Comparison of Modulator Simulation with Theory

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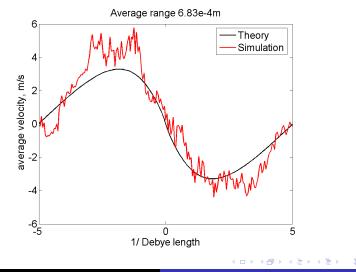
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Averaging range

- Velocity modulation changes when we measure it using different averaging range in transversal direction
- Theory uses $\sigma = 6.83e 4m$ as the averaging range

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Previous comparison

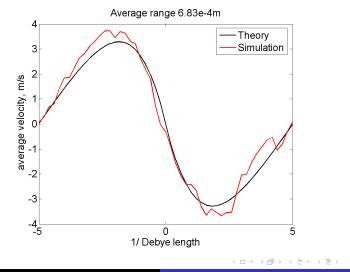


Previous comparison

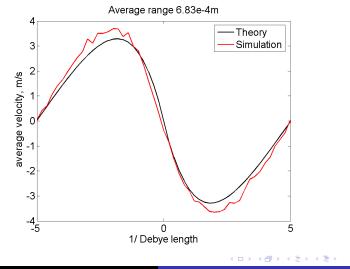
- Previous comparison was incorrect due to insufficient precision because of post-processing of data.
- Rerun simulations using different domain size but keep the same averaging range, and gather original data with full precision.

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Comparison with domain size -8e-4m to 8e-4m



Comparison with domain size -6.83e-4m to 6.83e-4m



Magnetic field of quadrupole

$$\begin{pmatrix} B_x \\ B_y \\ B_z \end{pmatrix} = -\frac{\mathsf{G}}{\mathsf{b}\mathsf{l}} \cdot \begin{pmatrix} B_{\mathsf{fiinge},x} \left(\mathsf{b}\mathsf{l} x, \mathsf{b}\mathsf{l} y, \mathsf{b}\mathsf{l} \left(z - \frac{1}{2}L \right) \right) + B_{\mathsf{fiinge},x} \left(\mathsf{b}\mathsf{l} x, \mathsf{b}\mathsf{l} y, \mathsf{b}\mathsf{l} \left(-z - \frac{1}{2}L \right) \right) \\ B_{\mathsf{fiinge},y} \left(\mathsf{b}\mathsf{l} x, \mathsf{b}\mathsf{l} y, \mathsf{b}\mathsf{l} \left(z - \frac{1}{2}L \right) \right) + B_{\mathsf{fiinge},y} \left(\mathsf{b}\mathsf{l} x, \mathsf{b}\mathsf{l} y, \mathsf{b}\mathsf{l} \left(-z - \frac{1}{2}L \right) \right) \\ B_{\mathsf{fiinge},z} \left(\mathsf{b}\mathsf{l} x, \mathsf{b}\mathsf{l} y, \mathsf{b}\mathsf{l} \left(z - \frac{1}{2}L \right) \right) - B_{\mathsf{fiinge},z} \left(\mathsf{b}\mathsf{l} x, \mathsf{b}\mathsf{l} y, \mathsf{b}\mathsf{l} \left(-z - \frac{1}{2}L \right) \right) \end{pmatrix}$$

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Magnetic field of quadrupole (continue)

$$\mathbf{B}_{\text{fringe}}(x, y, z) = \frac{1}{4} \begin{pmatrix} -y - 2\arctan\left(-\frac{\sin(y)}{e^{-z} + \cos(y)}\right) + \frac{y\sinh(z)}{\cos(x) + \cosh(z)} \\ -x - 2\arctan\left(-\frac{\sin(x)}{e^{-z} + \cos(x)}\right) + \frac{x\sinh(z)}{\cos(y) + \cosh(z)} \\ \frac{y\sin(x)}{\cos(x) + \cosh(z)} + \frac{x\sin(y)}{\cos(y) + \cosh(z)} \end{pmatrix}$$

Magnetic field of quadrupole (continue)

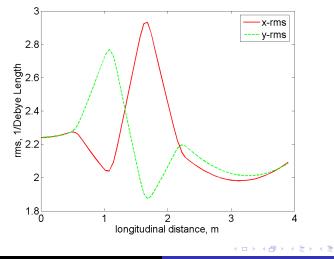
•
$$G = K = K_1 \cdot B\rho$$

•
$$b_1 = \pi/r_{bore}$$

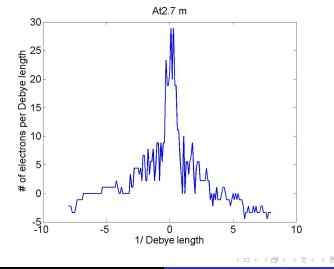
•
$$r_{bore} = 3cm$$

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RMS change due to quadrupoles

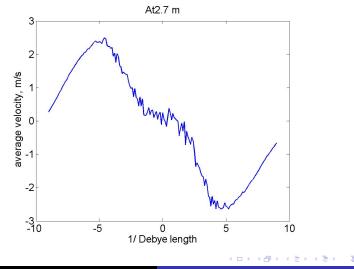


Modulator, longitudinal number distribution

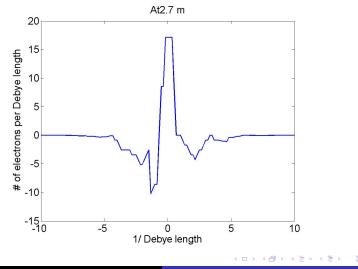


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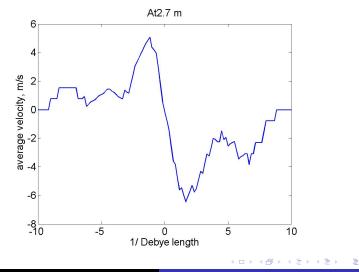
Modulator, longitudinal velocity distribution



Modulator, transversal number distribution



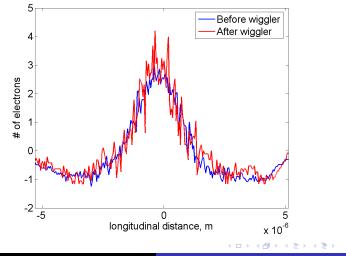
Modulator, transversal velocity distribution



- Run modulator simulations using 1/10 of the previous electron number density
- Take the output of modulator as input of wiggler
- Increase wiggler magnetic field strength by 5 times (from 0.2T to 1.0T).

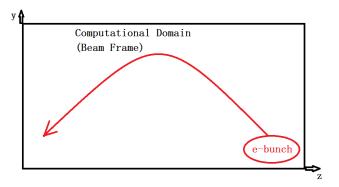
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Wiggler simulation



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Motion of electron bunch



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Motion of electron bunch

• Stronger wiggler magnetic field makes electron bunch move further along negative z direction, which requires larger computational domain.

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