Phase Advance in Quads

Jun Ma, Roman Samulyak

Department of Applied Mathematics and Statistics Stony Brook University

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Quads setting

- 0m 0.4245m : Drift
- 0.4245m 0.5815m : Q1, K1=-7.56277
- 0.5815m 0.9745m : Drift
- 0.9745m 1.1315m : Q2, K1=8.50925
- 1.1315m 1.5245m : Drift
- 1.5245m 1.6815m : Q3, K1=0.698665
- 1.6815m 2.0745m : Drift
- 2.0745m 2.2315m : Q4, K1=-8.30714
- 2.2315m 3m : Drift

β change



Jun Ma, Roman Samulyak Phase Advance in Quads

Calculate transverse phase advance using

- Transfer matrix
- Simulation



Figure: β change (left) and phase at initial (right).

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Figure: β change (left) and phase before Q1 (right).

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Figure: β change (left) and phase after Q1 (right).

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Figure: β change (left) and phase before Q2 (right).

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Figure: β change (left) and phase after Q2 (right).

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Figure: β change (left) and phase before Q3 (right).

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Figure: β change (left) and phase after Q3 (right).

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Figure: β change (left) and phase before Q4 (right).

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Figure: β change (left) and phase after Q4 (right).

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Figure: β change (left) and phase at final (right).

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Introduction	
Using Transfer Matrix	
Using Simulation	

• Cold beam as background

One line in transverse direction

Cold beam with ion

Subtract background to visualize modulation signal

• Cold beam with initial kick

Subtract background to visualize modulation signal

Cold beam with initial kick × 1e+6
No need to subtract background



Figure: Phase at initial of background (left) and signal (right).

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Figure: Phase before Q1 of background (left) and signal (right).

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Figure: Phase after Q1 of background (left) and signal (right).

Image: Image

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Figure: Phase before Q2 of background (left) and signal (right).

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Figure: Phase after Q2 of background (left) and signal (right).

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Figure: Phase before Q3 of background (left) and signal (right).

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Figure: Phase after Q3 of background (left) and signal (right).

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Figure: Phase before Q4 of background (left) and signal (right).

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Figure: Phase after Q4 of background (left) and signal (right).

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Figure: Phase at final of background (left) and signal (right).

Image: Image

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Figure: Phase at initial of background (left) and signal (right).

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Figure: Phase before Q1 of background (left) and signal (right).

Image: Image

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Figure: Phase after Q1 of background (left) and signal (right).

Image: Image

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Figure: Phase before Q2 of background (left) and signal (right).

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Figure: Phase after Q2 of background (left) and signal (right).

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Figure: Phase before Q3 of background (left) and signal (right).

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Figure: Phase after Q3 of background (left) and signal (right).

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Figure: Phase before Q4 of background (left) and signal (right).

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Figure: Phase after Q4 of background (left) and signal (right).

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Figure: Phase at final of background (left) and signal (right).

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Introduction	
Using Transfer Matrix	
Using Simulation	With initial kick $ imes$ 1e+6



Figure: Phase at initial using transfer matrix (left) and simulation (right).

Introduction	
Using Transfer Matrix	
Using Simulation	With initial kick $ imes$ 1e+6



Figure: Phase before Q1 using transfer matrix (left) and simulation (right).

Introduction	
Using Transfer Matrix	
Using Simulation	With initial kick $ imes$ 1e+6



Figure: Phase after Q1 using transfer matrix (left) and simulation (right).

Introduction	
Using Transfer Matrix	
Using Simulation	With initial kick $ imes$ 1e+6



Figure: Phase before Q2 using transfer matrix (left) and simulation (right).

Introduction	
Using Transfer Matrix	
Using Simulation	With initial kick $ imes$ 1e+6



Figure: Phase after Q2 using transfer matrix (left) and simulation (right).

Introduction	
Using Transfer Matrix	
Using Simulation	With initial kick $ imes$ 1e+6



Figure: Phase before Q3 using transfer matrix (left) and simulation (right).

Introduction	
Using Transfer Matrix	
Using Simulation	With initial kick $ imes$ 1e+6



Figure: Phase after Q3 using transfer matrix (left) and simulation (right).

Introduction	
Using Transfer Matrix	
Using Simulation	With initial kick $ imes$ 1e+6



Figure: Phase before Q4 using transfer matrix (left) and simulation (right).

Introduction	
Using Transfer Matrix	
Using Simulation	With initial kick $ imes$ 1e+6



Figure: Phase after Q4 using transfer matrix (left) and simulation (right).

Introduction	
Using Transfer Matrix	
Using Simulation	With initial kick $ imes$ 1e+6



Figure: Phase at final using transfer matrix (left) and simulation (right).