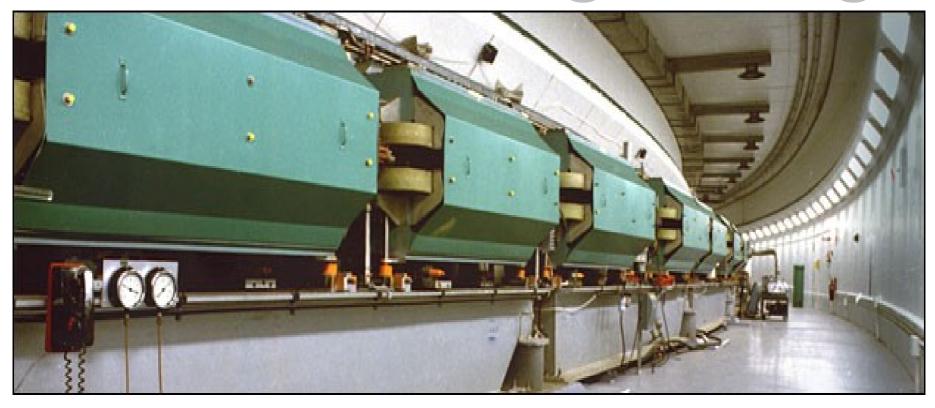
ACCELERATOR



THE PLANET OF THE APPS
OF ACCELERATORS
SBU Physics 2024 PHY691

- Charged particle accelerators are engines of discovery in a number of areas of science: life sciences, matter, energy
- Depending on the area, they are known as "atom smasher", "light source", "spallation neutron source", "neutrino factory", "collider", "hadrontherapy ring" and else
- It has taken close to a century since the emergence of the first founding concepts – for accelerators to reach their nowaday's super hightech level and the important place they now occupy in research and industry

This "tour of the accelerator planet" is organized in the following way:

- Some of the main accelerator classes are introduced following their historical chronology (as a concept or as a real, operational apparatus), which includes
 - (electrostatic accelerators / early XXth century)
 - (betatron / 1923)
 - linear accelerator resonant acceleration / 1924-1928
 - classical cyclotron / 1929, AVF cyclotron / 1938
 - (microtron / 1944)
 - (synchro-cyclotron phase stability / 1945)
 - synchrotron / 1945, strong focusing / 1950
 - (future: wake-field acceleration, ... / ?)
- We explore these accelerator techniques with
 - first, a state-of-the-art, essentially some present top-notch accelerator installations and their usage,
 - a bit of history/theory follows: origin, how the idea arose,
 - conclude showing where the technology is heading toward

We'll keep in mind, in addition, since it gives an understanding of the evolutions, and of preferred technologies depending on the application:

accelerators are "particle factories"

They are fabricated for producing intense beams of particles:

ions of all sorts, radioactive or not, protons, neutrons, neutrinos, photons of all energies from infra-red to gamma, etc.,

For a number of applications :

search for missing mass, supersymmetries, QCD theory, cosmology, cancer treatment, X-lasers, radioscopy, industrial ion implantation, security, and on and on

(electrostatic accelerators)
(betatron)

LINEAR ACCELERATORS

cyclotron

(microtron)

(synchro-cyclotron)

synchrotron

(acceleration techniques of the future)

Example of application (1/2)

Neutron production by spallation, aimed are replacing neutron reactors

• Flux, in modern research reactors, typically: 10¹⁵ /cm²/s

• From spallation sources, i.e., accelerators: 10¹⁷ /cm²/s

A greater flux reduces the time required to conduct an experiment.

(We'll see imilar leap in diverse other sectors, e.g., high photons flux from "light source" synchrotron versus X-ray tubes)

• The two technologies, reactor and accelerator, compete today.

Drawback of the reactor method: requires highly enriched U235, 20%, in some cases "weapon grade" EU, 93% U235 - potential for proliferation. Yet, there are programs to switch to LEU... that's another story!

SNS, Oak Ridge National Lab. Operates since 2006. The largest, highest power, *linear*, proton accelerator in the world.



A gain of 1200 Mev in kinetic energy, over 180 m

i.e., an average 7 MeV/m

that's the sate-ofthe-art A 180 m long, 2K frigidaire





Commissioning		2006
SCL linac length	m	180
Kinetic energy	GeV	1
Beam power	MW	1.4
Repetition rate	Hz	60
Duty factor (df)	%	6
Peak current (Ip)	mA	23
Average current	mA	1.4



 $= Ip x df \sim 23[mA] x 6[%]$

Example of application (2/2)

Free-Electron Lasers

FEL

Interest:

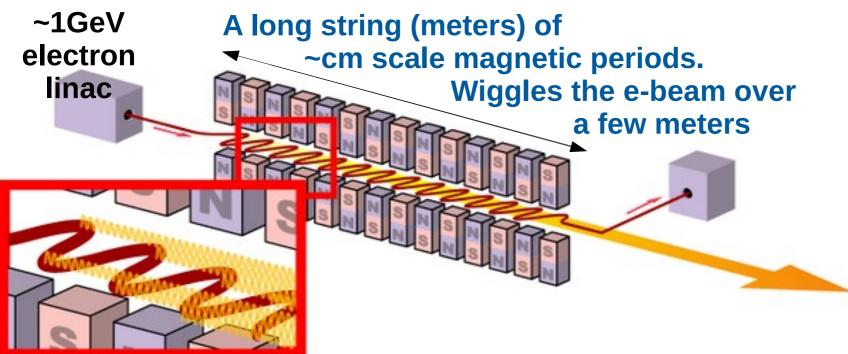
- laser-like, high energy (e.g., X) photon beams

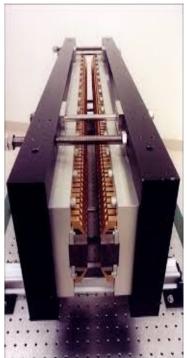
Applications:

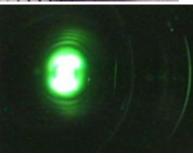
- applied research (condensed matter, ...)
- particle beam manipulations (e.g., beam cooling)

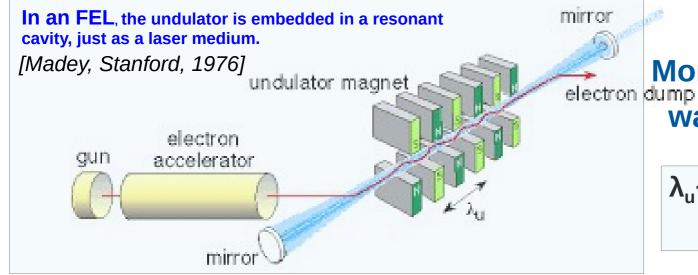
Undulator radiation

[Motz et als., Stanford, 1953]





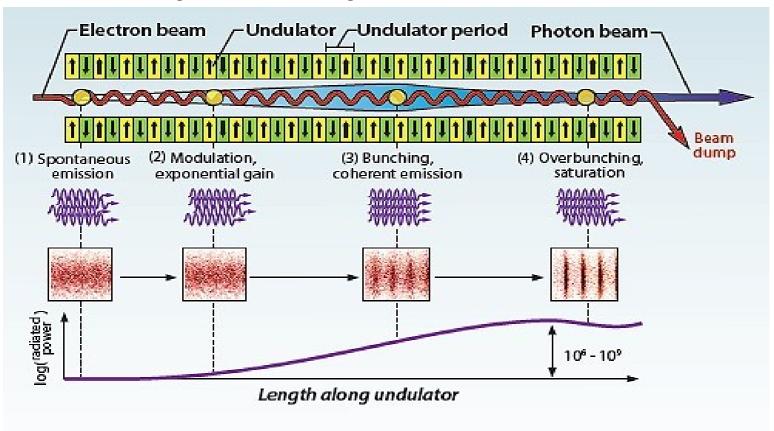




Monochromatic light spot, dump wavelength, $\lambda \sim \lambda_u / (2y^2)$

 λ_u ~ cm and y=2000*E_[GeV] $\rightarrow \lambda$ ~ nm laser beam

A derivative: SASE-FEL Self-Amplified Spontaneous Emisson

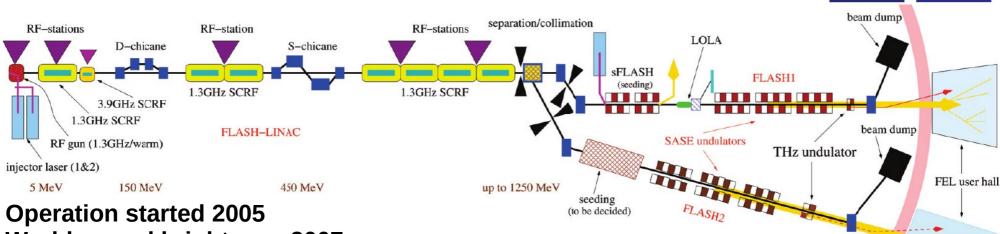


- Principle : the longitudinal density of the \sim 10s μ m long e-bunch modulates into a set of short sub-bunches, each with length \sim λ .
- Thus: partial radiation coherence, power from sub-bunch ~(Ne)² rather than (incoherent) power~N e², i.e., high brightness highly collimated femtosecond X-ray pulses.

 Can make life science X-movies!

FLASH SASE FEL INSTALLATION, **HAMBURG** FLASH2 COMMISSIONING





World record brightness 2007

European X-FEL followed: 2.1 km linac, 17.5 GeV, Å/fs pulses. Started 2017

e-:		
emittance $\beta \gamma \varepsilon_{x,y}$		
(1 nC, on-crest, 90% rms)	1.4	mm mrad
charge	0.08 - 1.0	nC
peak current	0.8 - 2.0	kA
beam energy	380 - 1250	MeV
bunches / train	1 - 450	
bunch spacing	1 - 25	μ s
train repetition frequency	10	Hz

γ (FLASH1):		
wavelength (fundamental)	4.2 - 45	nm
average single pulse energy	10 - 540	μJ
pulse duration (fwhm)	<30 - 200	fs
spectral width (fwhm)	0.7 - 2.0	%
peak power	1 - 3	GW
peak brilliance	$10^{29} - 10^{31}$	(+)
average brilliance	$10^{17} - 10^{21}$	(+)
(+): photons/(s mm ²	mrad ² 0.1%	bw)

Linear accelerators

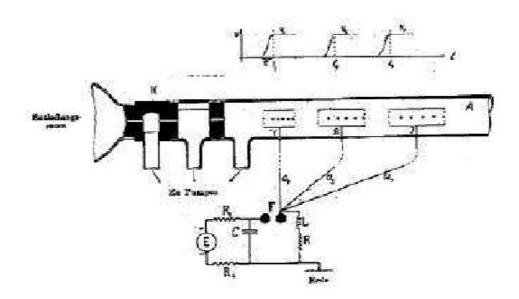
where they come from

Ising linac

- 1924, Ising proposes the acceleration using a variable electric field between drift tubes (the father of the Linac).
- The potential wave is applied to the gaps via wires (a1, a2, a3...) with adjusted lengths to ensure synchronism.

A consequence: only works if velocity increases with time → non-relativistic regime.

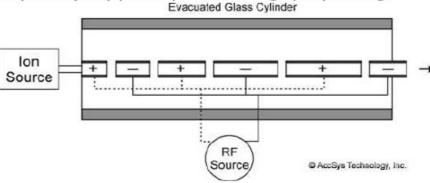
- Between gaps, particle bunchlets travel with constant velocity within drift tubes 1, 2, 3.
- It appeared not technologically possible to achieve a practical accelerator.
 - difficulty of spark excitation
 - inefficiency of wire transmission lines

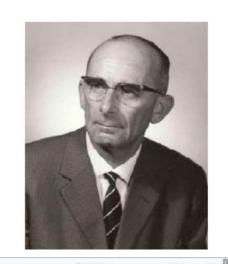


Wideroe linac (1/3)

Ising's principle of

- 1928, Rolf Wideroe in Berlin first demonstrates resonant acceleration by applying Ising principle using a 1 MHz, 25 kV generator, connected to drift tubes forming a series of successive gaps.
- He succedes accelerating potassium ions in that structure, up to 50 keV,
- achieving the resonance required correlation between the various parameters: type of ion, RF frequency, applied potential, gap spacing.





First Wideroe's linac

1453

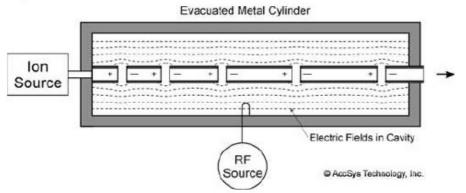
- Drift tubes with increasing length are arranged along beam propagation axis They act like Faraday cage: bunch inside tube feels no field
- They are applied $U(t) = U_0 \sin(\omega t)$. At a given time, potential alternates from one gap to the next (" π " mode accelerating structure)
- U(t) causes accelerating (or decelerating) gradient between tubes during half a period
- After n gap, a particle at (constant) phase ϕ with the wave has $E_n = nqU_0\sin\phi$
- Distance between gaps n and n+1 is (with v_n =velocity, T =RF period = $2\pi/\lambda$) $d_n = v_n T/2 = \beta_n \lambda/2$
- A straightforward, fundamental effect of this resonance method is "beam bunching".

Alvarez linac (1/2)

- The development of radar technology during WWII offered pulsed, high power, up to GHz RF generators ("magnetron", "klystron"), so allowing wavelengths in meter range (appropriate for ions v/c < 1) to cm range (electrons, $v \approx c$).
- 1946, L. Alvarez and coworkers at the Lawrence Berkeley Radiation Laboratory developed a proton linear accelerator based on injection of 200 MHz RF wave into a resonant metallic cylindrical

cavity containing the wideroe-type drift tube arrangement.

- the linac is injected with a 4 MeV electrostatic accelerator
- protons are accelerated up to 32 MeV in the Alvarez structure



Contribution in elementary particle physics

Remember, Wideroe's tubes were in a glass cylinder (strong antenna-like power losses), they were connected to an AC generator.

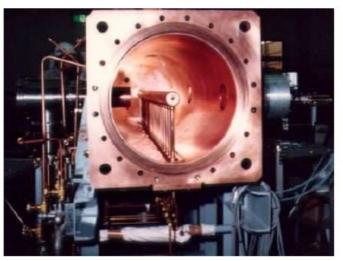
- Transverse focusing: ensured at gaps by grids shaping the (varying) E field.
- RF phasing : an accelerating standing wave fills the cavity. The particular resonant mode of interest (amongst oodles) is that with all gaps having the same polarity (" $\beta\lambda$ " or " 2π " accelerating mode)
- Evolutive geometry of the tubes (length & diameter) with distance causes cells to resonate on identical frequency.

Alvarez linac (2/2)

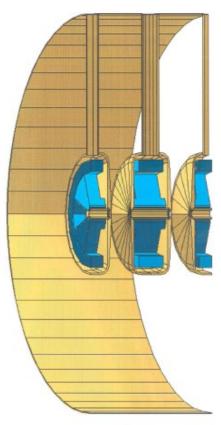
- Later on longitudinal focusing (phase stability) would be invented, ensuring best transmission. Transverse focusing today ensured with quadrupoles located in the drift tubes.
- DTLs are nowadays currently used as primary injection stages in hadron linac chains, or as injectors into synchrotrons.



202M Hz/70 MeV Alvarez injector linac at ISIS, RAL.



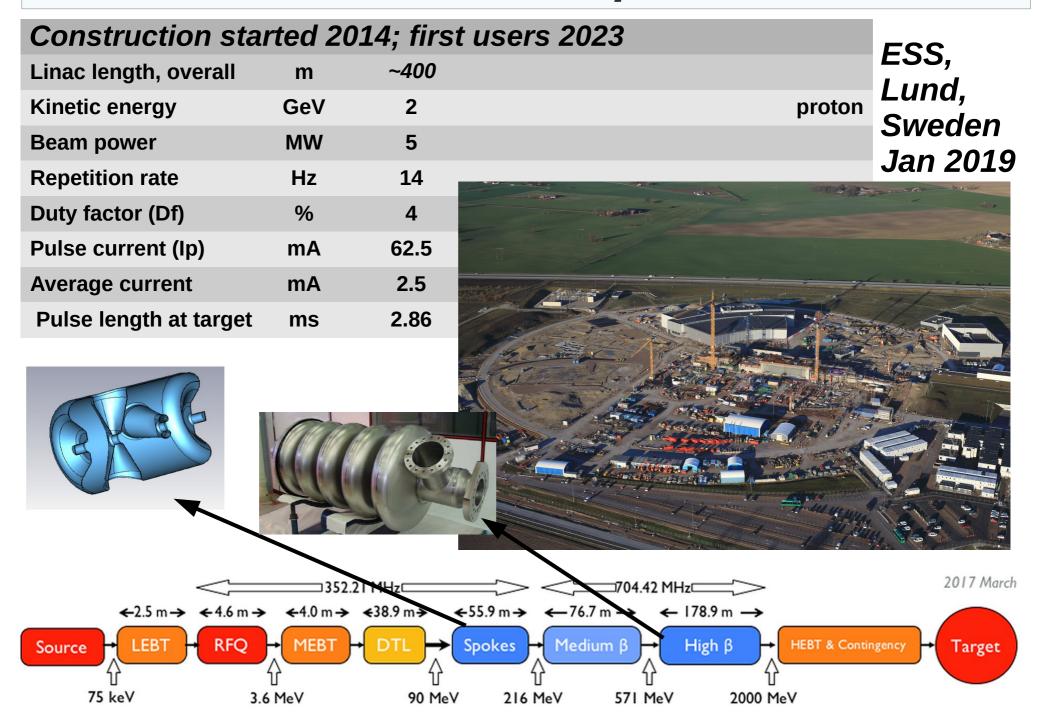
7 MeV Alvarez DTL, typical injector of medical synchrotron: pre-acceleration of protons or Carbons before injection into synchrotron.



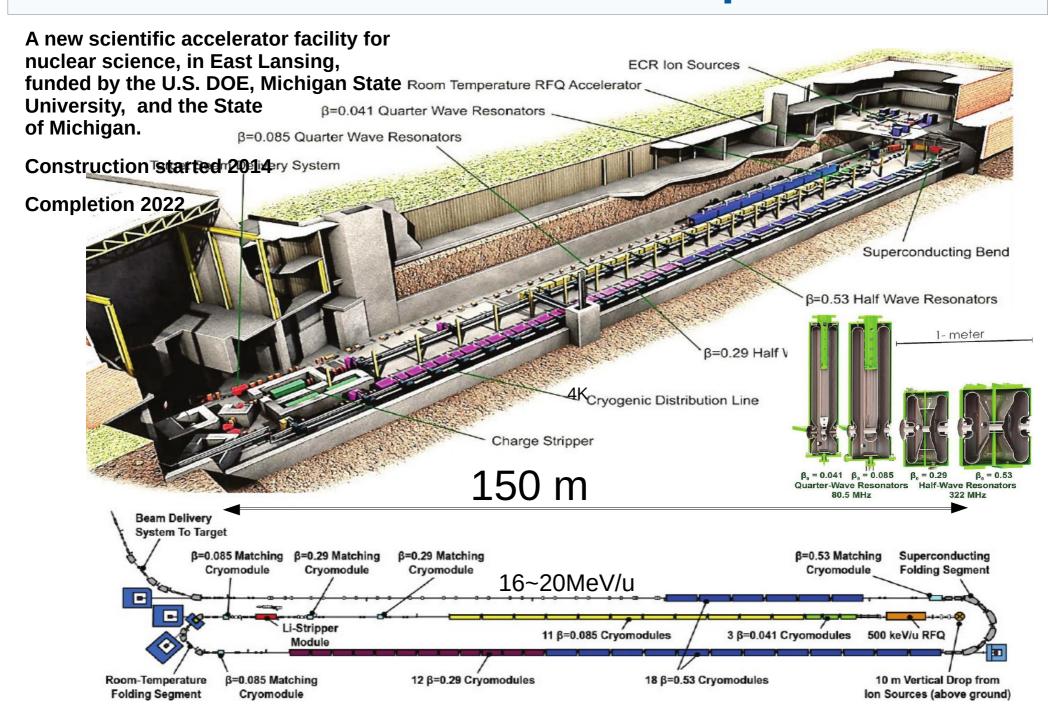
Quadrupoles in drift tubes.

Going where, nowadays?

* More sns: ESS, the EU spallation source *



* Intense beams of rare isotopes - FRIB *



* ENERGY * ACCELERATOR-DRIVEN SUBCRITICAL REACTOR



(600 MeV - 4 mA proton)

Reactor

- · Subcritical or Critical modes
- 65 to 100 MWth

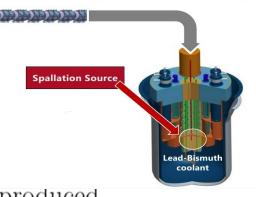


MYRRHA, Belgium

Multipurpose hYbrid Research Reactor for High-tech Applications
A flexible and fast spectrum irradiation facility

• Required beam power P_B , for P_{th} reactor power : With beam energy $\mathbf{E}_B \approx 1$ GeV, a handy estimate is

$$P_B \approx \frac{1}{2}(1 - k_{\text{eff}}) P_{\text{th}}$$



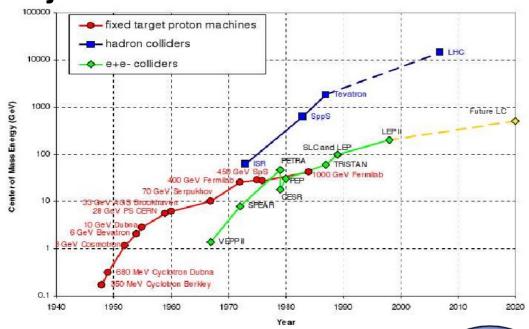
$$P_B = E_B \frac{P_{\rm th}}{f \, E_f} \frac{(1-k_{\rm eff})}{k_{\rm eff}} \begin{cases} k_{\rm eff} = {\rm neutron \ multiplication \ factor} = \frac{{\rm n \ produced}}{{\rm n \ absorbed}} \approx 0.95 - 1^{-1} \\ E_f = {\rm fission \ energy} \approx 200 {\rm \ MeV} \\ f = {\rm fraction \ of \ neutrons \ causing \ fission} \overset{1GeV-p}{\approx} \frac{20{\rm n/incident \ p}}{2.5{\rm n/fission}} \end{cases}$$

 \bullet $k_{\rm eff}$ is central to the accelerator parameters, the closer it is to 1, the lower the beam power to be brought in - but, drawback, the closer the reactor core to critical.

- Typical numbers -					
	ADS thermal power	$k_{ m eff}$	Proton beam Energy / Current / Power		
Demo transmuter MYRRHA:	50-100 MW-th	≈ 0.95	600 MeV / 4 mA / 2.4 MW		
EFIT industrial transmuter:	several 100 MW-th	≈ 0.97	800 MeV / 20 mA / 16 MW		
China's demonstrator program:	1000 MW-th		1.5 GeV / 10 mA / 15MW		

* High Energy Physics *

The international linear e+e- collider, a long history in itself. **Objective 2030s?**





~50MV/m



A Higgs factory - mass 125 GeV

 The CM energy available in a col wo particles, (1), (2), writes

$$E_{CM} = \sqrt{M_1^2 + M^2} \frac{1}{2\pi i v_1} \frac{1}{V_2 \gamma_1 \gamma_2} \frac{1}{(1 + M^2)^2} \frac{1}{\beta_2 \gamma_1 \gamma_2} \frac{1}{(1 + M^2)^2} \frac{1}{\gamma_2 \gamma_1 \gamma_2} \frac{1}{(1 + M^2)^2} \frac{1}{(1 + M^2)^2} \frac{1}{\gamma_2 \gamma_1 \gamma_2} \frac{1}{(1 + M^2)^2} \frac{1}{(1$$

- Considering particles with the san V ass M, in fixed target collision mode, incoming beam with energy E, one gets

saus roof & are accelerator energy The energy available ses as the

define particles on the same m ss M, in collider mode, beams with respective Marini Parini Pa ollision, one gets

(electrostatic accelerators)

(betatron)

linear accelerators

CYCLOTRONS

(microtron)

(synchro-cyclotron)

synchrotron

(acceleration techniques of the future)

Example of application (1/2)

High power, PSI, 600 MeV, 1.4 MW, CW

1973

1 Hans Willax

2 Miguel Olivo

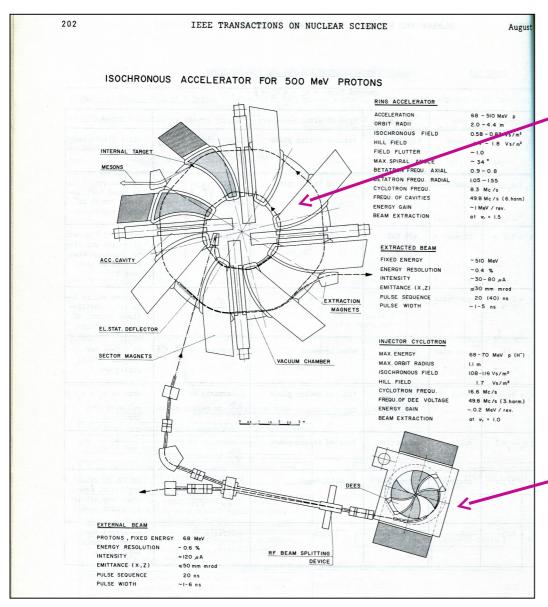
3 Thomas Stammbach

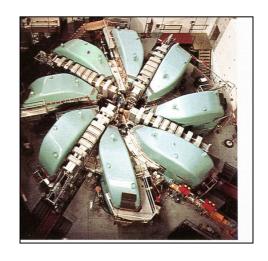
4 Werner Joho

5 Christa Markovits



1966: SIN early Design – Feb. 1974:1st 100 μ A beam



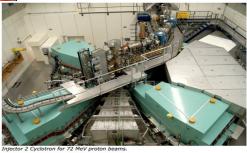


The 590 MeV Ring Cyclotron



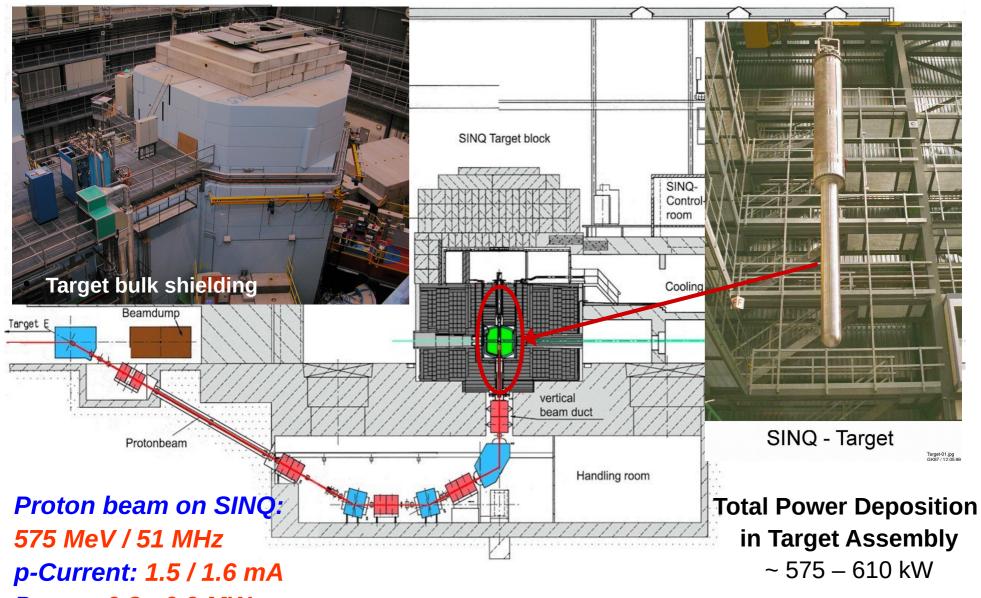
The old 72MeV Philips injector

Nowaday's 72MeV injector



escription

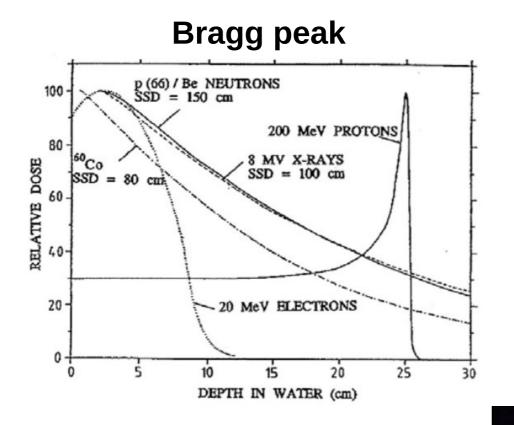
Neutron production at SINQ

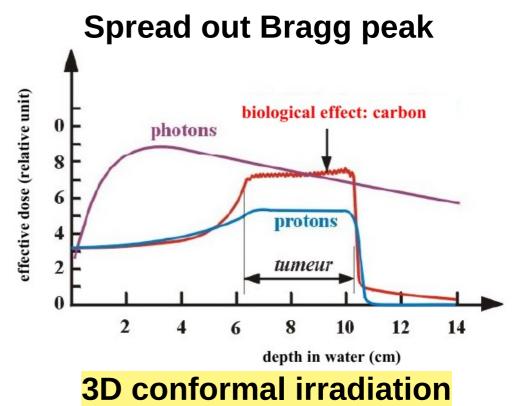


Power: 0.8 - 0.9 MW

Example of application (2/2)

Cancer tumor treatment "protontherapy"





Medical cyclotrons by IBA industrial company



Figure 2. IBA 230 MeV resistive cyclotron for proton therapy

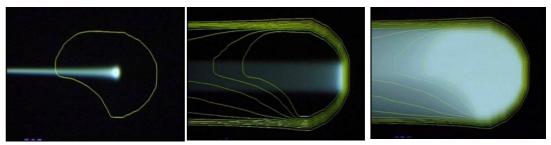


Figure 3. Gantry Treatment Room of the IBA Proteus Proton Therapy System

Ref.: Proceedings of CYCLOTRONS 2010, Lanzhou, China, REVIEW ON CYCLOTRONS FOR CANCER THERAPY, Yves Jongen#, IBA, Louvain-la-Neuve, Belgium

Protontherapy at the PSI national research center (uses a 250 MeV superconducting cyclotron)





Spot-scanning technique, developed at PSI

Through the scanning and superposition of dose-spots of a proton pencil beam, the desired dose distribution can be built up, and the dose can be precisely tailored to the 3-dimensionnal shape of the tumour.

Ref.: https://www.psi.ch/protontherapy/center-for-proton-therapy

Where cyclotrons come from

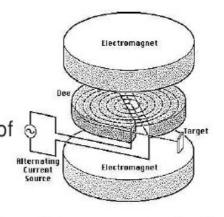


For his invention of the cyclotron

Cyclotron (1/5)

1929-1930, Ernest O. Lawrence inspired by Wideroe
 & Ising ideas invents (the principle of) the cyclotron :

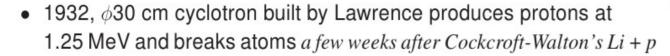
having read Wideroe's paper, he speculated on the use of a magnetic field to bring the particle back to a *single* accelerating gap next to acceleration.





- Doing so he found that the revolution frequency in uniform B is constant : the "cyclotron angular frequency", $\omega_0 = qB/m$

- That allows RF gap voltage at constant frequency, $f_{RF}=qB/2\pi m$.
- 1931, Stanley Livingston, Berkeley, demonstration with 5-inch cyclotron by acceleration of hydrogen ions up to 80 KeV (about 40 turns up to $r \approx 4.5$ cm).



- 1934, Berkeley, E.O. Lawrence builds a 27-inch cyclotron, accelerates protons to 3 MeV and D to 5 MeV
- 1939, E. O. Lawrence receives the Nobel Prize "for the invention and development of the cyclotron and for results obtained with it, especially with regard to artificial radioactive elements".

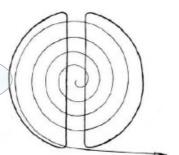


The device is inserted in the gap of an electromagnet.

• That was just the beginning of a lasting story, yet...

Cyclotron (2/5) - classical

Non-relativistic cyclotron



With B constant in time and uniform in space, as particles gain energy from the rf system, they stay in synchronism, but spiral outward in r.

- orbit :
$$r = v/\omega_0 = mv/qB$$

- focusing (1):

$$F_z = qvB_r pprox qvrac{\partial B_r}{\partial z}$$
z $\equiv qvrac{\partial B_z}{\partial r}$ z

$$\ddot{z} - \tfrac{qv}{m} \tfrac{\partial B_z}{\partial r} \mathbf{z} = 0 \to \omega_z^2/\omega_0^2 = \nu_z^2 = - \tfrac{r}{B_z} \tfrac{\partial B_z}{\partial r} = -k, \qquad \boxed{\nu_z = \sqrt{-k}}.$$

$$\nu_z = \sqrt{-k}$$
.

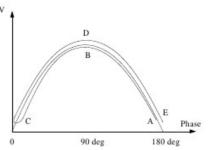
hence the field index k needs be negative: B_z is slowly decreased with radius.

Similarly, $|\nu_r = 1 + k|$. This sets the requirement |-1 < k < 0|

- focusing (2): is also ensured at lower energy by the electric field.
- isochronism :

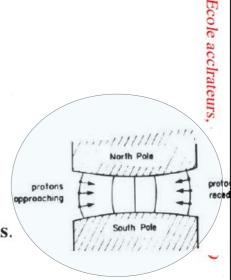
The condition for vertical focusing, -1 < k < 0 (B is not constant), spoils the isochronism.

As a consequence, the phase is not constant (ABCDE path)



- bunching: particle beam injected into the cyclotron necessarily gets bunched, at the frequency of the RF (the time interval between two bunches is an RF period)
- The classical limit ($\gamma \approx 1$) is ~25 MeV for protons, 50 MeV for D and α , (about 2-3% increase in mass), GANIL in Caen accelerates Carbon to about 100 MeV/u...
- That was enough energy to transmute all nuclei... The classical cyclotron allowed discovering oodles of nuclear reactions and isotopes.

Yet, let's keep in mind: transmutation was not the all story



Cyclotron (3/5) - classical

- Relativistic energies, the bad news :
 - The cyclotron resonance $\omega_0=qB/\gamma m$, with $r=\beta c/\omega_0$ yields $k=\frac{\beta}{\gamma}\frac{\partial\gamma}{\partial\beta}=\beta^2\gamma^2$
 - so k cannot satisfy -1 < k < 0,

isochronism requires that $B(r) \propto \gamma$, which yields vertical defocusing...

ullet That was the end of the story, $\sim 25\,\mathrm{MeV}$ protons, etc... :

Hans Bethe (1937): The "encouraging" comment...

"... it seems useless to build cyclotrons of larger proportions than the existing ones... an accelerating chamber of 37 cm radius will suffice to produce deuterons of 11 MeV energy which is the highest possible..."

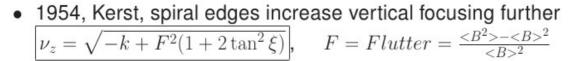
Frank Cole : "If you went to graduate school in the 1940s, this inequality (1 < k < 0) was the end of the discussion of accelerator theory."

Until...

... smarter!

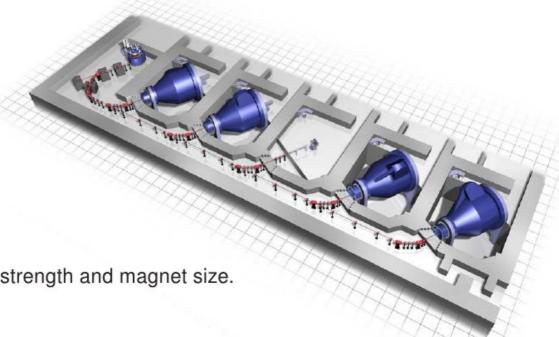
Cyclotron (4/5) - Thomas focusing

 1938, L.H. Thomas, "The Paths of Ions in the Cyclotron", introduces the "Thomas focusing", based on separate sector bending, namely, "edge-focusing",

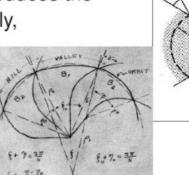


- That allowed having B(r) increase in proportion to γ , so to ensure constant RF frequency ($\omega_0 = qB/\gamma m$), while *preserving vertical focusing*.
- Modern cyclotrons still rely on these principles





• Cyclotron is limited in energy by its field strength and magnet size.

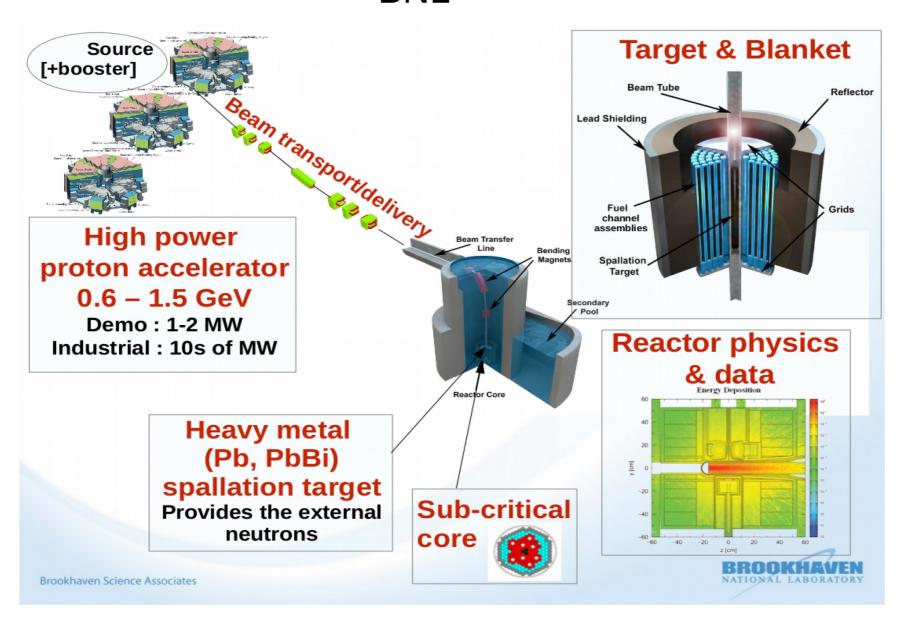


For N=+ cot 7/2 1930s

Cyclotrons,
going where
nowadays?

MORE HIGH POWER?

* ACCELERATOR-DRIVEN SUBCRITICAL REACTOR * - BNL -



On-going discussion : which is optimal in the ADS application ?

Reference : US ADS White Paper (2010)

• Separate sector cyclotron

Paul Scherrer Institute, 590 MeV, 1.3 MW CW beam First beam 1973

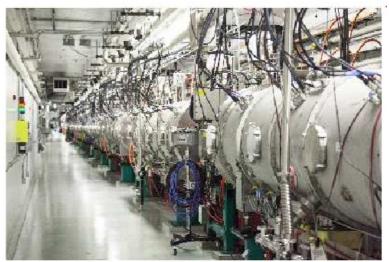
• Normal conducting proton linear accelerator



LANSCE 800 MeV n science center linac, first beam 1972. Ran in 1 mA / MW range in the 1980s, 120 Hz repetition rate, DC 7.5%.

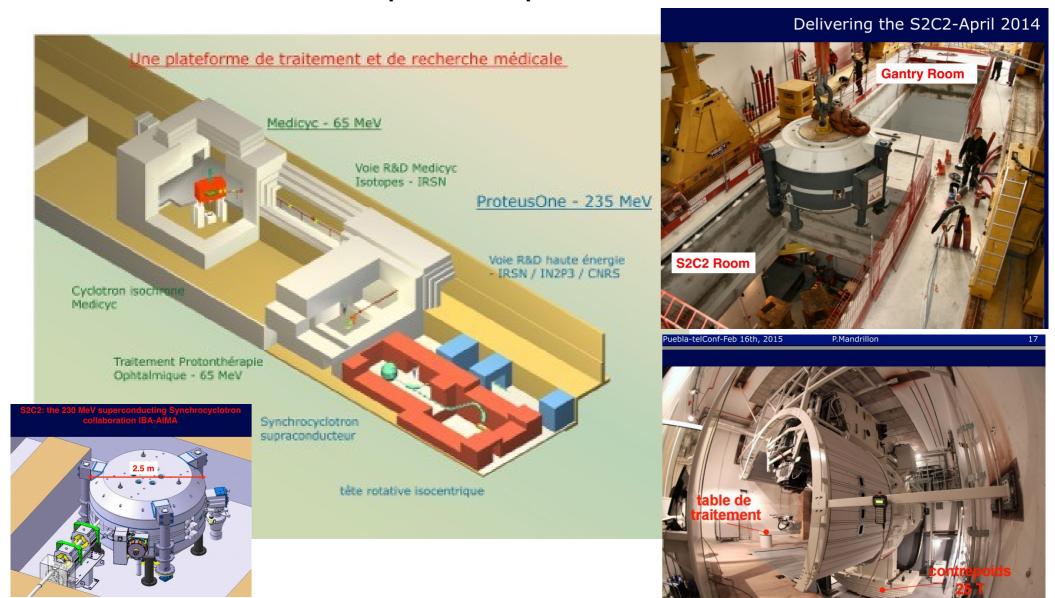
• Superconducting linear accelerator

SNS 1 GeV n science linac at ORNL, beam power 1.2 \sim 1.4 MW. Pulsed, DC \sim 6%. Accelerates H- for stripping injection into accumulator ring, First beam 2006



MORE MEDICAL & ISOTOPE PRODUCITON

New, S2C2 technology, MEDICYC, NICE (F) 250 MeV, super-compact, first beam 2016



(electrostatic accelerators)

(betatron)

linear accelerators

cyclotrons

(microtron)

(synchro-cyclotron)

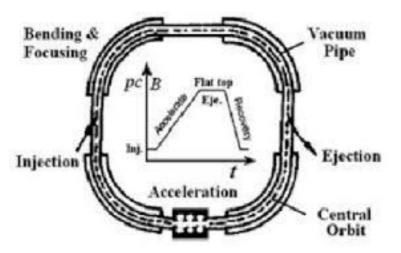
synchrotron

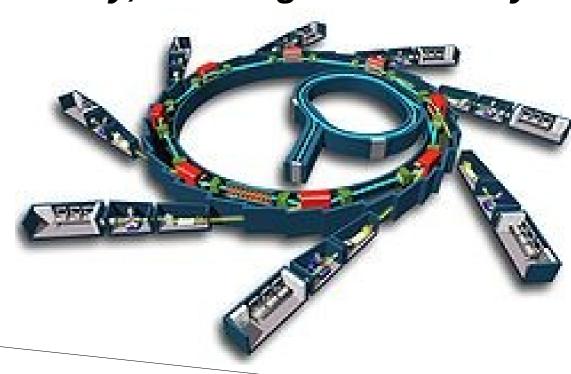
acceleration techniques of the future

synchrotron

Fancy, ~GeV light source style

Basic



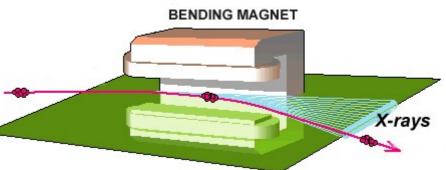


Beam focusing + guiding:

QUADRUPOLE LENS

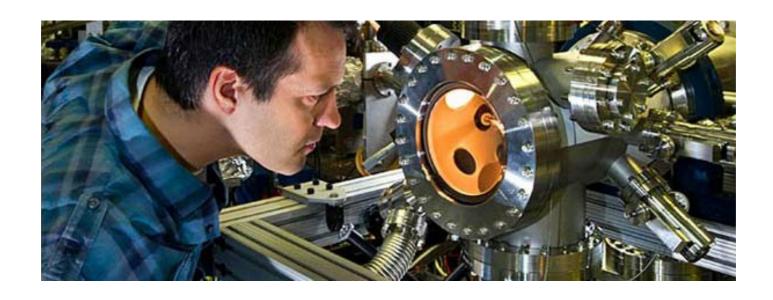




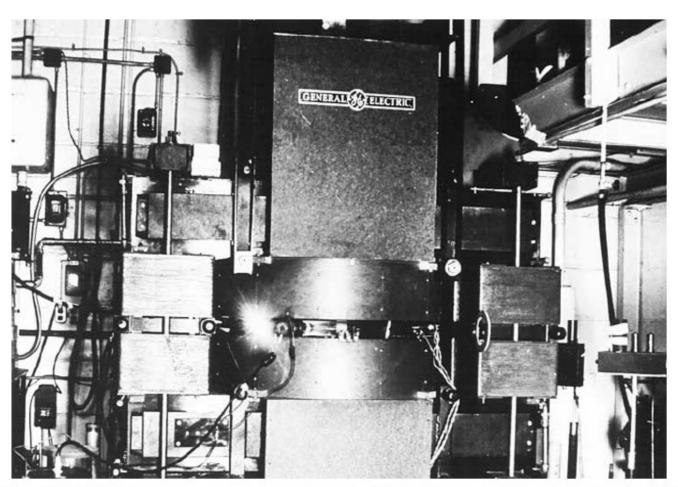


Synchrotron radiation in bonus!

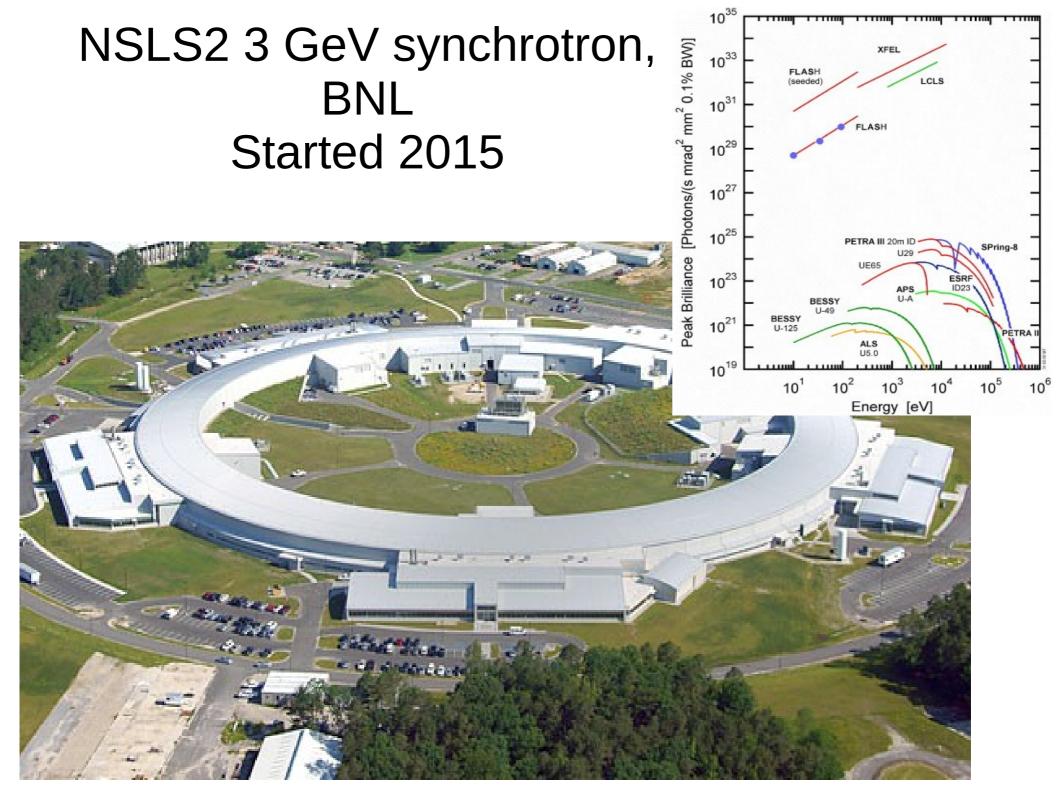
LIGHT SOURCES



How this started



The 300 MeV electron synchrotron built at General Electric Co. in 1940s. The photograph shows the synchrotron radiation emitted from the accelerator.

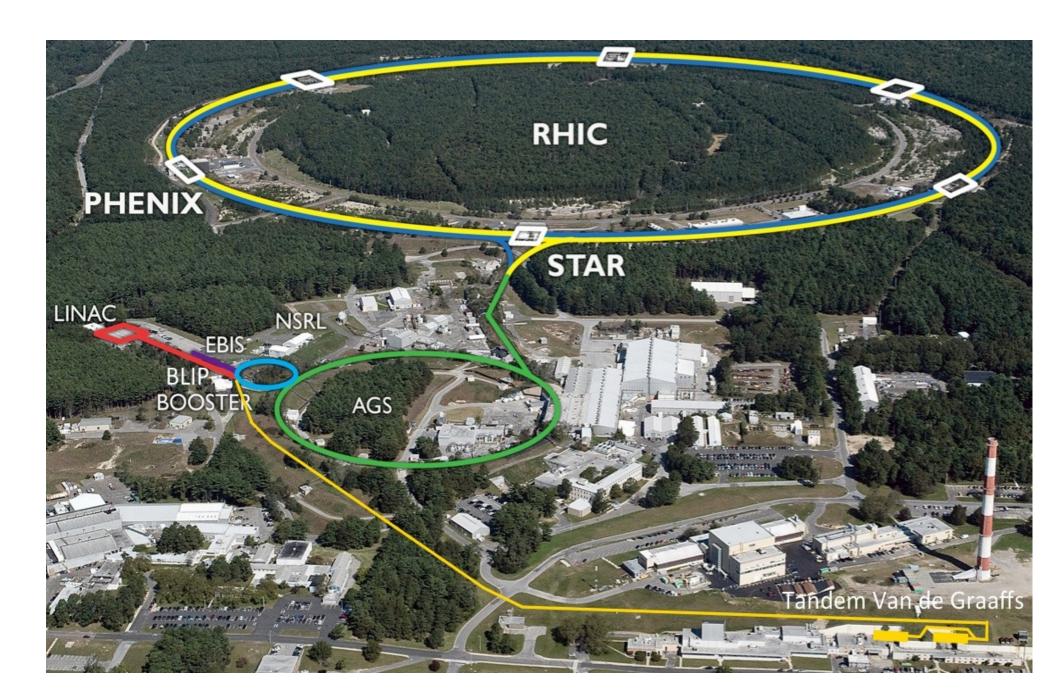


10³¹

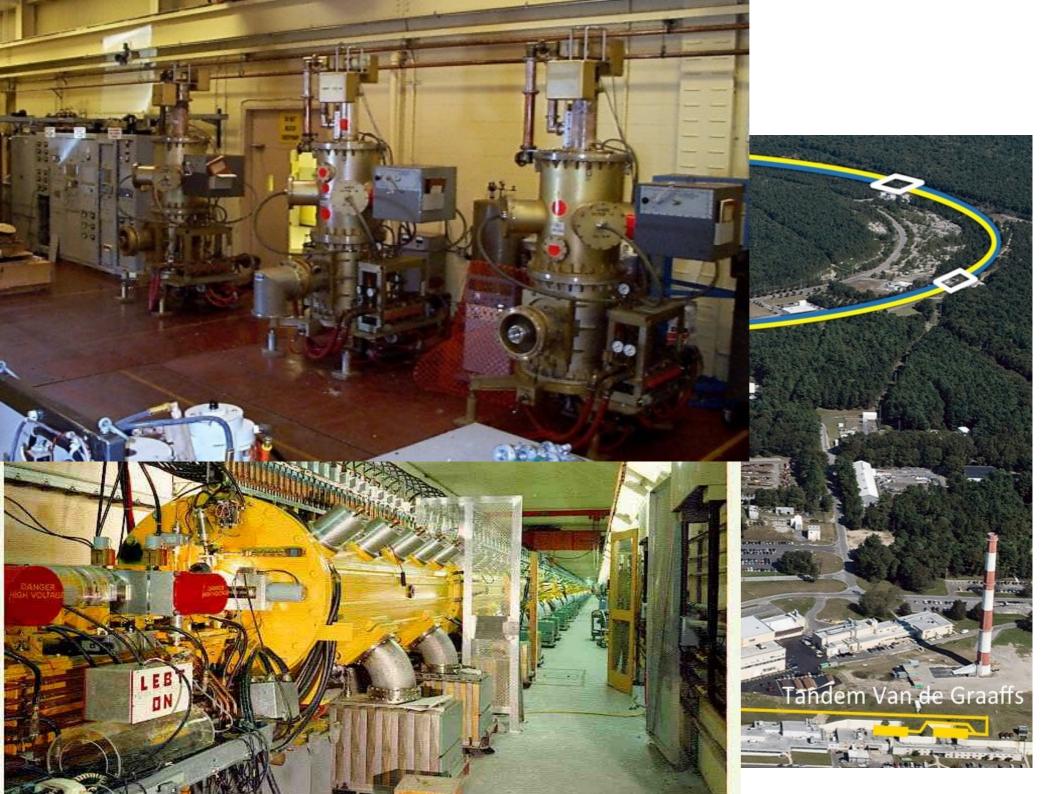
Nuclear research

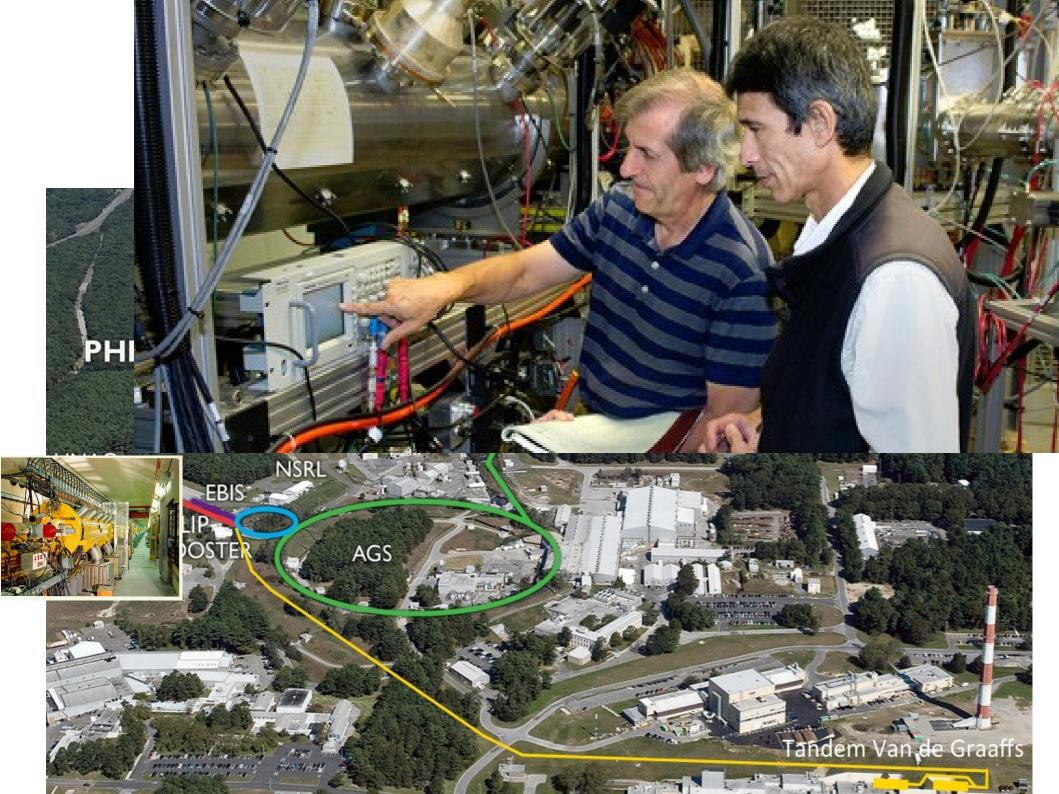
1 of the 2
LARGE COLLIDERS
ON THIS PLANET

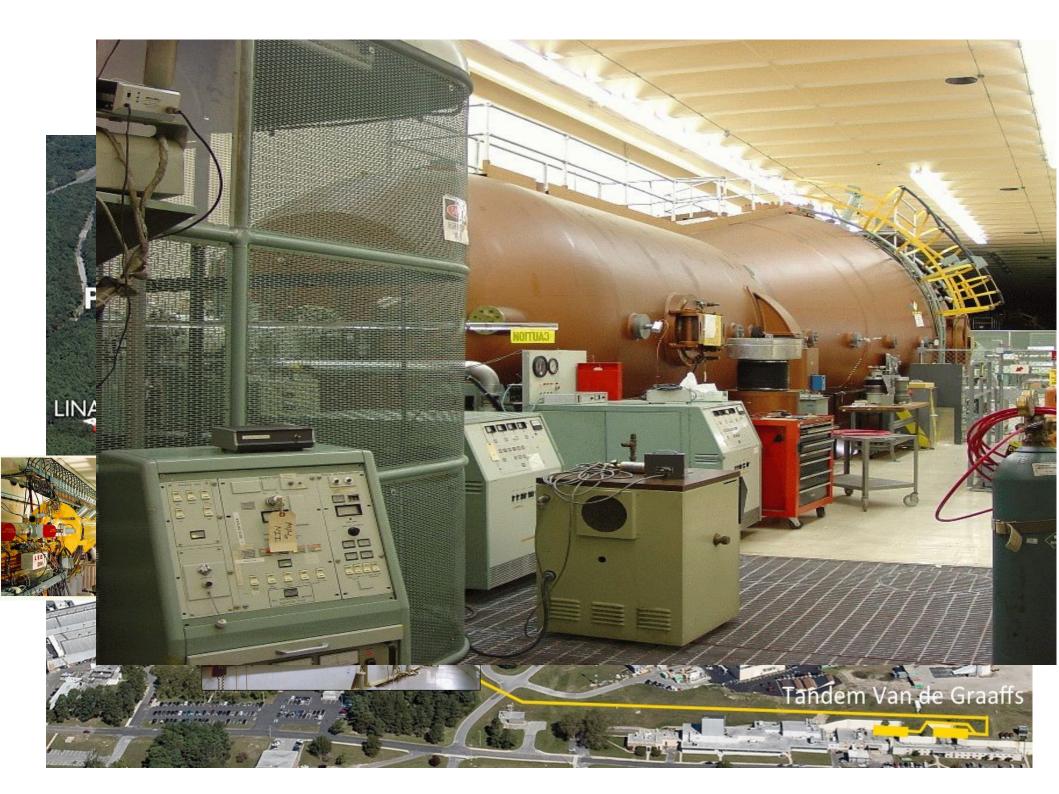
RHIC

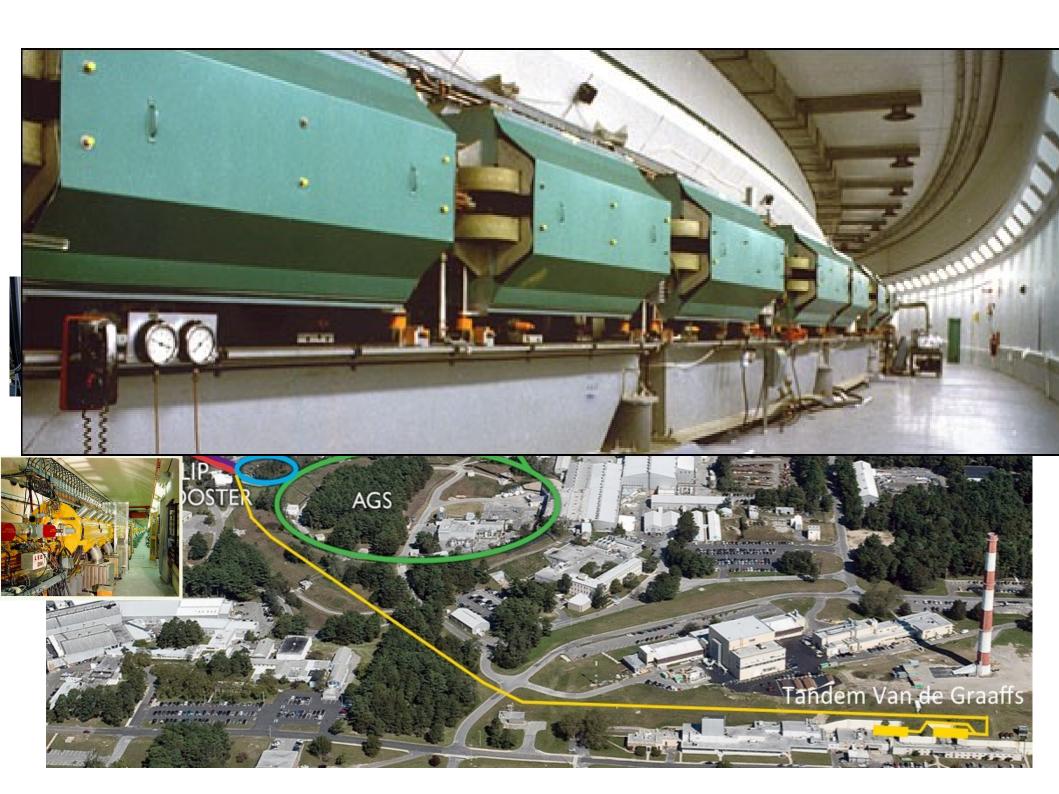




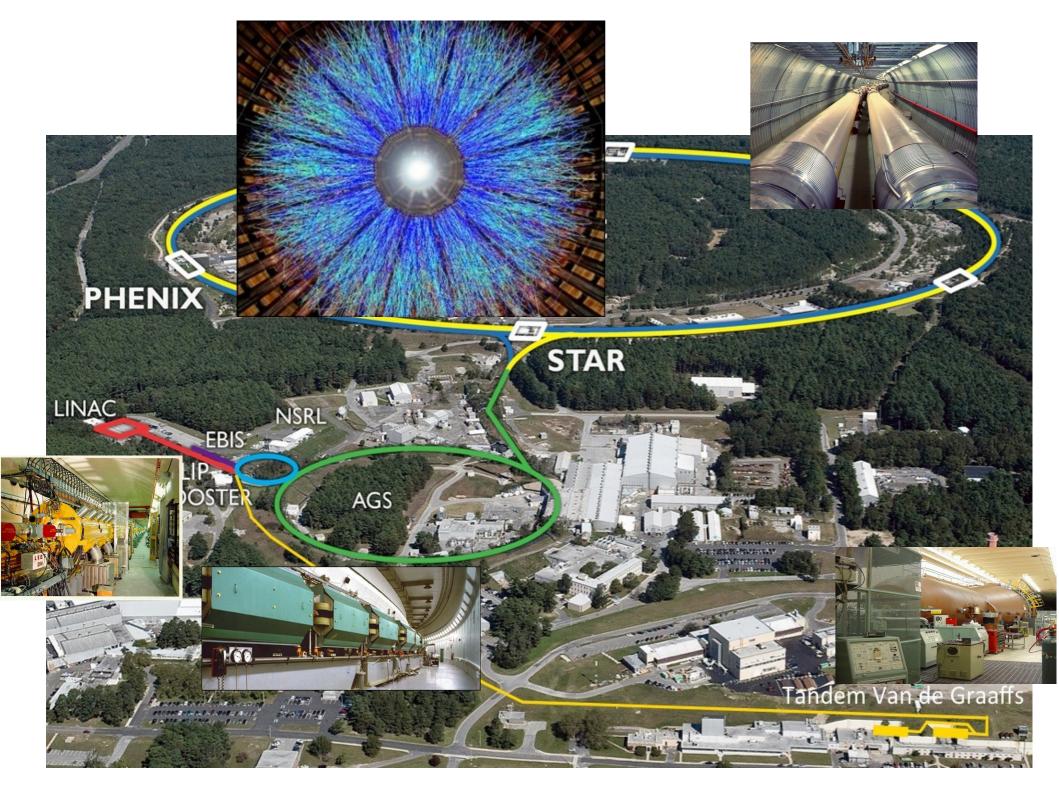












HEP

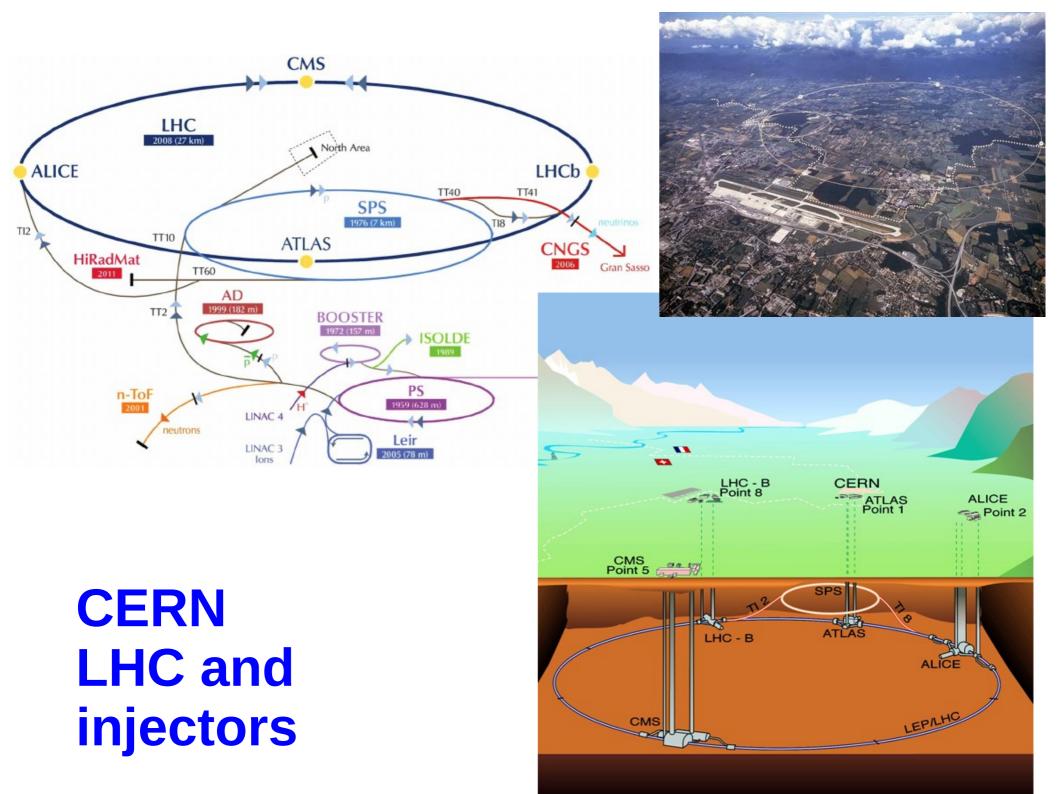
The largest collider: LHC

Construction started ~2000, first run : 2009 Energy 6.5 TeV per beam, 13 TeV CM

Discovery of Higgs Boson announced in 2012

10,000 people from 113 different countries contribute to science at the LHC

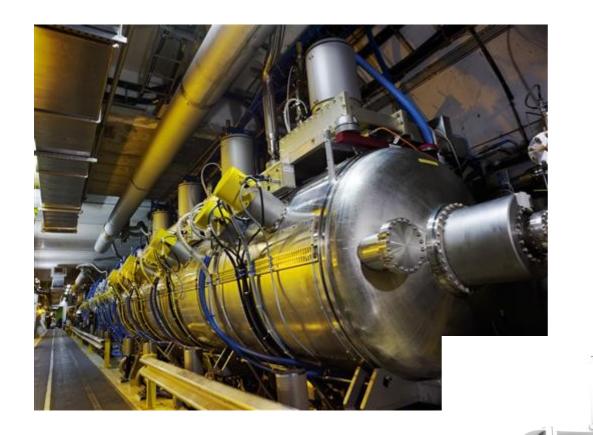




LHC DIPOLE: STANDARD CROSS-SECTION "2-in-1" design Interconnecting magnets



LHC SUPERCONDUCTING RF CAVITIES

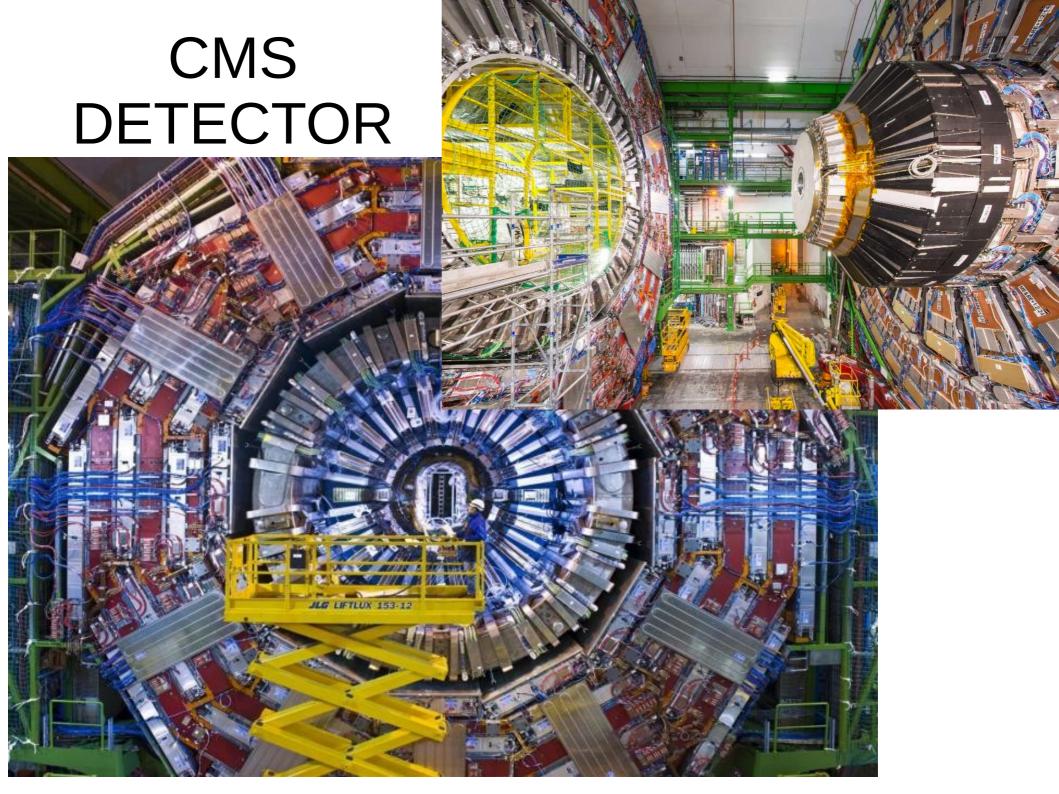


CONTROL ROOM



ATLAS DETECTOR





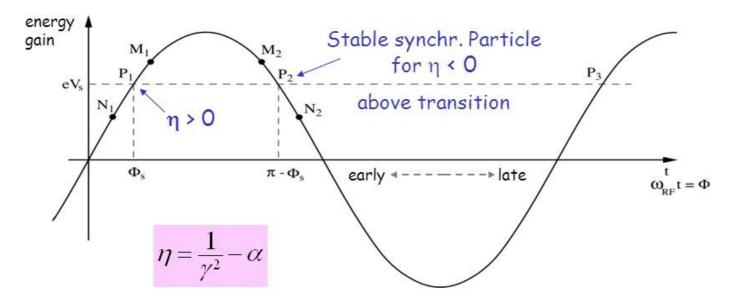
Synchrotrons, where from?

1944-Veksler; 1945-McMillan: discovery of phase stability - "longitudinal focusing". This is how it works.

Phase Stability in a Synchrotron

From the definition of η it is clear that an increase in momentum gives

- below transition (η > 0) a higher revolution frequency (increase in velocity dominates) while
- above transition ($\eta < 0$) a lower revolution frequency ($v \approx c$ and longer path) where the momentum compaction (generally > 0) dominates.



Cyclotron style "weak focusing" optics, at that time (dipole index 0<k<1)

1947: First observation of synchrotron light (SR), not fully understood (spectrum etc.) - Julian Schwinger would develop a full theory of SR in a circular accelerator

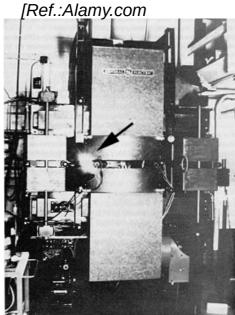


Vaccum chamber of GE

synchrotron

alamy stock photo

70 MeV synchrtron, GE



1946, Aug.: First synchrotron operation, 8 MeV proof-of-principle, by Goward in Woolwich, UK

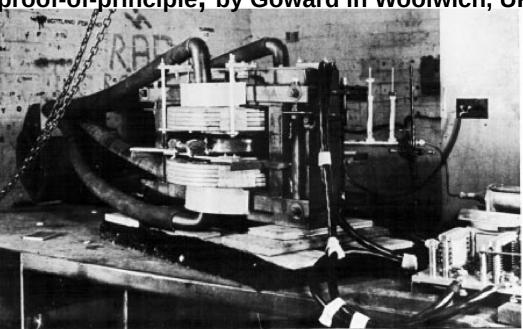
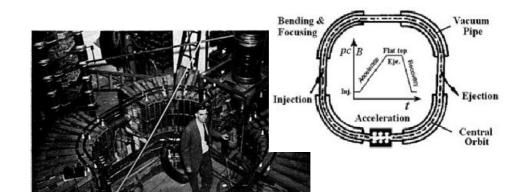


Fig. 4: The world's first synchrotron, installed at Malvern. The extra cooling system and RF feed to the resonator may be clearly seen.



The first "racetrack" sybnchrotron with straight sections, 300 MeV electron, University of Michigan, 1949.

STRONG FOCUSING: Invented in 1950

Strong index |k| > 1 + alternating gradient (k<0, k>0)



Hyperbolic gap, V=a xy
BF
BD

Magnetic pole

Magnetic pole

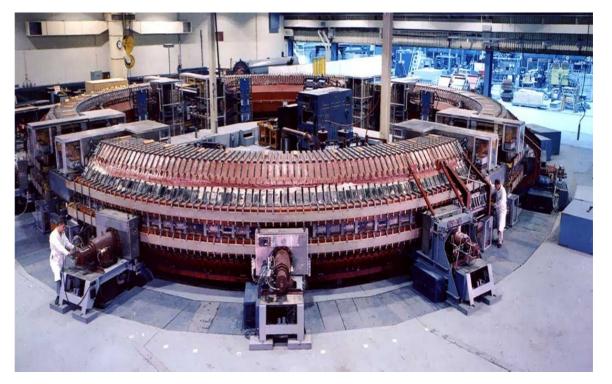
B

Mag

PS (1959), 30 GeV: few cm diameter vacuum chamber

Compare the dipoles:

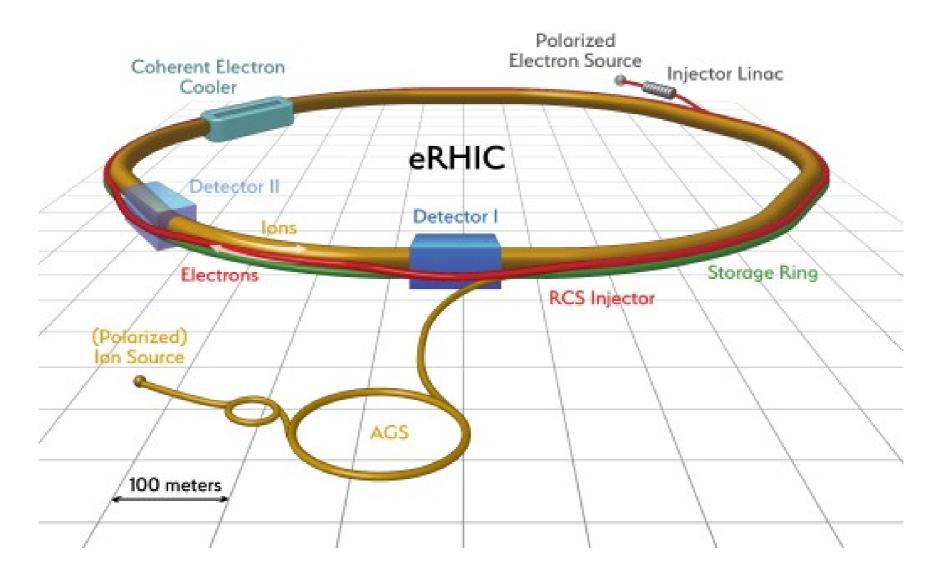
Cosmotron, 3 GeV: 1.22mx0.22m vacuum chamber



What's next?

eRHIC e-A collider at BNL

Want to join?

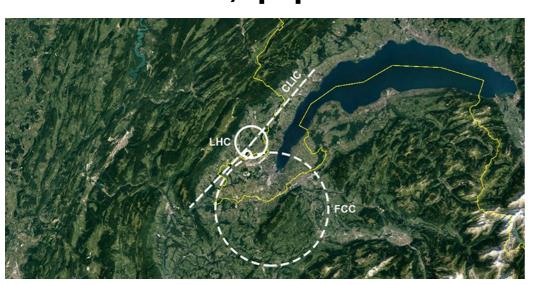


And then...? Anything after 27 km long fridge, 100 m underground LHC?

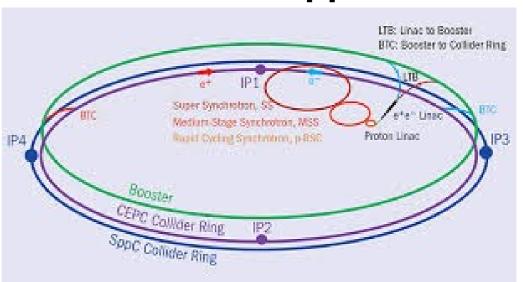
The answer is "yes"

Three-quarter century HEP projects:

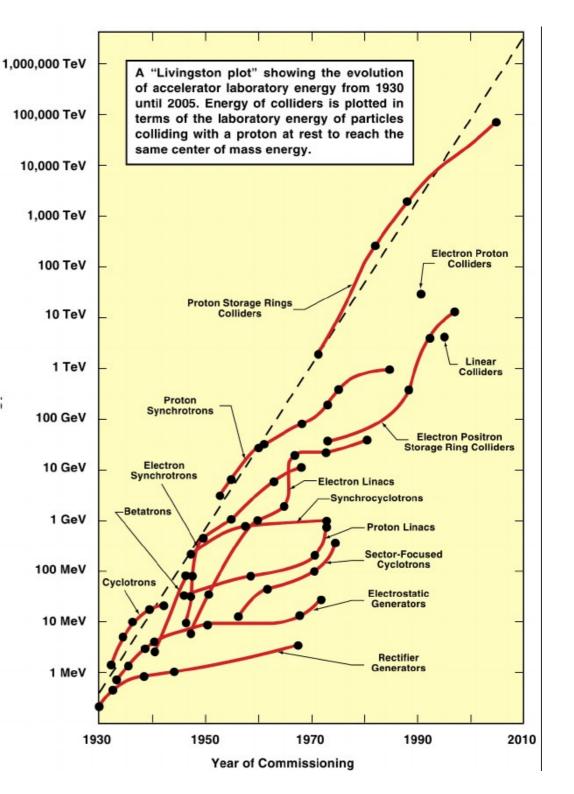
CERN's FCC-ee + FCC hh collider Circumference 100 km. exe/125GeV, pxp/100TeV



China's CEPC + CppC



THANK YOU FOR YOUR ATTENTION



BACKUP SLIDES

ELECTROSTATIC ACCELERATORS

Electrons (<100 keV) were the first projectiles [PJB] – Wimshurst type machines

- 1895 Lenard, e scattering on gas
- 1913 Franck and Hertz, excite electron shells by e bombardment

Natural (several MeV)

Prehistory

α particles were the first projectile atoms

- 1900s Rutherford figures out that α -particles are He nuclei.
- 1910 Rutherford and Madsen first smash atoms with α -particles to gain insight in the atom structure from scattering patterns. They detect the presence of a nucleus.
- 1910s Rutherford and Madsen kick out protons from various elements by that very method
- 1930s Bothe and Becker, Joliot-Curie family, Chadwick knock out neutrons by bombarding Be nuclei : $\alpha + ^9Be \longrightarrow ^{13}C + n$.

Chadwick convincingly shows that the emerging particles were neutrons.

Cosmic rays

- 1900s, Presence of radiation observed, using electroscopes and electrometers, even away from any radioactive source.
- 1932 Anderson discovers positron, predicted by Dirac
- ullet 1937 Anderson and Neddermeyer discover a particle with $220\times$ the electron mass, from cosmic ray snaps: the muon
- 1947 Lattes, Occhialini, Powell discover charged pions (today's $\bar{u}d$ and $\bar{d}u$ quark pairs)
- 1940s Discoveries of strange particles: $K^{\pm}, K_0, \Lambda, \Sigma^+$ (hadrons with one strange quark)
- The difficulty of these paths was that one had no control over the projectiles, their energies, their rate was rather scarce
- rate was rather scarce • 1928: Gamov predicts tunnneling: few 100keV H+ would suffice to penetrate nucleus • Hence the interest of accelerators for creating new particles. Milliampers of MeV particles from accelerators is equivalent to thousand-Curie radioactivity.
- 1928: Cockcroft and Walton start designing an 800 keV H+ generator, encouraged by Rutherford.

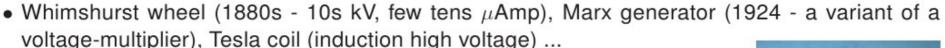
3 Electrostatic accelerators

A BRIEF INTRODUCTION

Creating strong electrostatic potential: simplest and most obvious method.
 This is a way to communicate energy to charged particles, by virtue of

$$\vec{F} = -q \, g \vec{radV}, \quad W = q \, V$$





- Two methods succeded : Crockcroft-Walton voltage multiplier,
 Van de Graaff electrostatic generator.
- Limitation on potential achievable for particle acceleration resides in
 - ohmic losses in apparatus structure proportional to potential
 - · current from ionized gas limited by saturation
 - corona discharge the major cause



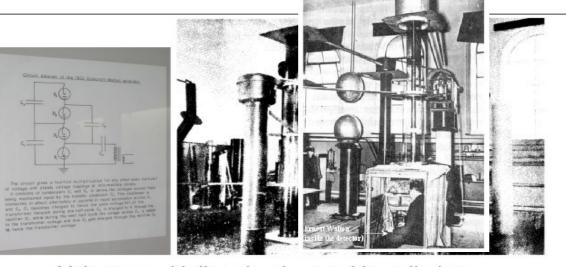


Cockcroft-Walton (1/3)

- A particular type of "voltage multiplier" (also known as "Greinacher multiplier", earlier proposed by Heinrich Greinacher, Swiss, 1919), coupled to accelerating gaps, at Cavendish Lab., 1932:
- interest of accelerator method proven by allowing first artificial nuclear transmutation, ${}^{7}_{3}Li + p \longrightarrow 2 \times \alpha + 17 \text{ MeV}$

 Only 20 years later, 1951, did they get the Nobel prize "for their pioneer work on the transmutation of atomic nuclei by artificially

accelerated atomic particles".



Voltage-multiplier circuitry and installation. ≥700 kV from a 200 kV transformer were obtained, $\sim 10 \mu A$ proton beam.

Penetration probability $1.8 \, 10^{-7}$ at 700 kV $\stackrel{10\mu A}{\longrightarrow} 10^7$ events/s.

John Douglas Cockcroft **Ernest Walton**



on the transmutation Discharge tube containing of atomic frydrogen nuclei by artificially accelerated atomic Accelerator particles. Accelerated Protons

Microscope

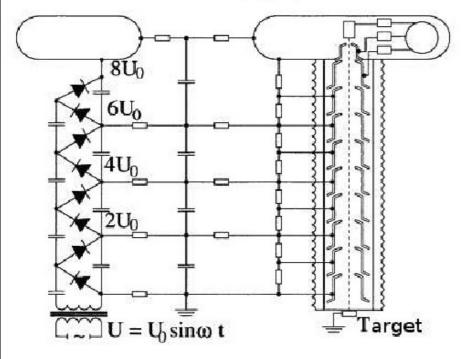
A scheme of C-W's 2-gap accelerator column. Potential for Li decay experiment was ∼700 kV

nuclei

(lithium)

Cockcroft-Walton (2/3), principle

The figure below shows principle assembly of (modern-style) Cockcroft-Walton voltage multiplier driven by AC voltage supply (left) and typical multi-electrode accelerator column (right).



Nowadays technologies allow up to $U_{total} \sim$ 5 MVolts, several tens mA DC (>100 kW beam).

Principles:

The maximum voltage is $2 \times n \times U_0$, plus a correction for current induced loss :

$$U_{total} = 2 \times n \times U_0 - \frac{2\pi I}{\omega C} \times f(n)$$

C = value of a capacitor

n = number of stages

I = ohmic loss + beam

 $f=\sim n^3$ polynomial dependence \Rightarrow limitation on n : voltage drop with I grows fast with the number of stages

It shows that large C and large ω reduce the effect of I on U_{total} .

Accelerator application : stability $\frac{\delta U_{tot}}{U_{tot}}{\approx}\frac{2\pi n^3}{RC\omega}{\approx}$ few%

Focusing: "cylindrical lens" principles

Exercise:

Take impedance $R \sim G\Omega$, capacity $C \sim nF$.

What is the order of magnitude of generator frequency $\omega/2\pi$ for $\frac{\delta U_{tot}}{U_{tot}}\sim 1\%$.

Response : kHz range.

Cockcroft-Walton (3/3)

- Cockcroft-Walton voltage multiplier is one amongst various other types of voltage multipliers
- A technique convenient in accelerator installations, still in use today in number of laboratories, at the front end of the injection chain.



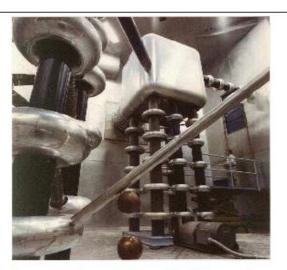
A modern version: the 810 kV, 30 mA Cockcroft-Walton injector at the PSI Mega-Watt cyclotron, using a voltage multiplier.

Exercise: value of n, U_0 ?

Resp.: n=5, $U_0 \sim 80 \text{ kV}$



Some more easy kVs...



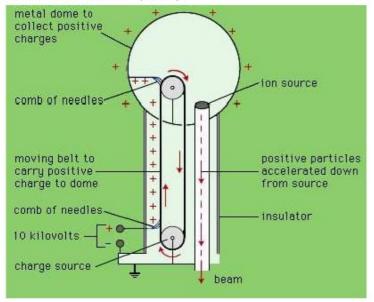
FermiLab injector (source, C-W and transfer lines are doubled for minimal down-time).

H-, 20 keV DC beam, accelerated to 750 keV prior to bunching and injection into a DTL.

And a trend, replacement by RFQ:

"[...] to reduce the maintenance requirements of the 750-keV pre-accelerator system, the replacement of the present Cockcroft-Walton accelerators with a single RFQ accelerator is proposed." (December 2008)

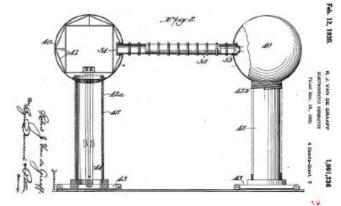
Van de Graaff (1/2)



Van de Graaff electrostatic generator, principle: + or - charges, as brought by the insulating belt, are stored at the outer surface of the bulbe. Sharp points of combs are close to, but not touching, the belt, charges are transported from and to the belt by corona effect. Potential is used to accelerate particles.



In the company of its developper...



Patent figure, Dec. 1931.



A 2×3.5 MV specimen, 1933.

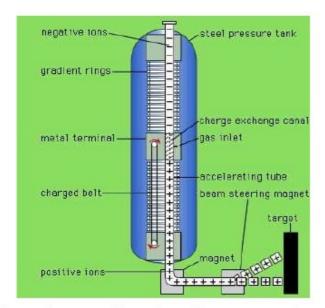
- The Van de Graaff generator is simple, easy to regulate, capable of producing high voltages and therefore high accelerations of electrons or ions (compared at that time to Cockcroft-Walton).
- It is preferred when low ripple (low energy spread) is important at megavolt potentials.
- Intensity limited to ∼mA.
- Effects limiting maximum achievable voltage are, size !, leackage, insulation, shape of electrodes...

Van de Graaff (2/2), Tandem

- There are nowadays hundreds of Van de Graaff accelerators over the world.
- Often under the form of "tandem Van de Graaff": doubles available energy, and gas pressurised (isolating gas SF6, freon, several 10⁵Pa): limit corona effects, reduce size, source and target at ground potential.

In the "Pelletron" (1960's), a pellet chain replaces the belt and induction devices replace the needle combs (yields better stability, reliability...)





Two-stage - "tandem" - pressurized Van de Graaff.



One of the two (face-to-face) stages of the 15 MV Tandem-Van de Graaff at BNL. Can accelerate 40 different types of ions.



The tandem Van de Graaff at Western Michigan University, used for basic research, student training...



20 MV tandem VdG at Tandar Lab., Argentina (above), a smaller ancestor in earlier times (below).

