## Phase Advance in Quads

Jun Ma, Roman Samulyak<br>Department of Applied Mathematics and Statistics Stony Brook University

2016.12.16

## Quads setting

- Om-0.4245m : Drift
- $0.4245 m-0.5815 m: ~ Q 1, K 1=-7.56277$
- 0.5815m-0.9745m : Drift
- $0.9745 \mathrm{~m}-1.1315 \mathrm{~m}: ~ \mathrm{Q} 2, \mathrm{~K} 1=8.50925$
- $1.1315 m-1.5245 m$ : Drift
- 1.5245m-1.6815m: Q3, K1=0.698665
- 1.6815m-2.0745m : Drift
- 2.0745m-2.2315m: Q4, K1=-8.30714
- $2.2315 m-3 m$ : Drift


## $\beta$ change



## Calculate transverse phase advance using

- Transfer matrix
- Simulation



Figure: $\beta$ change (left) and phase at initial (right).



Figure: $\beta$ change (left) and phase before Q1 (right).



Figure: $\beta$ change (left) and phase after Q1 (right).



Figure: $\beta$ change (left) and phase before Q2 (right).



Figure: $\beta$ change (left) and phase after Q2 (right).



Figure: $\beta$ change (left) and phase before Q3 (right).



Figure: $\beta$ change (left) and phase after Q3 (right).



Figure: $\beta$ change (left) and phase before Q4 (right).



Figure: $\beta$ change (left) and phase after Q4 (right).



Figure: $\beta$ change (left) and phase at final (right).

- Cold beam as background One line in transverse direction
- Cold beam with ion

Subtract background to visualize modulation signal

- Cold beam with initial kick

Subtract background to visualize modulation signal

- Cold beam with initial kick $\times 1 \mathrm{e}+6$

No need to subtract background


Figure: Phase at initial of background (left) and signal (right).



Figure: Phase before Q1 of background (left) and signal (right).



Figure: Phase after Q1 of background (left) and signal (right).


Figure: Phase before Q2 of background (left) and signal (right).


Figure: Phase after Q2 of background (left) and signal (right).


Figure: Phase before Q3 of background (left) and signal (right).


Figure: Phase after Q3 of background (left) and signal (right).


Figure: Phase before Q4 of background (left) and signal (right).


Figure: Phase after Q4 of background (left) and signal (right).



Figure: Phase at final of background (left) and signal (right).


Figure: Phase at initial of background (left) and signal (right).


Figure: Phase before Q1 of background (left) and signal (right).


Figure: Phase after Q1 of background (left) and signal (right).


Figure: Phase before Q2 of background (left) and signal (right).


Figure: Phase after Q2 of background (left) and signal (right).


Figure: Phase before Q3 of background (left) and signal (right).


Figure: Phase after Q3 of background (left) and signal (right).



Figure: Phase before Q4 of background (left) and signal (right).


Figure: Phase after Q4 of background (left) and signal (right).


Figure: Phase at final of background (left) and signal (right).



Figure: Phase at initial using transfer matrix (left) and simulation (right).



Figure: Phase before Q1 using transfer matrix (left) and simulation (right).



Figure: Phase after Q1 using transfer matrix (left) and simulation (right).


Figure: Phase before Q2 using transfer matrix (left) and simulation (right).



Figure: Phase after Q2 using transfer matrix (left) and simulation (right).



Figure: Phase before Q3 using transfer matrix (left) and simulation (right).



Figure: Phase after Q3 using transfer matrix (left) and simulation (right).



Figure: Phase before Q4 using transfer matrix (left) and simulation (right).



Figure: Phase after Q4 using transfer matrix (left) and simulation (right).


Figure: Phase at final using transfer matrix (left) and simulation (right).

