence of "SRINT" will cause computation of SR integrals ² ;		
	presence of "DKINT" will cause computation of Derbenev-Kondraten	0	

spin integrals³.

¹*TWISS* may be preceded by *FIT*[2], this allows finding the on- and off-momentum closed orbits prior to computation of respectively on- and off-momentum transport matrices, see example page 339. Prior *FIT*[2] may also find the stable spin precession direction, useful for instance if *DKINT=1* as computation of Derbenev-Kondratenko integrals requires \vec{n}_0 along closed orbit.

 2 Synchrotron radiation integrals are computed along particle number 1 trajectory, it is the responsibility of the user to ensure that particle number 1 is on the closed orbit, for instance using *FIT*[2].

 3 Derbenev-Kondratenko spin integrals are computed along particle number 1 trajectory, it is the responsibility of the user to ensure that (i) particle number 1 is on the closed orbit, (ii) its initial spin coordinates in *SPNTRK* are on the spin closed orbit.

• Example : orbit finding using FIT, followed by a TWISS procedure

"*KTW=2*" under *TWISS*, in the data sequence below, will cause 4 successive passes through the optical sequence, with the following purposes:

- pass 1: compute the on-momentum 4×4 transport matrix $[T_{ij}]$ and, if the sequence is optically stable, deduce the periodic beam matrix $\sigma = I \cos \mu + J \sin \mu \equiv [T_{ij}]$

- pass 2 and 3: repeat for off-momentum matrices $[T_{ij}](\pm \frac{dp}{n})$,

- pass 4: transport the on-momentum matrix through the sequence using $\sigma(s) = [T_{ij}] \sigma(s = 0) [\tilde{T}_{ij}]$, compute chromaticities, etc., print out outcomes to zgoubi.TWISS.out and zgoubi.res.

These 4 passes will result in

(i) the delivery of zgoubi.TWISS.out file, formatted in a similar form to MADX's twiss output, namely,

- a header with global parameters (sequence length, tunes, chromaticities, max- β 's, etc.)
- a listing of periodic orbit, optical functions and other data, along the structure ;

(ii) a print out to zgoubi.res of

- the on-momentum matrix of the optical structure,

- off-momentum matrices at $\frac{dp}{p} = \pm FacD * dD$, with dD the momentum sampling defined by OBJET[KOBJ=5]

(page 297),

- Twiss parameters at the end of the structure, in the case of a stable periodic structure,

- momentum compaction, chromaticities, etc.

In the following example, the *FIT* instruction which precedes *TWISS* first finds the orbit (on-momentum at the first pass, $\pm dp/p$ chromatic orbits at passes 2 and 3 respectively) which will then be the reference trajectory in *OBJET[KOBJ=5]*, in generating the 13 sample rays necessary for computation of the transport matrix.

```
'OBJET'
20015.55
                               ! Rigidity (kG.cm) for 6 GeV electrons.
                               ! Generate an 13 particle set. Normally used for MATRIX or TWISS computation.
.001 .01 .001 .01 0. .0001
                               ! Coordinate sampling for MATRIX computation : dY, dT, dZ, dP, ds (unused) and dD.
0. 0. 0. 0. 0. 1.
                               ! Coordinates of the reference orbit: Y- ,T- ,Z- ,P-, s- (unused) and D-ref,
                               ! these are the coordinates of particle number 1 of the 13-particle set.
'INCLUDE'
1
./myOpticalSequenceFile[fromHere:toThere]
'FIT'
4
                            ! 4 variables.
1 30 0 [-1.,1.]
                            ! vary Y0 of reference particle (i.e., particle number 1 of the 13-set)
1 31 0 [-1.,1.]
1 32 0 [-1.,1.]
1 33 0 (-1.,1.]
                            ! vary TO of reference particle (i.e., particle number 1 of the 13-set)
                             ! vary ZO of reference particle (i.e., particle number 1 of the 13-set)
1 33 0 [-1.,1.]
                            ! vary PO of reference particle (i.e., particle number 1 of the 13-set)
                            ! 4 constraints; penalty value is default 1e-10.
                           ! particle 1: Y0 initial = Y final
! particle 1: T0 initial = T final
! particle 1: Z0 initial = Z final
3.1 1 2 #End 0. 1. 0
3.1 1 3 #End 0. 1. 0
3.1 1 4 #End 0. 1. 0
3.1 1 5 #End 0. 1. 0
                           ! particle 1: P0 initial = P final
'FAISCEAU'
'TWISS'
2 1. 1.
                            ! KTW = 2, FacD = 1
 'END'
```

UNDULATOR Undulator magnet

Under development, to be documented

UNIPOT	Unipotential electrostatic lens		
IL	$IL = 1, 2[\times 10^n], 7$: print coordinates, fields, etc., step-by-step, in zgoubi.res (1), zgoubi.plt (2), zgoubi.impdev.out (7).	0-2[×10 ^{<i>n</i>}], 7	Ι
X_1, D, X_2, X_3, R_0	Length of first tube ; distance between tubes ; length of second and third tubes ; radius	5*m	5*E
V_1, V_2	Potentials	2*V	2*E
XPAS	Integration step	cm	Е
KPOS, XCE, YCE, ALE	KPOS=1 : element aligned, 2 : misaligned ; shifts, tilt.	1-2, 2*cm, rad	I, 3*E



VENUS	Simulation of a rectangular dipole magnet		
IL	$IL = 1, 2[\times 10^n], 7$: print coordinates, fields, etc., step-by-step, in zgoubi.res (1), zgoubi.plt (2), zgoubi.impdev.out (7).	$0-2[\times 10^n]$, 7	Ι
XL, YL, B_0	Length ; width = $\pm YL$; field	2*cm, kG	3*E
XPAS	Integration step	cm	Е
KPOS, XCE, YCE, ALE	KPOS=1 : element aligned, 2 : misaligned ; shifts, tilt.	1-2, 2*cm, rad	I, 3*E



A scheme of a few trajectories through VENUS rectangular dipole.

VFFA

To be documented. Examples, including input data files, are available at

https://sourceforge.net/p/zgoubi/code/HEAD/tree/trunk/exemples/FFAG/VFFA/

2	1	Λ
3	4	4

WIENFILT ¹	Wien filter	(page 150 in PART	A)
IL	$IL = 1, 2[\times 10^n], 7$: print coordinates, fields, etc., step-by-step, in zgoubi.res (1), zgoubi.plt (2), zgoubi.impdev.out (7).	$0-2[imes 10^n]$, 7	Ι
XL, E, B, HV	Length ; electric field ; magnetic field ; option : element inactive $(HV = 0)$ horizontal (HV = 1) or vertical $(HV = 2)$ separation	m, V/m, T, 0-2	3*E, I
$X_{\mathrm{E}}, \lambda_{E_{E}}, \lambda_{B_{E}}$	Entrance face : Integration zone extent ; fringe field extents, E and B respectively (\simeq gap height)	3*cm	3*E
$C_{E0} - C_{E5}$ $C_{B0} - C_{B5}$	Fringe field coefficients for E Fringe field coefficients for B	6*no dim 6*no dim	6*E 6*E
$X_S, \lambda_{E_S}, \lambda_{B_S}$ $C_{E0}-C_{E5}$ $C_{B0}-C_{B5}$	Exit face : See entrance face	3*cm 6*no dim 6*no dim	3*E 6*E 6*E
XPAS	Integration step	cm	Е
KPOS, XCE, YCE, ALE	KPOS=1 : element aligned, 2 : misaligned ; shifts, tilt.	1-2, 2*cm, rad	I, 3*E

YMY F

Reverse signs of Y and Z reference axes

(page 151 in PART A)

Equivalent to a 180° rotation with respect to X-axis



The use of YMY in a sequence of two dipoles of opposite signs.

PART C

Examples of input data files and output result files

INTRODUCTION

Several examples of the use of **zgoubi** are given here. They show the contents of the input and output data files, and are also intended to help understanding some subtleties of the data definition.

Example 1: checks the resolution of the QDD spectrometer SPES 2 of SATURNE Laboratory [76], by means of a *Monte Carlo initial object* and an *analysis of images* at the focal plane with histograms. The *measured field maps* of the spectrometer are used for that purpose. The layout of SPES 2 is given in Fig. 55.

Example 2: calculates the *first and second order transfer matrices* of an 800 MeV/c kaon beam line [77] at each of its four foci: at the end of the first separation stage (vertical focus), at the intermediate momentum slit (horizontal focus), at the end of the second separation stage (vertical focus), and at the end of the line (double focusing). The first bending is represented by its *3-D map* previously calculated with the TOSCA magnet code. The second bending is simulated with *DIPOLE*. The layout of the line is given in Fig. 56.

Example 3: illustrates the use of MCDESINT and REBELOTE with a simulation of the in-flight decay

$$K \longrightarrow \mu + \nu$$

in the SATURNE Laboratory spectrometer SPES 3 [43]. The angular acceptance of SPES 3 is ± 50 mrd horizontally and ± 50 mrd vertically; its momentum acceptance is $\pm 40\%$. The bending magnet is simulated with *DIPOLE*. The layout of SPES 3 is given in Fig. 57.

Example 4: illustrates the operation of *the fitting procedure*: a quadrupole triplet is tuned from -0.7/0.3 T to field values leading to transfer coefficients R12=16.6 and R34=-.88 at the end of the beam line. Other example can be found in [78].

Example 5: shows the use of the *spin and multi-turn tracking procedures*, applied to the case of the SATURNE 3 GeV synchrotron [8, 11, 79]. Protons with initial vertical spin ($\vec{S} \equiv \vec{S}_Z$) are accelerated through the $\gamma G = 7 - \nu_Z$ depolarizing resonance. For easier understanding, some results are summarized in Figs. 59, 60 (obtained with the graphic post-processor **zpop**, see Part D).

Example 6: shows *ray-tracing through a micro-beam line* that involves *magneto-electrostatic quadrupoles* for the suppression of second order (chromatic) aberrations [7]. The extremely small beam spot sizes involved (less than 1 micrometer) reveal the high accuracy of the ray-tracing (Figs. 61).

Many more examples can be found on the **zgoubi** development web site [6].

Examples

1 MONTE CARLO IMAGES IN SPES 2

Former Saclay/SATURNE and CERN QDD mass spectrometer [76].



Figure 55: SPES 2 Layout.

zgoubi data file.

SPES2 QDD SPECTROMETER, USING FIELD MAPS; MONTE-CARLO OBJECT WITH MOMENTUM GRID. 'MCOBJET' 1
2335. REFERENCE RIGIDITY.
2 DISTRIBUTION IN GRID.
10000 NUMMER OF PARTICLES.

2 10000 1 1 1 1 1 1 0. 0. 0. 0. 0. 1. 1 1 1 1 5 0. 0. 0. 0. 0. 0.101 0. 50.e-3 0. 50.e-3 0. 0. 1. 1. 1. 1. 1. 1. 9 9. 9. 9. 186387 548728 472874 //HSGYC	DISTRIBUTION IN GRID. NUMBER OF PARTICLES. UNIFORM DISTRIBUTIONS CENTRAL VALUES OF BARS. NUMBER OF BARS IN MOMENTUM SPACE BETWEEN MOMENTUM BARS. WIDTH OF BARS. SORTING CUT-OFFS (UNUSED) FOR P(D) (UNUSED) SEEDS.
1 .997 1.003 80 1 20 'D' 1 'Q' 'HISTO'	HISTO OF D.
3 -60. 60. 80 1 20 'T' 1 'Q' 'HISTO'	HISTO OF THETA0.
5 -60. 60. 80 1 20 'P' 1 'Q' 'DRIFT'	HISTO OF PHIO.
41.5	
0 0	IC IL.
96136E-3 1. 1.	BNORM, XNorm, YNorm
++++ CONCORDE ++++ 39 23	IX IY.
concord.map	field map file name, quadrupole
0 0 0 0	NO LIMIT PLANE.
2.5	XPAS.
2 0 0 0	KPOS.
'DRIFT'	
'CHANGREF'	POSITIONING OF THE
0. 32.5 -35.6	1-ST BENDING.
CARTEMES'	
1.04279E-3 1. 1.	
++++ A1 ++++	
117 52	field man file name finch divel
a1.map 0 0 0 0	field map file name, first dipole
2	
2.5	
2 U U U 'CHANGREF'	POSITIONING OF THE
028.65 -27.6137	EXIT FRAME.
'DRIFT'	
33.15 'CHANGREF'	POSITIONING OF THE
0. 27.5 -19.88	2-ND BENDING.
'CARTEMES'	
1.05778E-3 1. 1.	
++++ A2 ++++	
132 80	
a2.map	field map file name, second dipole
2	
2.5	
∠ U U U 'CHANGREF'	POSITIONING OF THE
418121.945	EXIT FRAME.
'DRIFT'	
3.55 'HISTO'	HISTO OF Y
25 2. 80 1	SHOWS THE RESOLUTION
20 'Y' 1 'Q'	OF THE SPECTROMETER.
'END'	

Excerpt from zgoubi.res : histograms of initial beam coordinates.

******	************* HISTO	******	******	*******	*****	*****
		HISTOGRAMME	DE LA COOR	DONNEE D		
		PARTICULES F	PRIMAIRES ET	SECONDATE	275	
		DANS LA FEN	VETRE : 0.9	970 /	1.003	
		NORMALISE		5,0 ,	1.000	
		HOIGHIELOE				
20						
19						
18						
17		D	D	D	D	D
16		- D	D	D	- D	D
15		- D	D	D	- D	D
14		D	D	D	D	D
13		- D	D	D	- D	D
12		D	D	D	- D	D
11		D	D	D	D	D
10		0	0	0	0	0
9		D	D	D	D	D
8		D	D	D	D	D
7		D	D	D	D	D
6		D	D	D	D	D
5		D	D	D	D	D
1		D	D	D	D	D
3		D	D	D	D	D
2		D	D	D	D	D
1		D	D	D	D	D
T	122456700	01224567000123	D 2456700012245	67000122466	C70001224E670001	22456700012245670001
	123430783	0123430709012.	A20102012242	67890123430	2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2	23430703012343070301
		2 5	4	5	0 /	8 5
	TOTAL COMDEN	CE	. 100	0.0 010 1.0	2000	
	NUMERO DU	CANAL MOVEN	. 100	-00 30K 10	5000	
	COMPERCE NU	CANAL MOIEN	:	20		
	UNI DUVC NU		: 20	30		
	VAL. PHIS. AU		: 1.00	0		
	RESOLUTION P	AK CANAL	: /.JU	UE-U		
	PARAMEIRES P	HISIQUES DE	LA DISIRIBU	TION :		
		MIN 0 000	LUUUUU PARIIC	1 002	MAN MAN A	00000 03
		MIN = 0.9980	, MAX =	1.002	, $MAX-MIN = 4$.	0000E-03
		MOTENNE = 1	1.000			
		SIGMA = 1.41	LU6E-03			
TDAT 1		0 + i	0 0000 0 00	0 20 24	0 000 44 62	0 0000 0 0000
IRAJ I	1EA, D, 1, 1, 2, P	,s,time : i	0.9980 0.00	0 -30.24	0.000 44.65	0.0000 0.0000
******	UTOTO	***********	***********	*********	*****	* * * * * * * * * * * * * * * * * * * *
2	H1310					
		UTOTOCDANNE	DE 13 0000	DONNER TH		
		DADTICUIDO	DE LA COUP	DONNEE THE	SIA	
		PARIICULES P	IDTDD . CO	SECONDAIP	CO 00 (MD	B 1
		DANG LA FEI	NITCE OU	.00 /	00.00 (III	5)
		NORM	ALISE			
2.0						
20						
19						
17						т
16		T		т	т	
1 5		- T T T	TT	т т	1 T T T T T	+ TT TT
10			11	1 1 m mmmma		
14			1111 11	I IIIII		
10	1					
12	1					
11	11	111111111111111				
10	00	000000000000000000000000000000000000000		000000000000	000000000000000000000000000000000000000	
9	11			111111111111		
8	11			111111111111		
	11			111111111111		
0	11					
C A	11	11111111111111		111111111111		
4	11	11111111111111		111111111111		
3	TT	111111TTTTTTTTTTTTT	LIIIIITTTTTTTTT	IIIIIIIIIII	LIIIIIIITTTTTTTTTTTTTTTT	IIIIIIIIIITT
2	11	····		TTTTTTTTTTTTTTTTTTTTTTTTTTTTTTTTTTTTTT		
1	11	1111111111111111		111111111111		1111111111111
	122456700	01234567000101	3456780010245	67890122454	5789012345679001	23456780012245670001
	123430/89	2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2	/10/03U12345 /	5 c c c c c c c c c c c c c c c c c c c	6 7	23430/050123430/0901
		د <u>ع</u>	4	U.	u /	o 9
	TOTAL COMPENS	CP	. 100	0.0 0110 1.0	2000	
	NUMERO DI	CANAL MOUTH		SUK IL		
	COMPTAGE 21	CANAL MUIEN		20		
	COMPIAGE AU		: 1	20		
	VAL. PHYS. AU		: 3.33	1E-15 (MRD)		
	RESOLUTION P	AK CANAL	: 1.5	u (MRD)	1	
	D. D. D. M.					
	FARAMETRES P	HISIQUES DE	LA DÍSTRIBU	TION :		
		COMPTAGE =]	LUUUU PARTIC	ULES 00		
		milin = -49.99	, MAX =	50.00	, MAA-MIN = 9	2.20 (PIKD)

MOYENNE = 0.3320 (MRD) SIGMA = 29.04 (MRD) TRAJ 1 IEX,D,Y,T,Z,P,S,time : 1 0.9980 0.000 -30.24 0.000 44.63 0.0000 0.0000

******	****
4	HISTO
	HISTOGRAMME DE LA COORDONNEE PHI PARTICULES PRIMAIRES ET SECONDAIRES DANS LA FENETRE : -60.00 / 60.00 (MRD) NORMALISE
20 19 18	
17	
16	P P P P PPPP PPPP PPP PPP PPP PPP P
14	PERF FFF FFFFFFFFFFFFFFFFFFFFFFFFFFFFFFF
13	
12	PPPPPPPPPPPPPPPPPPPPPPPPPPPPPPPPPPPPPP
11	₽₽₽₽₽₽₽₽₽₽₽₽₽₽₽₽₽₽₽₽₽₽₽₽₽₽₽₽₽₽₽₽₽₽₽₽₽₽₽
10	000000000000000000000000000000000000000
9	₽₽₽₽₽₽₽₽₽₽₽₽₽₽₽₽₽₽₽₽₽₽₽₽₽₽₽₽₽₽₽₽₽₽₽₽₽₽₽
8	
6	
5	
4	PPPPPPPPPPPPPPPPPPPPPPPPPPPPPPPPPPPPPP
3	₽₽₽₽₽₽₽₽₽₽₽₽₽₽₽₽₽₽₽₽₽₽₽₽₽₽₽₽₽₽₽₽₽₽₽₽₽₽₽
2	₽₽₽₽₽₽₽₽₽₽₽₽₽₽₽₽₽₽₽₽₽₽₽₽₽₽₽₽₽₽₽₽₽₽₽₽₽₽₽
1	₽₽₽₽₽₽₽₽₽₽₽₽₽₽₽₽₽₽₽₽₽₽₽₽₽₽₽₽₽₽₽₽₽₽₽₽₽₽₽
	123456/890128456/890189018866/8901890189018866/890189018866/890189018866/890189018866/890189018866/8901866/8901866/890189018866/8901866/8901866/890189018866/8901866/890189018866/8901866/8901866/89018901866/8901866/89018901866/89018901890189018901890189018901890018866/890018900189001890000000000000000000000
	TOTAL COMPTAGE : 10000 SUR 10000 NUMERO DU CANAL MOYEN : 51 COMPTAGE AU "" : 163 VAL. PHYS. AU "" : 3.331E-15 (MRD) RESOLUTION PAR CANAL : 1.50
	PARAMETRES PHYSIQUES DE LA DISTRIBUTION : COMPTAGE = 10000 PARTICULES MIN = -50.00 , MAX = 49.99 , MAX-MIN = 99.99 (MRD) MOYENNE = 0.2838 (MRD) SIGMA = 28.75 (MRD)
TRAJ 1	IEX,D,Y,T,Z,P,S,time: 1 0.9980 0.000 -30.24 0.000 44.63 0.0000 0.0000

Excerpt from zgoubi.res : the final momentum resolution histogram at the spectrometer focal surface.

* * * * * * *	*********	*******	*****	* * * * * * *	******	********	* * * * * * * * * * * *	*******	*****
16	HISTO	HISTO	OF						
		HISTOGR	AMME DI	e la	COORDONNEE Y				
		PARTICU	LES PR	IMAIRES	ET SECONDAIN	RES			
		DANS L	A FENE	TRE :	-0.5000 /	2.000	(CM)		
		NORMALI	SE						
20									
19									
18									
17					Y				
16					Y	Y			
15					Y	Y			
14					Y	Y			
13					Y	Y			
12					Y	Y			
11					Y	Y			
10				0	0	0	0		
9				Y	Y	Y	Y		
8				Y	Y	YY	Y		
7				Y	ΥY	YY	ΥΥ		
6		Y		YYY	ΥY	YY	ΥΥ		
5		Y	Y	YYY	ΥY	YY	YYYY		
4		Y	ΥΥ	YYY	YYY	YY	YYYY		
3		Y	Y YY	YYYYY	YYY	YYYY	YYYYY		
2		ΥY	YYYY	YYYYY	Y YYYY	YYYYY	YYYYYY		
1		YYY	YYYYYYY	YYYYYYY	YYYYYYYYYYYYYY	YYYYYYYY	YYYYYYYY		
	10045676								
	12343076	901234567	0901234	20/0901	23450/090123450	0/09012345	0/090123450	090123430	018901
		2	2	4	5	6	/	0	9
	TOTAL COMPT	AGE			10000 SUR 10	000			
	NUMERO DU	CANAL M	OYEN		51				
	COMPTAGE AU	"	"		246				
	VAL. PHYS. A	U "			0.750 (CM)				
	RESOLUTION	PAR CANA	L		3.125E-02 (CM)				
	PARAMETRES	PHYSIQUES	DE L	A DIST	RIBUTION :				
		COMPTAG	E = 10	000 PA	RTICULES				
		MIN = -	0.1486	, MA	X = 1.652	, MAX-MIN	= 1.800	(CM)	
		MOYENNE	= 0.7	576	(CM)				
		SIGMA =	0.462	1 (CM)				

TRAJ 1 IEX,D,Y,T,Z,P,S,time : 1 0.9980 0.2475 74.43 -6.2488E-03 -6.929 697.41 0.0000

2 TRANSFER MATRICES ALONG A TWO-STAGE SEPARATION KAON BEAM LINE

800 MeV/c kaon beam line at BNL Alternating Gradient Synchrotron [77]. The line includes two separation Wien filters.



Layout of LESB3 beamline.





zgoubi data file.

800 MeV/c KAON BEAM LINE. CALCULATION OF TRANSFER COEFFICIENTS.

'OBJET'	JN BEAM LINE. CALCU	LATION OF 1	RANSFER COEFFICIENIS.	1
2668.5100		AUTOMAT	IC GENERATION OF	
6 .1 .1 .1 .1 .1	0001	AN OBJ OF THE	ECT FOR CALCULATION FIRST ORDER TRANSFER	
0. 0. 0. 0. 0.	1.	COEFFIC	IENTS WITH 'MATRIX'	
'PARTICUL'	17733E-19 0 0 0	KAON M	A POP USE IN WIEN FILTE	2
'DRIFT'	.1//555 15 0. 0. 0. 0.	IGAON PI	a g, for ose in with fible	3
35.00000				
QUADRUPO'		Q1		4
76.2 15.24	13.6			
30. 30.				
4 0.2490 30 30	5.3630 -2.4100	0.9870 0	. 0.	
4 0.2490	5.3630 -2.4100	0.9870 0	. 0.	
1.1				
'DRIFT'				5
25.00000				
QUADRUPO'		Q2		6
45.72 15.24	-11.357			
30. 30.	5 3630 0 4300			
4 0.2490 30. 30.	5.3630 -2.4100	0.9870 0	. 0.	
4 0.2490	5.3630 -2.4100	0.9870 0	. 0.	
1.1				
1 0.0.0. 'DRIFT'				7
-1.898				,
TOSCA'		3-D MA	P THE OF FIRST	8
0 0 1 0313E-3 1	1 1	R X Y	BENDING MAGNET Z NORMALIZATION COFFECNT	9
1D map at z=0,	from TOSCA	D, X, 1	, a non-maintarion confirm	9
59 39 1 0				
ow6_0.map				
2 0. 0. 0. 0.				
1.1				
CHANGREF'				9
070.78 -4	13.8			2
FAISCEAU'				10
-49.38				11
OCTUPOLE'				12
0				
10. 15.24 .0	2			
4 0.2490	5.3630 -2.4100	0.9870 0	. 0.	
0. 0.				
4 0.2490	5.3630 -2.4100	0.9870 0	. 0.	
1 0. 0. 0.				
'SEXTUPOL'		SX1, CO	MPENSATION	13
U 10. 15.24 2.	.4	OF THE AT VF1	Theta.Phi ABERRATION	
0. 0. 0. 0.				
4 0.2490	5.3630 -2.4100	0.9870 0	. 0.	
4 0.2490	5.3630 -2.4100	0.9870 0	. 0.	
.4	5.5555 2.1100	0.0070 0		
1 0. 0. 0.				
DRIFT'				14
'WIENFILT'		FIRST	VERTICAL WIEN FILTER	15
0				
2.16 55.E5 -	0215576 2			
20. 10. 10. 0.2401 1.8639	-0.5572 0.3904	0. 0.		
0.2401 1.8639	0 -0.5572 0.3904	0. 0.		
20. 10. 10.	0 5570 0 2004	0 0		
0.2401 1.8639	-0.5572 0.3904	0. 0.		
1.				
. 0. 0. 0.				1.0
30.				10
QUADRUPO'		Q3		17
0	6 24			
30. 30.	-0.54			
4 0.2490	5.3630 -2.4100	0.9870 0	. 0.	
30.30.	5 3630 2 4100	0 0070 0	0	
- 0.2490 1.1	J.JUJU -2.41UU	0.2010 0		
1 0.0.0.				
DRIFT'				18
'MULTIPOL'		SX2 + 0	CTU, COMPENSATION	19
0		OF THE	D.Phi AND D2.Phi	17
10. 15.24 0	0. 08. 1.2 0.	0. 0. 0. 0.	0. ABERRATIONS AT VF	1
4 0.2490	5.3630 -2.4100	0.9870 n	. 0.	
0. 0. 0. 0. 0	. 0. 0. 0. 0. 0. 0	. 0.		
4 0.2490	5.3630 -2.4100	0.9870 0	. 0.	
u. u. u. u. 0. .4	0. 0.			
1 0. 0. 0.				
'DRIFT'				20
1313				
90.0 'MATRIX'		TRANSFE	R COEFFICIENTS	21

'COLLIMA'	FIRST VERTICAL FOCUS,	22
2 2 14.6 .15E10 0.0.	MASS SLIT	23
20.0 'QUADRUPO'	Q5	24
0 45.72 15.24 10.93		
30. 30. 4 0.2490 5.3630 -2.410	00 0.9870 0. 0.	
4 0.2490 5.3630 -2.410	00 0.9870 0. 0.	
1 0. 0. 0. 'DRIFT'		25
10.0 'MULTIPOL'	COMPENSATION OF	26
0 10. 15.24 0. 0. 0. 1. 0	ABERRATIONS AT VF2). 0. 0. 0. 0. 0.	
0. 0. 0. 0. 0. 0. 0. 0. 0. 4 0.2490 5.3630 -2.410	0. 0. 00 0.9870 0. 0.	
0. 0. 0. 0. 0. 0. 0. 0. 0. 4 0.2490 5.3630 -2.410	0. 0.)0 0.9870 0. 0.	
0. 0. 0. 0. 0. 0. 0. 0. 0. 0. 0. 0. 0. 0		
'DRIFT'		27
'QUADRUPO'	Q6	28
45.72 15.24 -11.18 30. 30.		
4 0.2490 5.3630 -2.410 30.30.	00 0.9870 0. 0.	
4 0.2490 5.3630 -2.410 1.1	00 0.9870 0. 0.	
1 0.0.0. 'DRIFT'		29
50.0 'WIENFILT'	SECOND VERTICAL WIEN FILTER	30
0 2.16 -55.E5 .0215576 2 20 10 10		
0.2401 1.8639 -0.5572 0.39 0.2401 1.8639 -0.5572 0.39		
20. 10. 10. 0.2401 1.8639 -0.5572 0.39	304 0. 0.	
0.2401 1.8639 -0.5572 0.39 1.	304 0. 0.	
1. 0. 0. 0. 'DRIFT'		31
30.0 'QUADRUPO'	Q7	32
0 45.72 15.24 -6.44		
30. 30. 4 0.2490 5.3630 -2.410	00 0.9870 0. 0.	
4 0.2490 5.3630 -2.410	00 0.9870 0. 0.	
1 0. 0. 0. 'DRIFT'		33
25.00000 'QUADRUPO'	Q8	34
0 45.72 15.24 8.085		
30. 30. 4 0.2490 5.3630 -2.410	00 0.9870 0. 0.	
30. 30. 4 0.2490 5.3630 -2.410	00 0.9870 0. 0.	
1.1 1 0.0.0.		35
40.0 'COLLIMA'	SECOND VERTICAL FOCUS.	36
2 1 172E10 0. 0.	MASS SLIT	
'MATRIX' 2 0	TRANSFER COEFFICIENTS	37
'DRIFT' -25.0		38
, DIPOLE-M, 3 0 0	SIMULATION OF THE MAP OF THE SECOND BENDING MAGNET	39
18.999 0.0.0. 79.3329 17.7656 140 //80	(UFGRADED VERSION OF 'AIMANI')	
151. 4 .1455 2.26706395 1	1.1558 0. 0. 0.	
0.00 21.90 1.E6 -1.E6 1		
10. 1.	1.26 1.26	
4 .1455 2.26706395 1 -43.80 -21.90 -1.E6 -1.E6 1	1.1558 0. 0. 0. 1.1558 0. 0. 0. 1.E6 -1.E6	
4 .1455 2.26706395 1 -43.80 -21.90 -1.E6 -1.E6 1 0.0. 4 .1455 2.26706395 1	L.E5 1.E6 L.1558 0. 0. 0. L.E6 -1.E6 L.1558 0. 0. 0.	
4 .1455 2.26706395 1 -43.80 -21.90 -1.E6 -1.E6 1 0.0. 4 .1455 2.26706395 1 -43.80 -21.90 -1.E6 -1.E6 1 0	1.255 1.256 1.1558 0. 0. 0. 1.266 -1.26 1.1558 0. 0. 0. 1.266 -1.26 126 NO SHIMMING SCD ORDER INTERPORTATION	
4 .1455 2.26706395 1 -43.80 -21.90 -1.E6 -1.E6 1 0.0. 4 .1455 2.26706395 1 -43.80 -21.90 -1.E6 -1.E6 1 0 2 2.5 2	LEG 1.EG 1.1558 0. 0. 0. L.EG -1.EG 1.1558 0. 0. 0. LEG -1.EG 1EG NO SHIMMING SCD ORDER INTERPOLATION	
4 .1455 2.26706395 1 -43.80 -21.90 -1.E6 -1.E6 1 0.0. 4 .1455 2.26706395 1 -43.80 -21.90 -1.E6 -1.E6 1 0 2 2.5 2 147.48099 -0.31007 147.48 /DRIFT/	1.E6 1.E6 1.1558 0. 0. 0. 1.E6 -1.E6 1.E6 -1.E6 1E6 NO SHIMMING SCD ORDER INTERPOLATION	40
4 .1455 2.26706395 1 -43.80 -21.90 -1.E6 -1.E6 1 0.0. 4 .1455 2.26706395 1 -43.80 -21.90 -1.E6 -1.E6 1 0 2 2.5 2 147.48099 -0.31007 147.48 'DRIFT' -15.00000 'QUADRUPO'	LEG 1.EG 1.1558 0. 0. 0. L.EG -1.EG 1.1558 0. 0. 0. LEG -1.EG 1EG NO SHIMMING SCD ORDER INTERPOLATION 3099 0.31007 Q9	40
4 .145 2.26706395 1 -43.80 -21.90 -1.E6 -1.E6 1 0.0. 4 .1455 2.26706395 1 -43.80 -21.90 -1.E6 -1.E6 1 0 2 2.5 2 147.48099 -0.31007 147.48 'DRTFY' -15.00000 'QUADRUPO' 0 35.56 12.7 -13.69 -13.91	LES 1.E6 1.1558 0. 0. 0. L.E6 -1.E6 1.1558 0. 0. 0. LE6 -1.E6 1E6 NO SHIMMING SCD ORDER INTERPOLATION 3099 0.31007 Q9	40
4 .1455 2.26706395 1 -43.80 -21.90 -1.E6 -1.E6 1 0.0. 4 .1455 2.26706395 1 -43.80 -21.90 -1.E6 -1.E6 1 0 2 2.5 2 147.48099 -0.31007 147.48 /DRIFT' -15.00000 'QUADRUPO' 0 35.56 12.7 -13.69 -13.91 30. 25.4 4 0.2490 5.3630 -2.410	LES 1.ES 1.1558 0. 0. 0. LEG -1.EG 1.1558 0. 0. 0. LEG -1.EG 1EG NO SHIMMING SCD ORDER INTERPOLATION 3099 0.31007 Q9 00 0.9870 0. 0.	40
4 .1455 2.26706395 1 -43.80 -21.90 -1.E6 -1.E6 1 0.0. 4 .1455 2.26706395 1 -43.80 -21.90 -1.E6 -1.E6 1 0 2 .5 2 .5 2 147.48099 -0.31007 147.48 'DRIFT' -15.00000 'QUADRUPO' 0 35.56 12.7 -13.69 -13.91 30. 25.4 4 0.2490 5.3630 -2.410	LEG 1.EG L.1558 0. 0. 0. L.EG -1.EG L.1558 0. 0. 0. LEG -1.EG 1EG NO SHIMMING SCD ORDER INTERPOLATION 099 0.31007 Q9 00 0.9870 0. 0. 00 0.9870 0. 0.	40

'DRIFT' 25.00000						42
'QUADRUPO'			Q10			43
0						
35.56 12.7	11.97					
30. 25.4						
4 0.2490	5.3630	-2.4100	0.9870	Ο.	0.	
30. 25.4						
4 0.2490	5.3630	-2.4100	0.9870	Ο.	0.	
1.1						
1 0. 0. 0.						
'DRIFT'						44
200.0						
'MATRIX'			TRANS	FER (COEFFICIENTS	45
2 0				IE E	INAL FOCUS	
/FND/					10000	46
LND						40

Excerpt of zgoubi.res : first and second order transfer matrices and higher order coefficients at the end of the line.

		FIRST	ľ	ORDI	ER COEFFICI	ENTS	S	(MKSA):									
		3.60453 -2.05368 2.240965E- 1.185290E- -0.387557	-05		-4.453265E-02 0.270335 -8.687757E-0 -4.356398E-0 2.313953E-02	2 7 7 2	-3 4 -: -:	.049728E-04 .700517E-05 3.60817 2.05043 264218E-05	-1 1 -1 -0		65832E-04 63910E-05 31805E-02 86991 15244E-06	0 0 0 1	.0000		-5.22 -9.56 -7.81 -3.98	978 191 536 339	3E-02 8E-02 7E-02 2E-02 7
		0.00000			0.00000	-	~	0.00000		0.0	00000	0	.0000	00	1.0	000	D
		DetY-1 =		-(0.1170246601,	,	D	etZ-1 =	0.	000	00034613						
		R12=0 at	0	.16	47 m,		R	34=0 at -0.	6034	E-	D1 m						
	Fi	irst order sy	/mp	let	ic conditions	s (e	exp	ected values	= ())	:						
		-0.1170		3.4	4614E-06 -3	1.82	2071	E-04 3.09	73E-	-05	4.6007E-	04	-8	.0561E-0)5		
		SECON	JD	ORI	DER COEFFIC	IEN	ſS	(MKSA):									
1	11	7.34	1	21	-1.78	1	31	1.399E-02	1	41	1.456E-02	1	51	0.00	1	61	36.3
1	12	-1.78	1	22	-530.	1	32	-1.308E-03	1	42	-1.743E-03	1	52	0.00	1	62	12.3
1	13	1.399E-02	1	23	-1.308E-03	1	33	-0.611	1	43	-0.522	1	53	0.00	1	63	-2.771E-02
1	14	1.456E-02	1	24	-1.743E-03	1	34	-0.522	1	44	0.163	1	54	0.00	1	64	-2.211E-02
1	15	0.00	1	25	0.00	1	35	0.00	1	45	0.00	1	55	0.00	1	65	0.00
1	16	36.3	1	26	12.3	1	36	-2.771E-02	1	46	-2.211E-02	1	56	0.00	1	66	2.88
2	11	-303.	2	21	3.81	2	31	3.684E-02	2	41	3.581E-02	2	51	0.00	2	61	144.
2	12	3.81	2	22	-62.9	2	32	-5.821E-04	2	42	-1.638E-04	2	52	0.00	2	62	-0.759
2	13	3.684E-02	2	23	-5.821E-04	2	33	1.05	2	43	1.94	2	53	0.00	2	63	-1.031E-02
2	14	3.581E-02	2	24	-1.638E-04	2	34	1.94	2	44	6.70	2	54	0.00	2	64	-4.285E-02
2	15	0.00	2	25	0.00	2	35	0.00	2	45	0.00	2	55	0.00	2	65	0.00
2	16	144.	2	26	-0.759	2	36	-1.031E-02	2	46	-4.285E-02	2	56	0.00	2	66	-65.3
3	11	-0.145	3	21	2.158E-02	3	31	20.6	3	41	86.0	3	51	0.00	3	61	-0.201
3	12	2.158E-02	3	22	64.6	3	32	1.61	3	42	0.496	3	52	0.00	3	62	8.793E-02
3	13	20.6	3	23	1.61	3	33	0.710	3	43	0.128	3	53	0.00	3	63	39.1
3	14	86.0	3	24	0.496	3	34	0.128	3	44	64.8	3	54	0.00	3	64	7.17
3	15	0.00	3	25	0.00	3	35	0.00	3	45	0.00	3	55	0.00	3	65	0.00
3	16	-0.201	3	26	8.793E-02	3	36	39.1	3	46	7.17	3	56	0.00	3	66	1.46
4	11	-8.254E-02	4	21	1.146E-02	4	31	10.7	4	41	47.3	4	51	0.00	4	61	-0.127
4	12	1.146E-02	4	22	33.0	4	32	0.787	4	42	0.157	4	52	0.00	4	62	3.566E-02
4	13	10.7	4	23	0.787	4	33	0.365	4	43	6.774E-02	4	53	0.00	4	63	17.5
4	14	47.3	4	2.4	0.157	4	34	6.774E-02	4	44	33.1	4	54	0.00	4	64	1.05
4	1.5	0.00	4	25	0.00	4	35	0.00	4	45	0.00	4	55	0.00	4	65	0.00
4	16	-0.127	4	26	3.566E-02	4	36	17.5	4	46	1.05	4	56	0.00	4	66	0.715
5	11	568	5	21	-7 67	5	31	-5 970E-02	5	41	-5 682E-02	5	51	0 00	5	61	-251
5	12	-7 67	5	22	225	5	32	1 283E-03	5	42	6 947E-04	5	52	0 00	5	62	2 77
5	13	-5 970E-02	5	23	1 2838-03	5	33	10.2	5	13	10 2	5	53	0.00	5	63	0 215
5	14	-5 682E-02	5	20	6 947E-04	5	30	10.2	5	44	1 59	5	54	0 00	5	64	0 129
5	15	0.00	5	25	0.00	5	25	0.00	5	15	1.39	5	55	0.00	5	65	0.129
5	16	-251	5	26	2 77	5	36	0.215	5	-1.5	0.00	5	56	0.00	5	66	112
~	- U			20	4.11		20	· · L L J	9	- 1 U	U . 12 J		00	0.00	J	00	1 1 L .

HIGHER ORDER COEFFICIENTS (MKSA):

Y/Y3	5784.8
Y/T3	9.40037E+05
Y/Z3	0.70673
Y/P3	0.42104
T/Y3	-18607.
T/T3	1.04607E+05
T/Z3	-0.10234
T/P3	5.25793E-02
Z/Y3	32.161
Z/T3	18.425
Z/Z3	-872.50
Z/P3	-785.20
P/Y3	15.460
P/T3	7.5264
P/Z3	-409.98
P/P3	-389.15

3 IN-FLIGHT DECAY IN SPES 3



Figure 57: Layout of SPES 3 spectrometer.

zgoubi data file

```
SIMULATION OF PION IN-FLIGHT DECAY IN SPES3 SPECTROMETER
'MCOBJET'
                                                                      1
3360.
                                     REFERENCE RIGIDITY (PION).
                                     DISTRIBUTION IN WINDOW.
                                     BUNCHES OF 200 PARTICLES.
200

        1
        1
        1
        1
        1
        UNIFORM DISTRIBUTION

        0.
        0.
        0.
        0.
        1.
        CENTRAL VALUES OF

                                    CENTRAL VALUES OF BARS.
.5e-2 50.e-3 .5e-2 50.e-3 0. 0.4 WIDTH OF BARS.
1 1 1 1 1 1 CUT-OFFS (UNUSED)
9 9. 9. 9. 9. UNUSED.
   9.9.9.9.9.
186387 548728 472874
                                    SEEDS.
'PARTICUL'
                                                                       2
139.6000 0. 0. 26.03E-9 0.
                                    PION MASS AND LIFE TIME
'MCDESINT'
                                                                       3
105.66 0.
                                    PION -> MUON + NEUTRINODECAY
136928 768370 548375
'ESI'
                                                                       4
77.3627
'CHAMBR'
                                    STOPS ABERRANT MUONS.
                                                                       5
1
1 100.10.245.0.
'DIPOLE'
                                                                       6
2
80. 208.5
                                    TOTAL ANGLE AT, CENTRAL RADIUS RM
33. 30. 0. 0. 0.
                                    CENTRAL ANGLE, FIELD, INDICES
46. -1.
                                    ENTRANCE EFB
4. .14552 5.21405 -3.38307 14.0629 0. 0. 0.
15. 0. -65. 0. 0. -65.
46. -1.
                                    EXIT EFB
4. .14552 5.21405 -3.38307 14.0629 0. 0. 0.
-15. 69. 85. 0. 1.E6 1.E6
                                    LATERAL EFB (INHIBITED)
0. 0.
4. .14552 5.21405 -3.38307 14.0629 0. 0. 0.
-15. 69. 85. 0. 1.E6 1.E6 1E6
                                    2ND DEGREE INTERP., MESH 0.4 CM
2 10.0
4.
                                     STEP SIZE
2
164.755 .479966 233.554 -.057963
'CHAMBR'
                                                                       7
2
1 100. 10. 245. 0.
'CHANGREF'
                                    TILT ANGLE OF
                                                                       8
0. 0. -49.
                                    FOCAL PLANE.
'HISTO'
                                   TOTAL SPECTRUM (PION + MUON).
                                                                      9
2 -170. 130. 60 1
20 'Y' 1 'Q'
'HISTO'
                                  PION SPATIAL SPECTRUM
                                                                     10
2 -170. 130. 60 2
20 'P' 1 'P'
                                   AT FOCAL PLANE.
'HISTO'
                                   MUON SPATIAL SPECTRUM
                                                                      11
2 -170. 130. 60 3
20 'y' 1 'S'
                                   AT FOCAL PLANE.
'HISTO'
                                  MUON MOMENTUM SPECTRUM
                                                                      12
1 .2 1.7
20 'd' 1 'S'
               60 3
                                   AT FOCAL PLANE.
'REBELOTE'
                                   (49+1) RUNS = CALCULATION OF
                                                                     13
49 0.1 0
                                   (49+1)*200 TRAJECTORIES.
'END'
                                                                      14
```

Excerpt of zgoubi.res : histograms of primary and secondary particles at focal surface of SPES3.





Figure 58: Vary B in all quadrupoles, for fitting of the transfer coefficients R_{12} and R_{34} at the end of the line. The first and last quadrupoles are coupled so as to present the same value of B.

zgoubi data file.

```
MATCHING A SYMMETRIC QUADRUPOLE TRIPLET
 'OBJET'
                                                                                                                          1
                     RIGIDITY (kG.cm)
2501.73
5
                     11 PARTICLES GENERATED FOR USE OF MATRIX
2. 2. 2. 2. 2. 0. .001
0. 0. 0. 0. 0. 0. 1.
'ESL '
                                                                                                                          2
200.
 'QUADRUPO'
                3
                                                                                                                          3
0
40. 15. -7.
0. 0.
6 .1122 6.2671 -1.4982 3.5882 -2.1209 1.723
0 0.
6 .1122 6.2671 -1.4982 3.5882 -2.1209 1.723
5.
1 0. 0. 0.
'ESL'
                                                                                                                          4
30.
'QUADRUPO'
                  5
                                                                                                                          5
0
40. 15. 3.
6 .1122 6.2671 -1.4982 3.5882 -2.1209 1.723
0. 0.
0. 0.
6 .1122 6.2671 -1.4982 3.5882 -2.1209 1.723
5.
1 0. 0. 0.
 'ESL'
                                                                                                                          6
30.
 'QUADRUPO'
                 7
                                                                                                                          7
0
40. 15. -7.
0. 0.
6 .1122 6.2671 -1.4982 3.5882 -2.1209 1.723
0. 0.
6 .1122 6.2671 -1.4982 3.5882 -2.1209 1.723
5.
1 0. 0. 0.
'ESL'
                                                                                                                          8
200.
 'MATRIX'
                                                                                                                          9
1 0
'FIT2'
                     VARY B IN QUADS FOR FIT OF R12 AND R34
                                                                                                                         10
2
                     # OF VARIABLES
  12 7.12 2.
                     SYMMETRIC TRIPLET => QUADS #1 AND #3 ARE COUPLED
3
                     PRMTR #12 OF ELEMENTS #3, 5 AND 7 IS FIELD VALUE
5
   12 0.
            2.
2
  1.E-10
                     # OF CONSTRAINTS, PENALTY
1
   1 2 8 16.6 1.
                     CNSTRNT #1 : R12=16.6 AFTER LAST DRIFT (LMNT #8)
1 3 4 8 -.88 1.
                     CNSTRNT #2 : R34=-.88 AFTER LAST DRIFT
 'END'
                                                                                                                         11
```
Excerpt of zgoubi.res : first order transfer matrices prior to and after fitting.

**************************************	**************** X WITH STARTING	**************************************	*****	*****	*****	* * * * * * * *	*	
	MATRICE DE	TRANSFERT OR	DRE 1 (MKSA)					
5.43427	17.0254	0.00000	0.00000	0.0	0000	0.0000	0	
1.67580	5.43425	0.00000	0.00000	0.0	0000	0.0000	0	
0.00000	0.00000	-1.27003	-0.974288	0.0	0000	0.0000	0	
0.00000	0.00000	-0.629171	-1.27004	0.0	0000	0.0000	0	
0.00000	0.00000	0.00000	0.00000	1.0	0000	0.0000	0	
0.00000	0.00000	0.00000	0.00000	0.0	0000	1.0000	0	
**************************************	**************************************	**************************************	* * * * * * * * * * * * * * * * * *	****	*****	* * * * * * *	*	
LMNT VAR PAR	AM MINIMUM	INITIAL	FINAL	MAXIMUM	STEP	NAME	LBL1	LBL2
3 1	12 -21.0	-7.00	-6.972765137	7.00	1.707E-04	QUADRUP	0 3	*
7 1 1	20 -6.97	-7.00	-6.972765137	7.00	1.707E-04	2		
5 2	12 -3.00	3.00	3.229344585	9.00	1.266E-04	OUADRUP	0 5	*
STATUS OF CONS	TRAINTS (Target	penalty = 1	0000E - 10)			2		
TYPE T J I	MNT# DEST	RED	WEIGHT F	EACHED	KT2	*	Parameter(s)	
1 1 2	8 1 6600	000E+01 1	0000E+00 1 65	99981E+01		*	∩ ·	
1 3 4	8 -8 8000	000E-01 1	0000E+00 -8.80	00964E-01		*	0.	
Fit reached pe	nalty value 8	.4374E-11	0.000	0000111 01			•••	
****	****	* * * * * * * * * * * * * * *	* * * * * * * * * * * * * * * * *	****	****	* * * * * * * *	*	
MATRIX, WITH NE	W VARIABLES :							
5.27056	16.6000	0.00000	0.00000	0.0	0000	0.0000	0	
1.61443	5.27450	0.00000	0.00000	0.0	0000	0.0000	0	
0.00000	0.00000	-1.24205	-0.880010	0.0	0000	0.0000	0	
0.00000	0.00000	-0.622553	-1.24620	0.0	0000	0.0000	0	
0.00000	0.00000	0.00000	0.00000	1.0	0000	0.0000	0	
0.00000	0.00000	0.00000	0.00000	0.0	0000	1.0000	0	
* * * * * * * * * * * * * * * *	*****	* * * * * * * * * * * * * * *	* * * * * * * * * * * * * * * * * *	****	****	* * * * * * * *	*	



5 MULTITURN SPIN TRACKING IN SATURNE 3 GeV SYNCHROTRON

Figure 59: Tracking over 3000 turns. These simulations exhibit the first order parameters and motions as produced by the multi-turn ray-tracing.

(A) Horizontal phase-space: the particle has been launched near to the closed orbit (the fine structure is due to Y - Z coupling induced by bends fringe fields, also responsible of the off-centering of the local closed orbit - at ellipse center).

(B) Vertical phase-space: the particle has been launched with $Z_0 = 4.58 \ 10^{-3} \text{ m}$, $Z'_0 = 0$. A least-square fit by $\gamma_Z Z^2 + 2\alpha_Z Z Z' + \beta_Z Z'^2 = \varepsilon_Z/\pi$ yields $\beta_Z = 2.055 \text{ m}$, $\alpha_Z = 0.444$, $\gamma_Z = 0.582 \text{ m}^{-1}$, $\varepsilon_Z/\pi = 12 \ 10^{-6} \text{ m.rad}$ in agreement with matrix calculations. (C) Fractional tune numbers obtained by Fourier analysis for $\varepsilon_Y/\pi = \varepsilon_Z/\pi \simeq 12 \ 10^{-6} \text{ m.rad}$: $\nu_Y = 0.63795$, $\nu_Z = 0.60912$ (the integer part is 3 for both).

(**D**) Longitudinal phase-space ("(DP, phase)" in Zgoubi notations): particles with initial momentum dispersion of 5 10^{-4} (1), 10^{-3} (2), 1.65 10^{-3} (3) (out of acceptance), are accelerated at 1405 eV/turn ($\dot{B} = 2.1$ T/s); analytical calculations give accordingly momentum acceptance of 1.65 10^{-3} .



Figure 60: Crossing of $\gamma G = 7 - \nu_Z$, at $\dot{B} = 2.1$ T/s.

(A) $\varepsilon_Z/\pi = 12.2 \ 10^{-6}$ m.rad. The strength of the resonance is $|\varepsilon| = 3.3 \ 10^{-4}$. As expected from the Froissart-Stora formula [80] the asymptotic polarization is about 0.44.

(B) The emittance is now $\varepsilon_Z/\pi = 1.2 \ 10^{-6}$ m.rad; comparison with (A) shows that $|\varepsilon|$ is proportional to $\sqrt{\varepsilon_Z}$.

(C) Crossing of this resonance for a particle having a momentum dispersion of 10^{-3} .

zgoubi data file (beginning and end).

SATURNE. CROSSING Ga	ammaG=7-NUz, NU	Jz=3.60877(c	erturbed)	71.6256 'BEND'
'OBJET' 5015.388			834.04 MeV, proton	0 247.3003
2			,	20. 8. 4.2401
4 1 6.2E-02 6.5E-02	.458 0. 0.	1.00 'c	' EpsilonY/pi ⁻ 0. (Closed orb.)	it) 20.8.
0.356 0.379 0.647 0.689	.458 0. 0. .458 0. 0.	1.0005 '1	, ,	4 .2401 #30 120
1.024 1.09	.458 0. 0.	1.0016 '3	,	'ESL' 71 6256
1 1 1 1 'SCALING'				'QUADRUPC
1 4 MULTIDOI				0 46.723 1
2		CROSSIN	IG GammaG=7-Nuz+/-14E, E=3.3E-4	0. 0.
5015.388E-3 5034.3 1 3442	391E-3	AT 2.1 FROM 83	T/s, IN 3442 MACHINE TURNS, 34.041 TO 838.877 MeV	6 .1122 0. 0.
QUADRUPO				6 .1122 #30150130
2 5015.388E-3 5034.3	391E-3			1 0. 0. 0
1 3442 BEND				392.148
2				'MULTIPOL
5015.388E-3 5034.3 1 3442	391E-3			48.6273
CAVITE				0. 0. 0. 6 .1122
1. 1.0037	78894	RELATIV	YE CHANGE OF SYNCHRONOUS RIGIDITY	0. 0. 0.
1 3442				0. 0. 0.
938.2723 1.60218928	2-19 1.7928474	0.0.		#30 50 30
'SPNTRK' 3				'ESL'
(MARVER) #CtaxtRing				392.148 / QUADRUPC
'QUADRUPO'	QP 1		5	0
0 46.723 10763695	5	.763695	= FIELD FOR BORO=1 T.m	46.723 1
0. 0.	-			6 .1122
ь .1122 6.2671 -1.4 0. 0.	1982 3.5882 -2.	1209 1.723		6 .1122
6 .1122 6.2671 -1.4	1982 3.5882 -2.	1209 1.723		#30 50 30 1 0. 0. 0
1 0. 0. 0.				'ESL'
'ESL' 71.6256	SD 2		6	'BEND'
'BEND'	DIP 3 4	3	7	0 247.3003
247.30039 0. 1.57	7776			20. 8.
20. 8042760566	567	0 0		4 .2401 20. 8.
20. 8042760566	567 20.	8.		4 .2401
4 .2401 1.8639 #30 120 30 bend	.5572 .3904 0. 3 0. 0. 0	0.0. .1963495408	1	'ESL'
'ESL'	SD 2		8	71.6256 / MULTIPOL
/1.6256 'MULTIPOL'	QP 5		9	0
0 48 6273 10 0 - 76	55533 0 0 0	0 0 0	0 0	48.6273
0. 0. 0. 0. 0. 00	.0 0. 0. 0. 0. 0.	0. 0. 0.		6 .1122
6 .1122 6.2671 -1.4 0. 0. 0. 0. 0. 0.	1982 3.5882 -2. 0. 0. 0. 0.	1209 1.723		6 .1122
6 .1122 6.2671 -1.4	1982 3.5882 -2.	1209 1.723		0. 0. 0. #30 50 30
#30 50 30 Quad	0. 0. 0. 0.			1 0. 0. 0
1 0. 0. 0. 'ESL'	SD 2		10	71.6256
71.6256				'BEND'
'BEND' 0	DIP 3 4	13	11	247.3003
247.30039 0. 1.57	7776			20. 8. 4 .2401
4 .2401 1.8639	.5572 .3904 0.	0.0.		20. 8.
20. 8042760566	567 20. 5572 .3904 0.	8.		#30 120
#30 120 30 bend	3 0. 0. 0	.1963495408	1	
71.6256	5D 2		12	1701/
'QUADRUPO'	QP 1		13	'ESL' 392.148
46.723 10763695	5			'MARKER' #
0. 0. 6 .1122 6.2671 -1.4	1982 3.5882 -2.	1209 1.723		'CAVITE'
0. 0.	1982 3 5882 -2	1209 1 723		1 105.55568
#30 50 30 Quad		1205 1.725		6000.
1 0. 0. 0. 'ESL'	SD 2		1.4	b_zgoubi.
71.6256				'SPNPRNL'
0	DIP 3 4	1 3	15	'SPNPRT'
247.30039 0. 1.57	7776			'REBELOTE 2999 0.1
4 .2401 1.8639	.5572 .3904 0.	0. 0.		'END'
20. 8042760566 4 .2401 1.8639 -	567 20. .5572 .3904 0	8.		
#30 120 30 bend	3 0. 0. 0	.1963495408		
'ESL' 71.6256	SD 2		16	
'MULTIPOL'	QP 5		17	
48.6273 10. 0	.765533 0. 0. 0	. o. o. o	. 0. 0.	
0. 0. 0. 0. 0. 0.	0. 0. 0. 0. 1982 3.5882 -2	0.		
0. 0. 0. 0. 0. 0.	0. 0. 0. 0.	0.		
ь .1122 6.2671 -1.4 0. 0. 0. 0. 0. 0.	1982 3.5882 -2. 0. 0. 0. 0.	1209 1.723		
#30 50 30 Quad				
± v. v. V.				

'ESL'	SD 2	18
'BEND'	DIP 3 4 3	19
0 247.30039 0. 1.57776		
20. 804276056667 4 2401 1 8639 - 5572	3904 0 0 0	
20. 804276056667	20. 8.	
4 .2401 1.86395572 #30 120 30 bend 3 0	. 3904 0. 0. 0. . 0. 01963495408	
'ESL' 71.6256	SD 2	20
'QUADRUPO'	QP 1	21
46.723 10763695		
0. 0. 6 .1122 6.2671 -1.4982 3	.5882 -2.1209 1.723	
0. 0.	5882 -2 1209 1 723	
#30 50 30 Quad	.5662 2.1265 1.725	
'ESL'		22
392.148 'MULTIPOL'	QP 5	23
0	300000000	
0. 0. 0. 0. 0. 0. 0. 0.	0. 0. 0.	
6 .1122 6.2671 -1.4982 3 0. 0. 0. 0. 0. 0. 0. 0.	.5882 -2.1209 1.723 0. 0. 0. 0.	
6 .1122 6.2671 -1.4982 3 0. 0. 0. 0. 0. 0. 0. 0. 0	.5882 -2.1209 1.723	
#30 50 30 Quad		
'ESL'		24
392.148 'QUADRUPO'	QP 1	25
0		
0. 0.		
6 .1122 6.2671 -1.4982 3 0. 0.	.5882 -2.1209 1.723	
6 .1122 6.2671 -1.4982 3 #30 50 30 Ouad	.5882 -2.1209 1.723	
1 0. 0. 0.	2	26
71.6256	SD 2	20
'BEND' 0	DIP 3 4 3	27
247.30039 0. 1.57776		
4 .2401 1.86395572	.3904 0. 0. 0.	
20. 804276056667 4 .2401 1.86395572	20. 8. .3904 0. 0. 0.	
#30 120 30 bend 3 0	. 0. 01963495408 SD 2	28
71.6256		
0	QP 5	29
48.6273 10. 0765533 0. 0. 0. 0. 0. 0. 0. 0.	0. 0. 0. 0. 0. 0. 0. 0. 0. 0. 0. 0.	
6 .1122 6.2671 -1.4982 3 0 0 0 0 0 0 0 0	.5882 -2.1209 1.723	
6 .1122 6.2671 -1.4982 3	.5882 -2.1209 1.723	
#30 50 30 Quad	. 0. 0.	
1 0. 0. 0. 'ESL'	SD 2	30
71.6256		21
0	DIF 2 4 2	21
247.30039 0. 1.57776 20. 804276056667		
4 .2401 1.86395572	.3904 0. 0. 0.	
4 .2401 1.86395572	.3904 0. 0. 0.	
#30 120 30 bend 3 0	. 0. 01963495408	
		:::::
'ESL'		84
/MARKER' #EndRing		86
'CAVITE'		87
1		
6000. 0.	SIN(phis) = .234162, dE=1.40497 keV/	Turn.
'FAISCNL' b_zgoubi.fai		88
'SPNPRNL'		89
'SPNPRT'		90
2999 0.1 99	TOTAL NUMBER OF TURNS = 3000	91
'END'		92



Figure 61: Upper plot: 50-particle beam tube ray-traced through a double focusing quadrupole doublet typical of the front end design of micro-beam lines. Initial conditions are : $Y_0 = Z_0 = 0$, angles T_0 and P_0 random uniform within ± 0.2 mrad, and momentum dispersion $\delta p/p$ uniform in $\pm 3 \, 10^{-4}$.

Lower plot: (**D**) sub-micronic cross-section at the image plane of a 4000-particle beam with initial conditions as above, obtained thanks to the second-order achromatic magneto-electrostatic quadrupole doublet (the image size would be $\Delta Y \approx \Delta Z \approx \pm 50 \mu m$ with regular magnetic quadrupoles, due to the momentum dispersion). Note the high resolution of the ray-tracing which still reveals image structure of nanometric size.

zgoubi data file.

MICROBEAM LINE, WITH A MAGNETO-ELECTRO 'MCOBJET' 20.435 1 200 1 1 1 1 1 1 0.0.0.0.0.1. 0.2e-3 0.2e-3 0.0003 10.10.10.10.10.10. 9 9.9.9.9. 16387 548728 472844	STATIC QUADRUPOLE DOUBLET. RANDOM OBJECT DEFINITION 1 RIGIDITY (20keV PROTONS). DISTRIBUTION IN WINDOW. NUMBER OF PARTICLES. UNIFORM DISTRIBUTION. CENTRAL VALUE, AND HALF WIDTH OF DISTRIBUTION. CUT-OFFS (UNUSED). FOR P(D) - UNUSED. SEEDS.	
'PARTICUL'	PARTICLE MASS AND CHARGE 2	
938.2723 1.60217733E-19 0. 0. 0. 'DRIFT'	DRIFT. 3	
500.	55755	
59.	DRIFT. 4	
'EBMULT'	FIRST MAGNETO-ELECTROSTATIC 5	
0 10.2 10.09272.986 0.0.0.0.0.0. 0.0.0.0.0.0.0.0.0.0.0.0.0.0.0.0.0.	QUADRUPOLE. 0. 0. 0. ELECTRIC Q-POLE COMPONENT. 0. ENTRANCE EFB, SHARP EDGE.	
6 .1122 6.2671 -1.4982 3.5882 -2.1209 0. 0. 0. 0. 0. 0. 0. 0. 0. 0. 0.	1.723 0. EXIT EFB. SHARP EDGE.	
6 .1122 6.2671 -1.4982 3.5882 -2.1209	1.723	
0. 0. 0. 0. 0. 0. 0. 0. 0. 0. 0. 10.2 10. 0. 1.89493 0. 0. 0. 0. 0. 0. 0. 0. 0. 0. 0. 0. 0. 0. 0. 0.	0. 0. 0. MAGNETIC Q-POLE COMPONENT. 0. ENTRANCE EFB, SHARP EDGE.	
6 .1122 6.2671 -1.4982 3.5882 -2.1209 0. 0. 0. 0. 0. 0. 0. 0. 0. 0. 0. 0. 6 .1122 6.2671 -1.4982 3.5882 -2.1209	1.723 0. EXIT EFB, SHARP EDGE. 1.723	
1 0. 0. 0. 'DRIFT'	DRIFT. 6	
4.9 'EBMULT' 0	SECOND MAGNETO-ELECTROSTATIC 7 QUADRUPOLE.	
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	0. 0. 0. 1.723 1.723 0. 0. 0. 0. 1.723 1.723 1.723	
1 0. 0. 0. 'DRIFT'	DRIFT. 8	
'HISTO' 2 -5E-6 5E-6 60 2 20 /Y/ 1 /O/	HISTOGRAM 9 OF THE Y COORDINATE.	
'HISTO' 4 -5E-6 5E-6 60 2	HISTOGRAM 10 OF THE Z COORDINATE.	
20 'Z' I 'Q' 'FAISCNL' RA ravs.out FO	YS ARE STORED IN rays.out 11 R FURTHER PLOTTING.	
'REBELOTE' RUN AGAIN, FOR RAY-TRACING		
19 0.1 0 A	TOTAL OF 200*(19+1) PARTICLES.	

zgoubi.res file.

12 REBELOTE RUN AGAIN	******************
Multiple pass, from element # 1 : MCOBJET /labell=RANDOM /label2=OBJECT to F ending at pass # 20 at element # 12 : REBELOTE /labell=RUN	REBELOTE /labell=RANDOM /label2=OBJECT /label2=AGAIN
End of pass # 19 through the optical structure	
Total of 3800 particles have been launched	
****	****
Next pass is $\#$ 20 and last pass through the optical structure	

Reference magnetic rigidity = 20.435 KG*CM	
Object built up of 200 particles Distribution in a Window Contral values (MKS) woite:	
Yo, To, Zo, Po, Xo, BR/BORO : 0.000 0.000 0.000	0.000 0.000 1.000
Width (+/- , MKSA units) : DY, DT, DZ, DP, DX, DBR/BORO : 0.00 2.000E-04 0.00 Cut-offs (* +/-Width) :	2.000E-04 0.00 3.000E-04
NY, NT, NZ, NP, NX, NBR/BORO : 1.00 1.00 1.0	00 1.00 1.00 1.00
Y, T, Z, P, X, D: Uniform Uniform Uniform	Uniform Uniform Uniform
2 PARTICUL PARTICLE MASS	************
Particle properties :	
Mass = 938.272 MeV/c2 Charge = 1.602177E-19 C	
<pre>Reference data : mag. rigidity (kG.cm) : 20.435000 =p/q, such that dev.= mass (MeV/c2) : 938.27230 momentum (MeV/c) : 6.1262621 energy, total (MeV) : 938.29230 energy, knetic (MeV) : 1.9998909E-02 beta = v/c : 6.5291616518E-03 gamma : 1.000021316 beta*gamma : 6.529300852E-03</pre>	=B*L/rigidity
<pre>electric rigidity (MeV) : 3.9999376635E-02 =T[eV]*(gamma+1)/ga</pre>	amma, such that dev.= $E \star L/rigidity$
***************************************	***************************************

```
DRIFT
                        DRIFT.
                                    Drift, length = 500.00000 cm
TRAJ #1 IEX.D.Y.T.Z.P.S.time : 1 2.999865E-04 -2.027052E-02 -4.054104E-02 -9.359114E-02 -1.871823E-01 5.0000001E+02 2.55365E+00
Cumulative length of optical axis = 5.00000000 m at ; Time (for ref. rigidity & particle) = 2.554417E-06 s
4 DRIFT
                        DRIFT.
                                   Drift, length = 59.00000 cm
TRAJ #1 IEX,D,Y,T,Z,P,S,time: 1 2.999865E-04 -2.266244E-02 -4.054104E-02 -1.046349E-01 -1.871823E-01 5.5900001E+02 2.85498E+00
Cumulative length of optical axis = 5.59000000 m at ; Time (for ref. rigidity & particle) = 2.855839E-06 s
5 EBMULT
                        FIRST
                                       ELECTRO-MA
       ---- MULTIPOLE
                 ULTIPOLE :

Length of element = 10.200000

Bore radius R0 = 10.000

E-DIPOLE = 0.0000000E+00 V/m

E-QUADRIPOLE = 0.272960E+03 V/m

E-SEXTUPOLE = 0.000000E+00 V/m

E-OCTUPOLE = 0.000000E+00 V/m
                                                                 cm
                  E-DECAPOLE
                                  = 0.0000000E+00 V/m

        E-DECAPOLE
        0.0000000E+00
        V/m

        E-DODECAPOLE
        0.000000E+00
        V/m

        E-14-POLE
        0.000000E+00
        V/m

        E-14-POLE
        0.000000E+00
        V/m

        E-16-POLE
        0.000000E+00
        V/m

        E-20-POLE
        0.000000E+00
        V/m

                  Entrance/exit field models are sharp edge
FINTE, FINTS, gap: 0.0000E+00 0.0000E+00 5.0000E+00
                  FINTE, FINTS, gap :
      ----- MULTIPOLE :

Length of element = 10.200000

Bore radius RO = 10.000

B-DIPOLE = 0.000000E+00 kG

B-QUADRUPOLE = 1.8949300E+00 kG

B-SEXTUPOLE = 0.000000E+00 kG

B-OCTUPOLE = 0.000000E+00 kG

D-DECAPOLE = 0.000000E+00 kG
                  B-DECAPCLE = 0.000000E+00 kG
B-DODECAPOLE = 0.000000E+00 kG
B-14-POLE = 0.000000E+00 kG
B-16-POLE = 0.000000E+00 kG
B-18-POLE = 0.000000E+00 kG
                 B-20-POLE
                 Entrance/exit field models are sharp edge
FINTE, FINTS, gap : 0.0000E+00 0.0000E+00 5.0000E+00
  *** Warning : sharp edge model, vertical wedge focusing approximated with first order kick. FINT at entrance = 0.000
  *** Warning : sharp edge model, vertical wedge focusing approximated with first order kick. FINT at exit = 0.000
                       Integration step : 0.8000 cm
\label{eq:cumulative length of optical axis = 5.69200000 m \mbox{; Time (for ref. rigidity & particle) = 2.907949 E-06 s}
.....
       6 DRIFT
                        DRIFT.
                                   Drift, length = 4.90000 cm
TRAJ #1 IEX,D,Y,T,Z,P,S,time : 1 2.839285E-04 -1.310701E-02 9.564949E-01 -1.603604E-01 -5.590035E+00 5.7410014E+02 2.93210E+00
\label{eq:cumulative length of optical axis = 5.74100000 \qquad \text{m at ; Time (for ref. rigidity & particle) = 2.932982E-06 s}
.....
       7 EBMULT
                        SECOND
                                      ELECTRO-MA
       ---- MULTIPOLE
                   LTIPOLE :
Length of element = 10.200000
Bore radius RO = 10.000
                 Length of element = 10.2000
Bore radius RO = 10.000
E-DIPOLE = 0.000000E+00 V/m
E-QUADRUPOLE = 1.3779900E+04 V/m
E-SEXTUPOLE = 0.0000000E+00 V/m
E-DCTUPOLE = 0.0000000E+00 V/m
                                                                cm
                 Entrance/exit field models are sharp edge
              MULTIPOLE :
Length of element = 10.20000
B-DIPOLE = 0.000000E+00 kG
B-QUADRUPOLE = -2.8159200E+00 kG
B-SEXTUPOLE = 0.0000000E+00 kG
D-OCTUPOLE = 0.0000000E+00 kG
D-DECADOLE = 0.000000E+00 kG

        B-OCTUPOLE
        =
        0.000000E+00 kG

        B-DECAPOLE
        =
        0.000000E+00 kG

        B-DDDECAPOLE
        =
        0.000000E+00 kG

        B-14-POLE
        =
        0.000000E+00 kG

        B-18-POLE
        =
        0.000000E+00 kG

        B-120-POLE
        =
        0.000000E+00 kG

                 Entrance/exit field models are sharp edge
FINTE, FINTS, gap : 0.0000E+00 0.0000E+00 5.0000E+00
                  FINTE, FINTS, gap :
  \star\star\star Warning : sharp edge model, vertical wedge focusing approximated with first order kick. FINT at entrance =
                                                                                                                                            0.000
  *** Warning : sharp edge model, vertical wedge focusing approximated with first order kick. FINT at exit =
                                                                                                                                        0.000
                       Integration step : 0.8000 cm
\label{eq:cumulative length of optical axis = 5.84300000 \qquad \text{m ; Time (for ref. rigidity \& particle) = 2.985092E-06 s}
```

9 HISTO	HISTOGRA
	HISTOGRAMME DE LA COORDONNEE Y PARTICULES PRIMAIRES ET SECONDAIRES DANS LA FENETRE : -5.0000E-06 / 5.0000E-06 (CM) NORMALISE
20 19 18 17 16 15 14 13 12 11 10 9 8 7 6 5 4 3 2 1	Y Y Y Y Y Y Y YYYY Y YYYY YYYYYYYYYYYY
	3 4 5 6 7 8
	TOTAL COMPTAGE : 4000 SUR 4000 NUMERO DU CANAL MOYEN : 51 COMPTAGE AU " : 109 VAL PHYS. AU " : 0.000E+00 (CM) RESOLUTION PAR CANAL : 1.667E-07 (CM)
	PARAMETRES PHYSIQUES DE LA DISTRIBUTION : COMPTACE = 4000 PARTICULES MIN = -3.4326E-06, MAX = 3.4347E-06, MAX-MIN = 6.8674E-06 (CM) MOYENNE = -2.853IE-08 (CM) SIGMA = 1.8519E-06 (CM)
TRAJ #1 D,Y ************************************	T,Z,P,S,IEX : 1.0002E+00 9.0257E-07 -2.3996E-01 -1.0770E-06 1.7947E+00 6.09300E+02 1 HISTOGRA
	HISTOGRAMME DE LA COORDONNEE Z PARTICULES PRIMAIRES ET SECONDAIRES DANS LA FENETRE : -5.0000E-06 / 5.0000E-06 (CM) NORMALISE
20 19 18 17 16 15 14 13 12 11 10 9 8 7 6 5 4 3 2 2 1	2 2 22 2 22 2 22 22 22 22 22 22 22 22 22 22 22 22 22 222 22 222 22 222 22 222 22 222 2222222 2 22222222 2 2222222222222222 2 222222222222222222222222222222222222
	1234567890123456789012345678901234567890123456789012345678901 3 4 5 6 7 8
	TOTAL COMPTAGE : 4000 SUR 4000 NUMERO DU CANAL MOYEN : 51 COMPTAGE AU " : 169 VAL. PHYS.AU " : 0.000E+00 (CM) RESOLUTION PAR CANAL : 1.667E-07 (CM)
	PARAMETRES PHYSIQUES DE LA DISTRIBUTION : COMPTAGE = 4000 PARTICULES MIN = -1.9150E-06, MAX = 1.9110E-06, MAX-MIN = 3.8260E-06 (CM) MOYENNE = -3.8539E-09 (CM) SIGMA = 1.1232E-06 (CM)
TRAJ #1 D,Y, ***********************************	T,Z,P,S,IEX : 1.0002E+00 9.0257E-07 -2.3996E-01 -1.0770E-06 1.7947E+00 6.09300E+02 1 IL RAYS ARE Ir at
**************************************	TE RUN AGAIN,

**** FIN D'EFFET DE 'REBELOTE' **** IL Y A EU 20 PASSAGES DANS LA STRUCTURE # PARTICULES ENVOYEES : 4000

FGM PRINCIPAL : ARRET SUR CLE REBELOTE

PART D

Running zgoubi and its post-processor/graphic interface zpop

INTRODUCTION

The **zgoubi** package, including this guide, examples, the **zpop** graphic/analysis post-processor, is available on web [6]. The **zgoubi** *FORTRAN* package is transportable; it has been compiled, linked and executed over the years on several types of systems (e.g. CDC, CRAY, IBM, DEC, HP, SUN, VAX, UNIX, LINUX).

An additional *FORTRAN* code, **zpop**, allows the post-processing and graphic treatment of **zgoubi** output files. **zpop** has been routinely used on DEC, HP, SUN stations, and is now on UNIX and LINUX systems.

1 GETTING TO RUN zgoubi AND zpop

1.1 Making the Executable Files zgoubi and zpop

1.1.1 The transportable package zgoubi

Compile and link the FORTRAN source files (normally, just run the Makefile), to create the executable zgoubi.

zgoubi is written in standard FORTRAN, mostly 77, therefore it does not require linking to any library.

1.1.2 The post-processor and graphic interface package zpop

Compile the FORTRAN source files (normally, just run the Makefile).

zpop links to the graphic library, libminigraf.a [81]. This creates the executable zpop.

zpop is to be run on an xterm window.

1.2 Running zgoubi

The principles are the following:

- Fill up zgoubi.dat with the input data that describe the problem (see examples, Part C).
- Run **zgoubi** no argument needed, by default the input file is assumed to be zgoubi.dat. Specific arguments allow specifying a different input data file name, see below.
- Results of the execution will be printed by default into zgoubi.res and, upon options as appearing in zgoubi.dat, into various additional output files, for instance zgoubi.fai, zgoubi.plt (see section 2 below).
- The command zgoubi accepts the following arguments (see zgoubi_main.f source file) :
 - -in or -fileIn, followed by an the input file name,
 - -out or -fileOut, followed by an output file name,
 - -fileLog, followed by a log file name,

-rank, followed by an integer number, this causes the seed in *MCOBJET* to be overriden, replaced by reading the current time instead,

- -saveExec, this will cause saving a copy of zgoubi exec in the local directory,
- -saveZpop, this will cause saving a copy of **zpop** exec in the local directory.

1.3 Running zpop

- Run **zpop** on an xterm window. This will open a graphic window.
- To access the data plotting sub-menu, select option 7.
- To access the data treatment sub-menu, select option 8.
- An on-line Help provides some information regarding the available post-processing procedures (Fourier transform, elliptical fit, synchrotron radiation spectral brightness, field map contours, tune diagram, etc.).

2 zgoubi OUTPUT FILES

When explicitly requested by means of the appropriate keywords, options, or dedicated *LABEL*'s, extra storage files are opened by **zgoubi** (*FORTRAN "OPEN*" statement) and filled up during the execution.

Their content can be post-processed using the interactive program **zpop** and its dedicated graphic and analysis procedures.

Most of these files are formmatted in columns, plotting their content using 'gnuplot' [85] is straightforward. A library of 'gnuplot' command files can be found in **zgoubi** sourceForge repository [6].

zgoubi procedures that create and fill these extra output files are the following (refer to Part A and Part B of the guide):

- Keywords *FAISCNL*, *FAISTORE*: fill a '.fai' type file (normally named [b_]zgoubi.fai) with particle and spin coordinates and a lot of other informations.
- Keywords SPNPRNL, SPNSTORE: fill a '.spn' type file (normally named [b_]zgoubi.spn) with spin coordinates and other informations.
- Option IC = 2, with field map keywords (e.g. CARTEMES, TOSCA) : fill zgoubi.map with 2-D field map.
- Option IL = 2, with magnetic and electric element keywords: fill zgoubi.plt with the particle coordinates and experienced fields, step after step, all along the optical element.
- Using the keyword MARKER with '.plt' as a second LABEL will cause storage of current coordinates into zgoubi.plt.
- A "PRINT" instruction may appear as an argument in many keywords, for instance CAVITE, MATRIX, ... This results in an output file with name of the form "zgoubi.thisKeyword.out", sometimes "zgoubi.thisKeyword.Out", for instance:

zgoubi.CAVITE.Out (keyword CAVITE), zgoubi.MATRIX.out (keyword MATRIX), zgoubi.OPTICS.out (keyword OP-TICS), zgoubi.PICKUP.out (keyword PICKUPS), zgoubi.TWISS.out (keyword TWISS), etc.

The purpose of this is mostly twofold: allow easy plotting as the data are listed under the form of columns (using gnuplot for instance), and a help in debugging. It is in addition easy to add variables to the Fortran write statement of concern, for more computation information output to zgoubi.*thisKeyword*.out. Lookup "PRINT" in the Index, for details.

Typical examples of graphics that one can expect from the post-processing of these files by **zpop** are the following (see examples, Part C):

• '.fai' type files:

possible plots include phase-space plots (transverse and longitudinal), aberration curves, at the position where *FAISTORE* or *FAISCNL* appears in the optical structure. Histograms of coordinates. Fourier analysis (e.g., spin motion, tunes, in case of multi-turn tracking), calculation of Twiss parameters from phase-space ellipse matching.

• zgoubi.map

possible plots include isomagnetic field lines of a 2-D map. Superimposing trajectories read from zgoubi.plt is possible.

• zgoubi.plt

possible plots include trajectories inside magnets and other lenses (these can be superimposed over field lines obtained from zgoubi.map). Fields experienced by the particles at the traversal of optical elements. Spectral-angular distribution of synchrotron radiation.

zgoubi.spn

possible plots include spin coordinates and histograms, at the position where SPNPRNL appears in the structure. Resonance crossing when performing multi-turn tracking.

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